

# 4 Star Formation Relations (+ Strengthened Cluster Survival) With One Single Model

Geneviève Parmentier

Astronomisches-Rechen Institut  
Zentrum für Astronomie Heidelberg

Germany



UNIVERSITÄT  
HEIDELBERG  
ZUKUNFT  
SEIT 1386



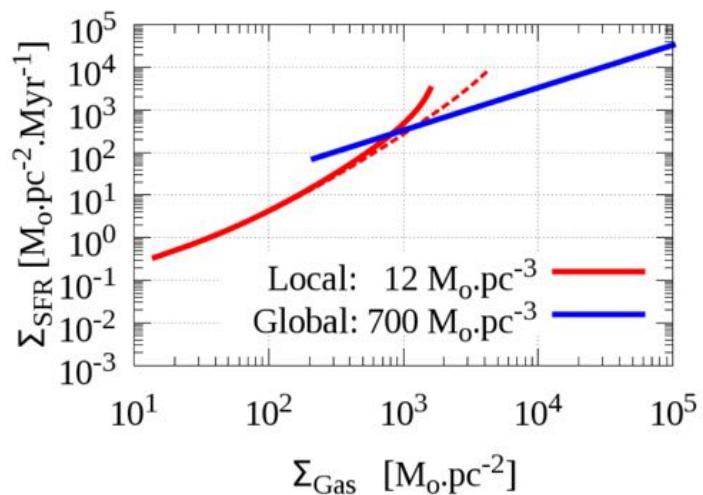
# Outline

Star cluster formation  
in centrally-concentrated  
molecular clumps



## A. Gas-embedded systems

➤ What star formation relations  
characterize such systems?





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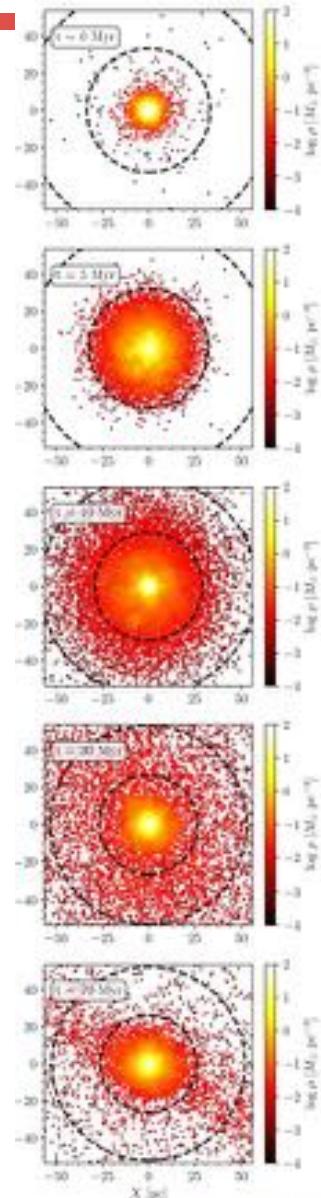
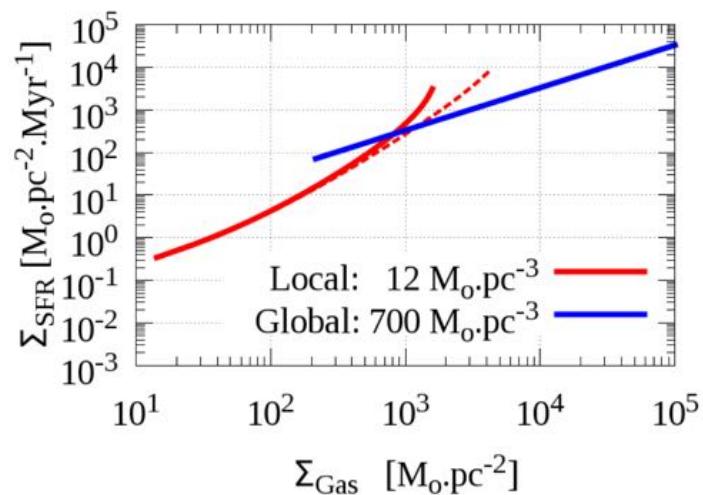


## B. Gas-free systems

➤ When the residual  
star-forming gas is  
gone, how do such  
systems evolve ?

## A. Gas-embedded systems

➤ What star formation relations  
characterize such systems?





# First Star Formation Relation (Volume/Theory)

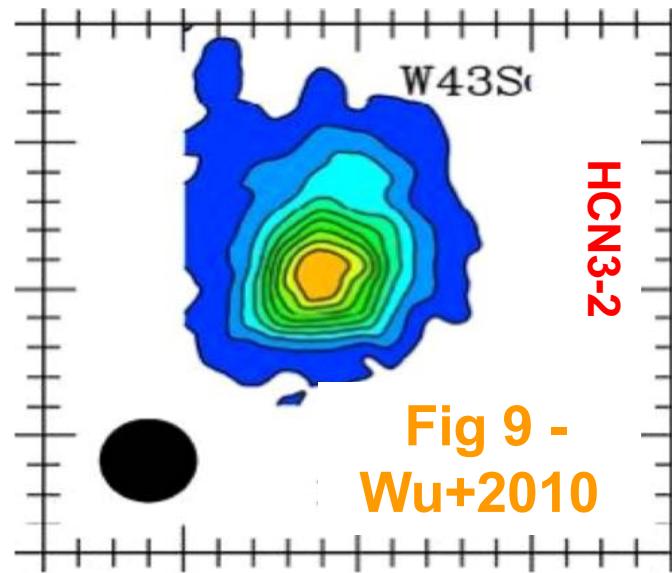
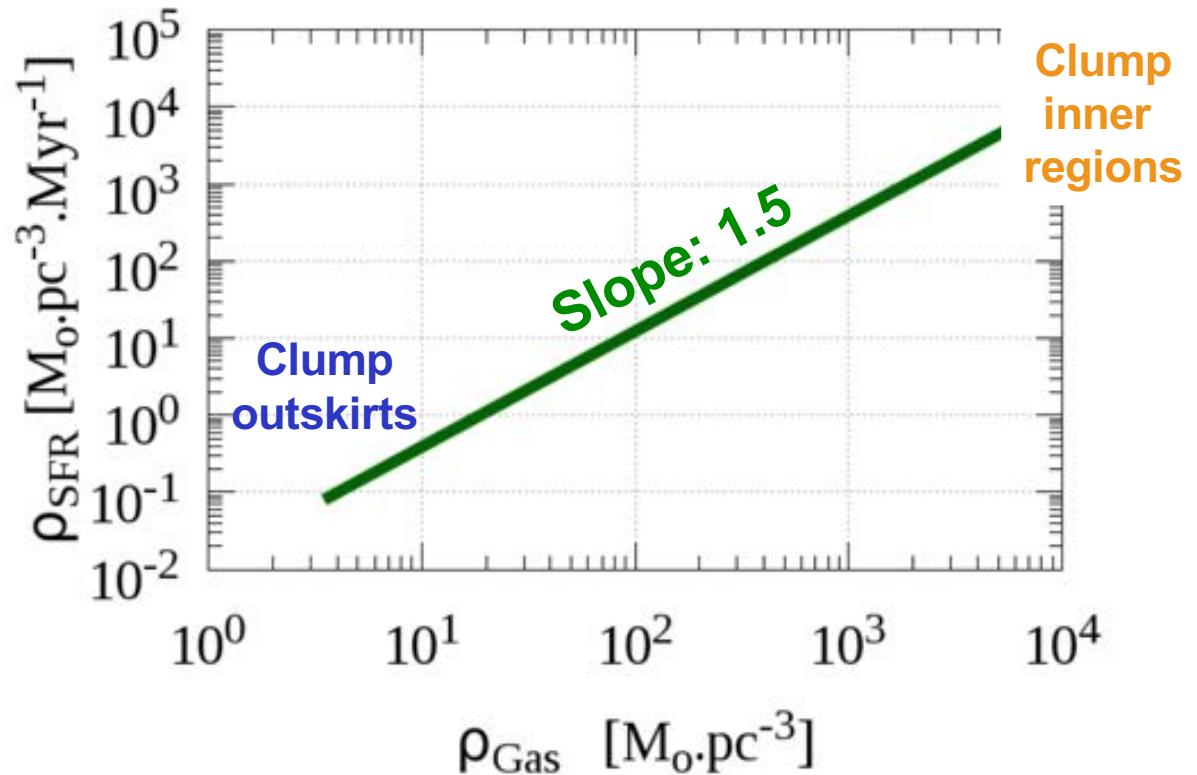


Fig 9 -  
Wu+2010



- Molecular clumps have volume density gradients
- If stars form with a constant star formation efficiency per free-fall time,  $\epsilon_{ff}$ , the volumetric star formation relation is a power-law of slope 3/2
- Shell-by-shell representation
- Local star formation relation

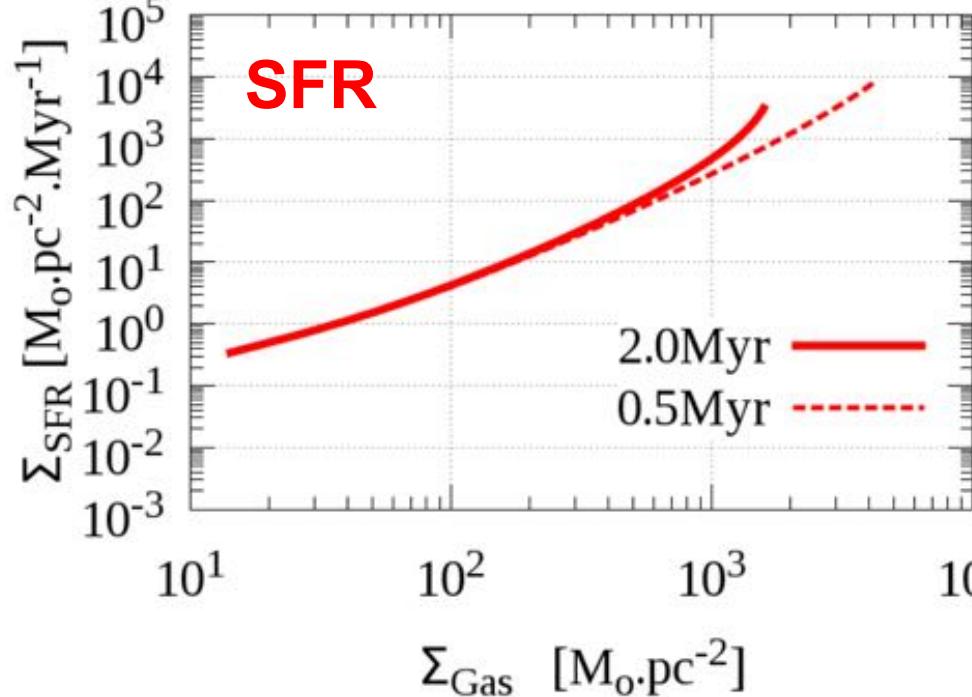
$$\rho_{SFR} = \frac{\epsilon_{ff} \rho_{gas}}{\tau_{ff}}$$

L.  $\rho_{SFR} \propto \rho_{gas}^{1.5}$





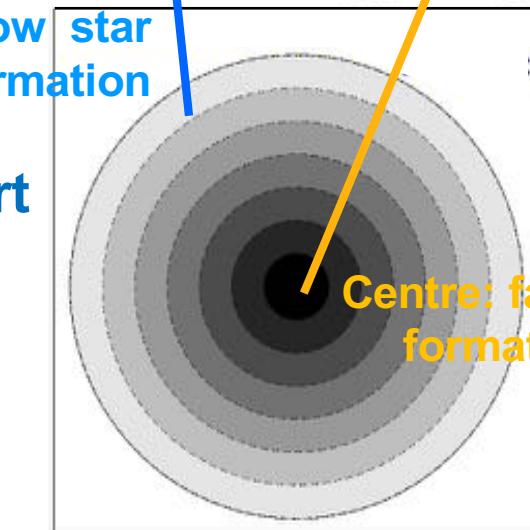
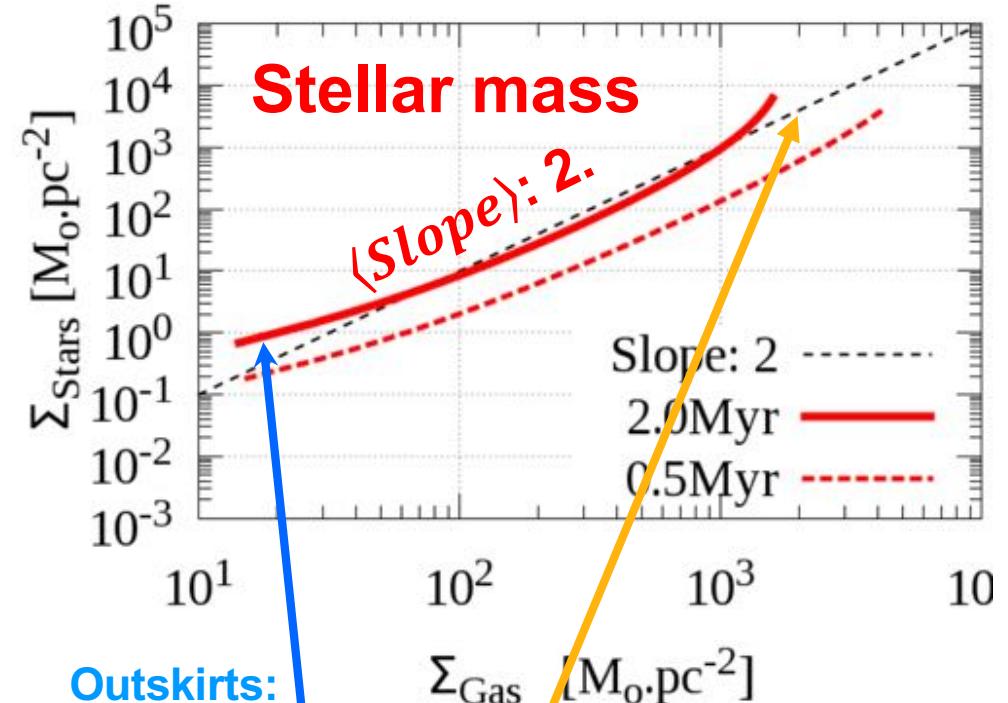
# Second Star Formation Relation (Surface/Observ.)



$$\text{II. } \Sigma_{SFR} \propto \Sigma_{\text{gas}}^2$$

- Steeper than its volumetric counterpart
- Contour-by-contour representation
- Local star formation relation

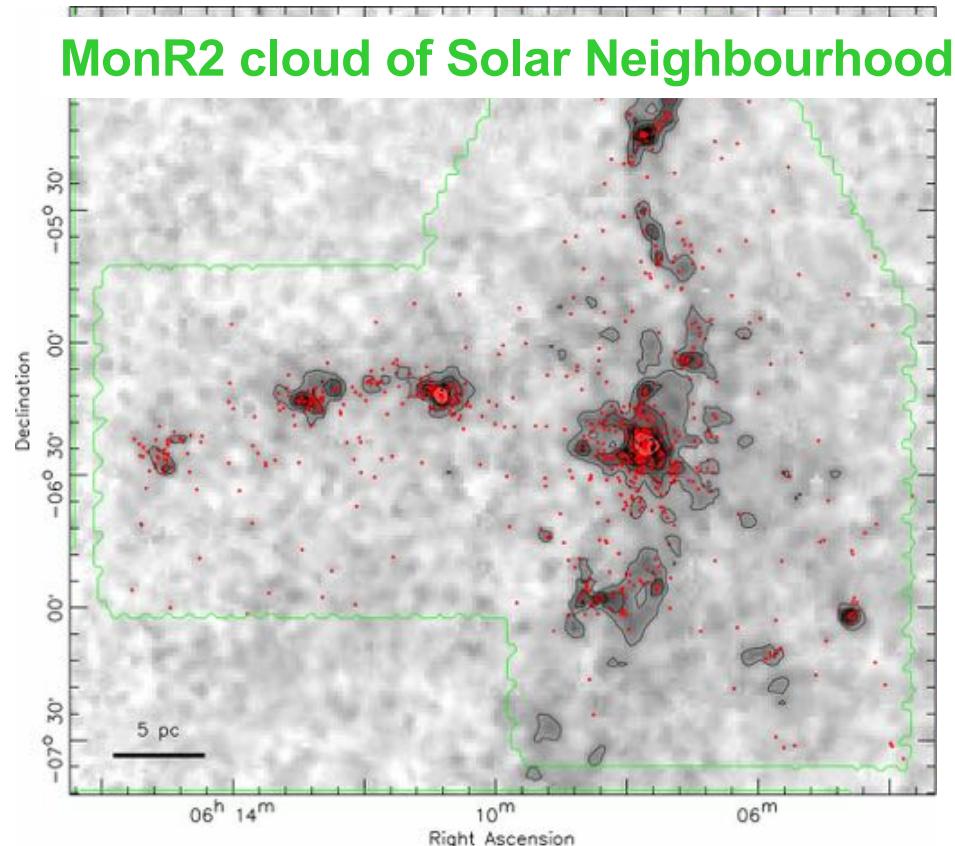
Parmentier & Pfalzner (2013)



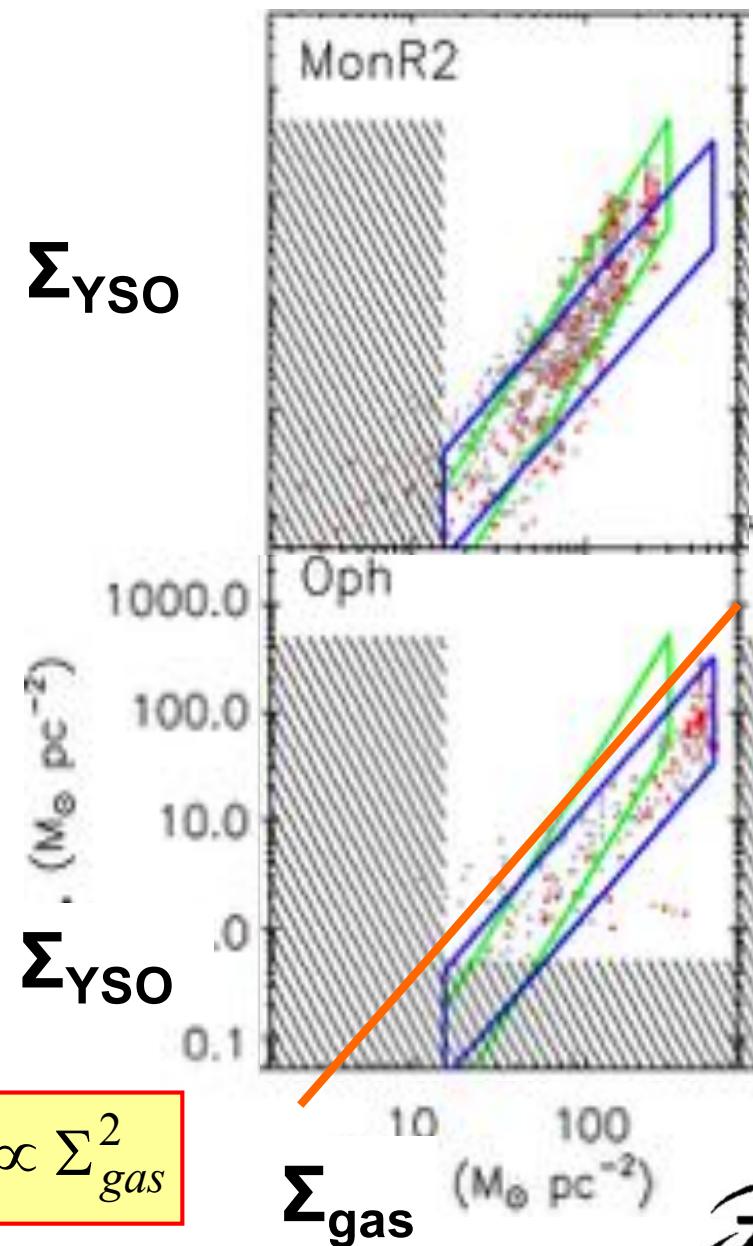


# Sol. N. Molecular Clouds Show Quadratic SF Relations

Fig. 1, Gutermuth+ (2011)



$$\Sigma_{YSO} \propto \Sigma_{gas}^2$$





# Sol. N. Molecular Clouds Show Quadratic SF Relations

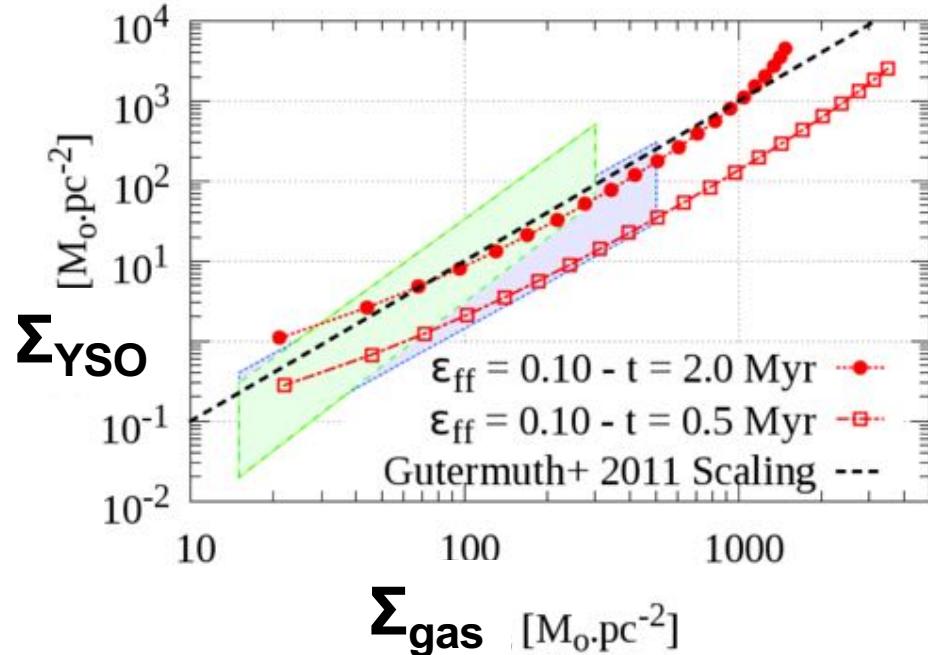


Fig 3, Parmentier & Pfalzner (2013)

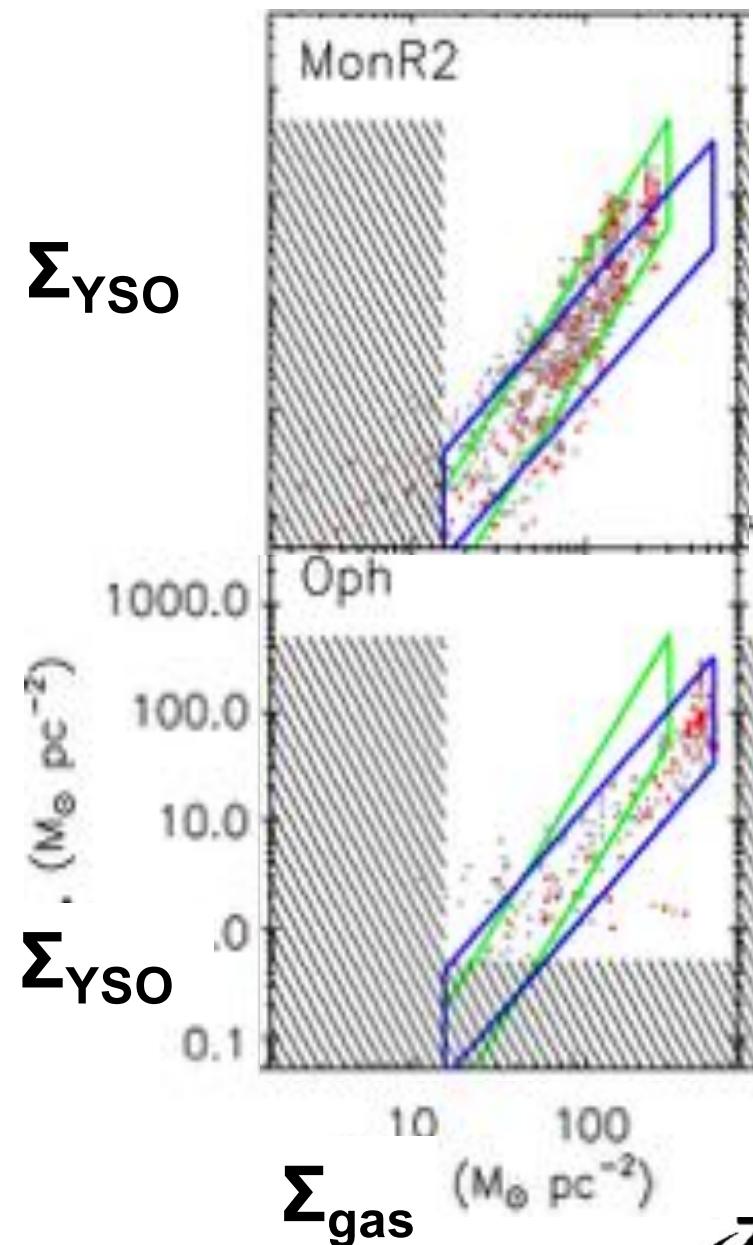


Fig. 9, Gutermuth+ (2011)

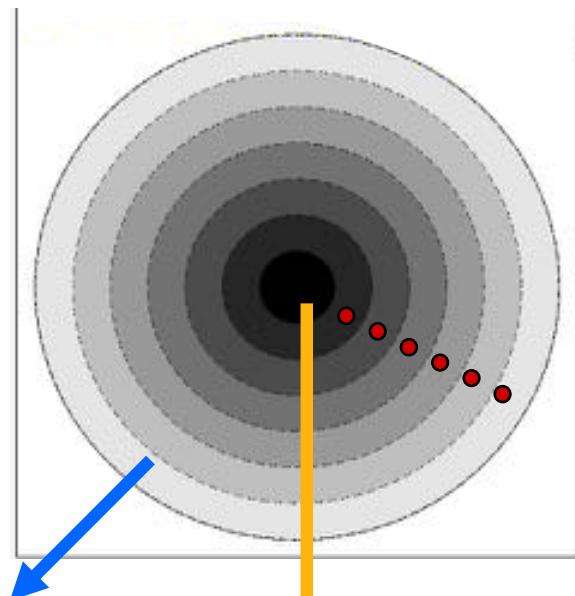


# From a Local SF Relation ...

## Local perspective:

- Contour-by-contour basis
- One clump is enough

Clump distance: e.g. 500 pc



Outskirts:  
slow  
star  
formation

Centre:  
fast  
star  
formation

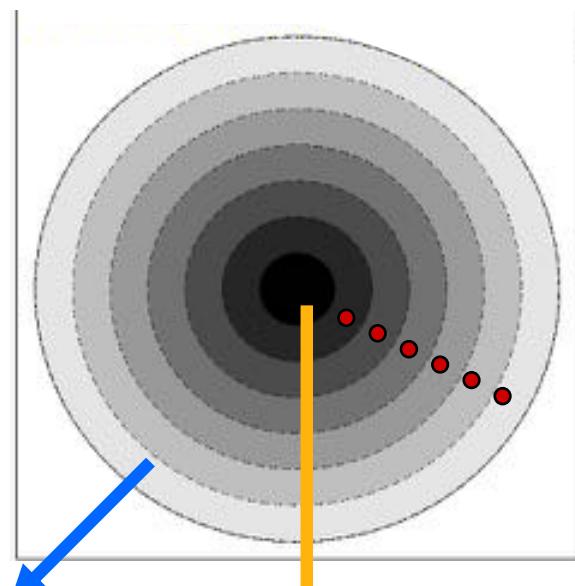


# ... to a Global (= Third) SF Relation

## Local perspective:

- Contour-by-contour basis
- One clump is enough

Clump distance: e.g. 500 pc



Outskirts:  
slow  
star  
formation

Centre:  
fast  
star  
formation

Clump at a distance where it cannot be resolved

$(\Sigma_{gas}^{glob}, \Sigma_{SFR}^{glob})$

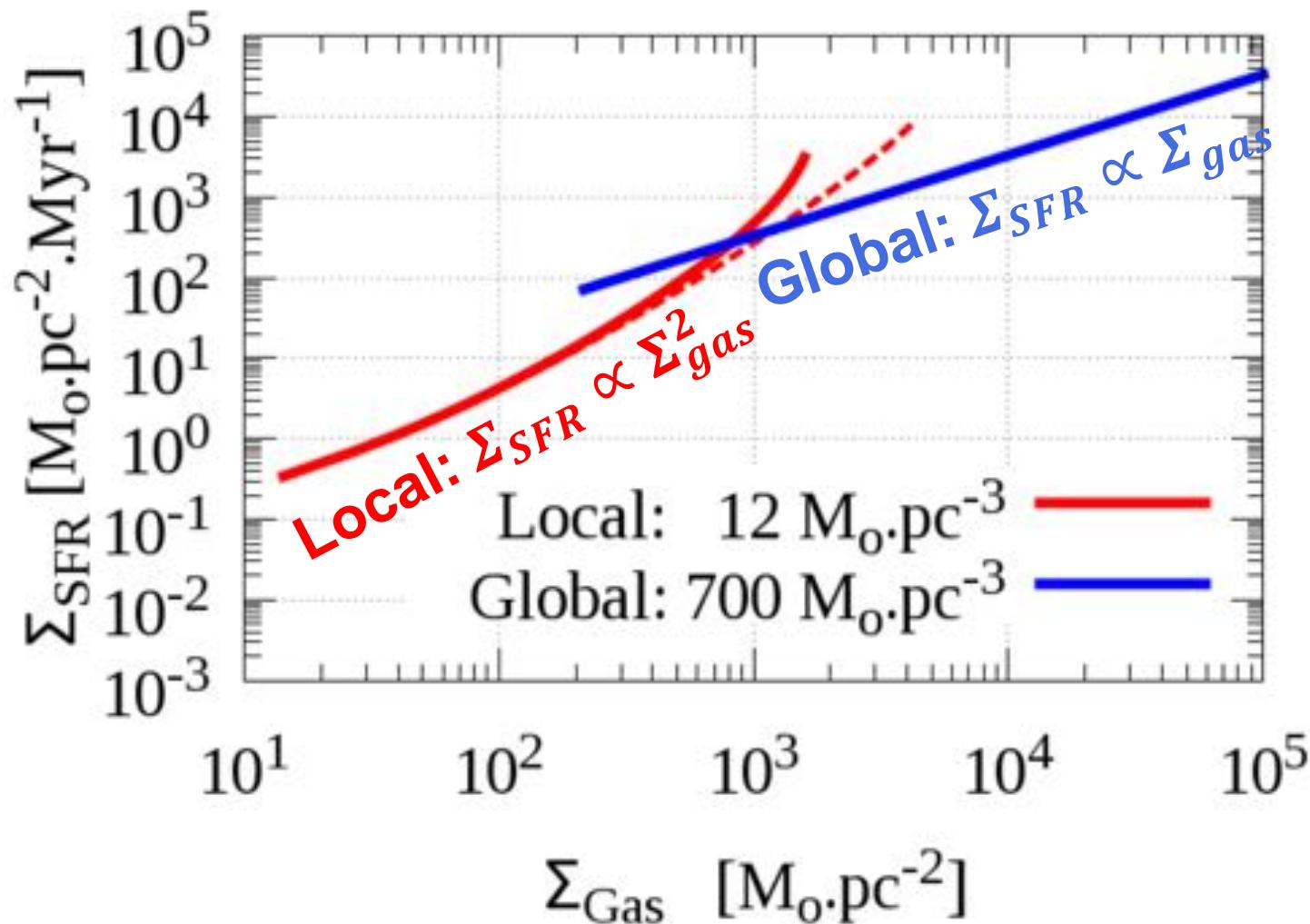
## Global perspective:

- A population of clumps is needed
- e.g. HCN(1-0) molecular clumps
- To first order: common free-fall time
  - Slope: 1
  - Third / linear SF relation

$$\text{III. } \Sigma_{SFR} \propto \Sigma_{gas}$$

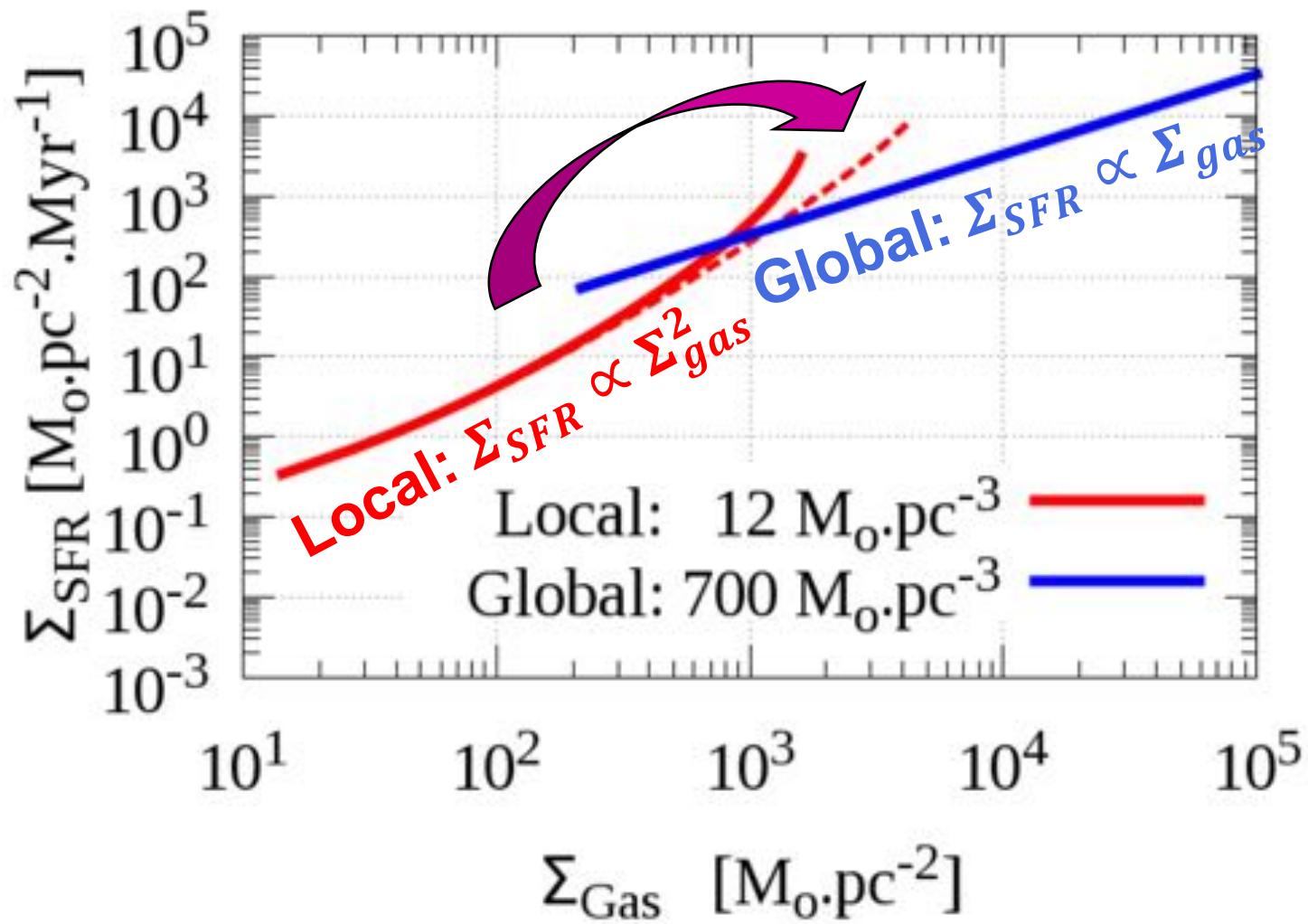


# Composite SF Relation: II + III



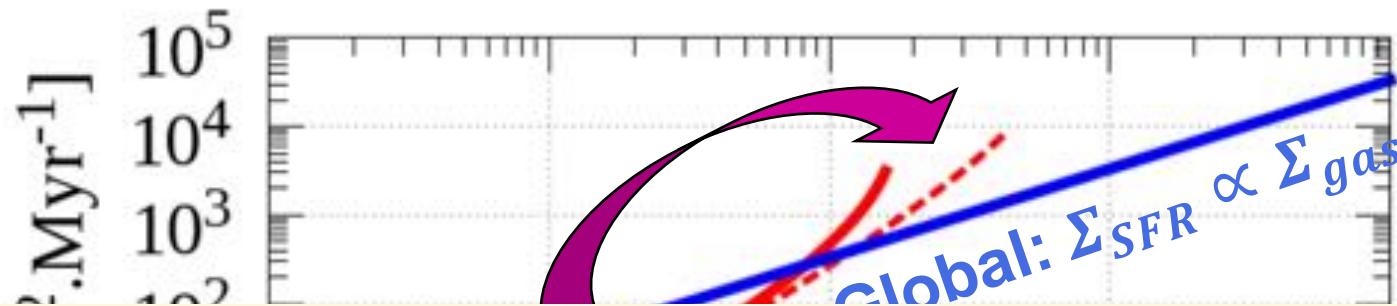


# Break-Point in Composite SF Relation

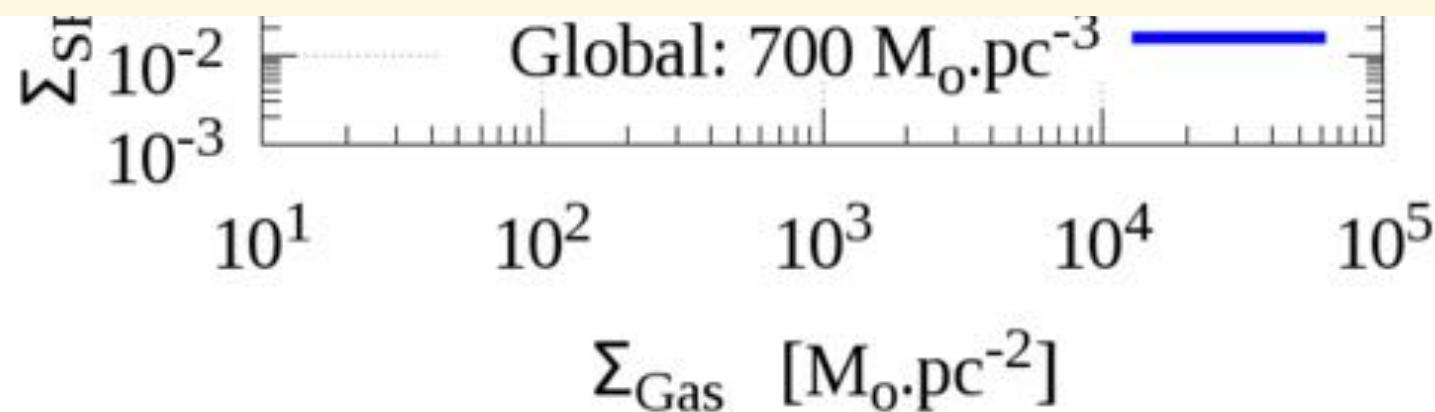




# Break-Point in Composite SF Relation



## Mind the step !





# Break-Point in Composite SF Relation

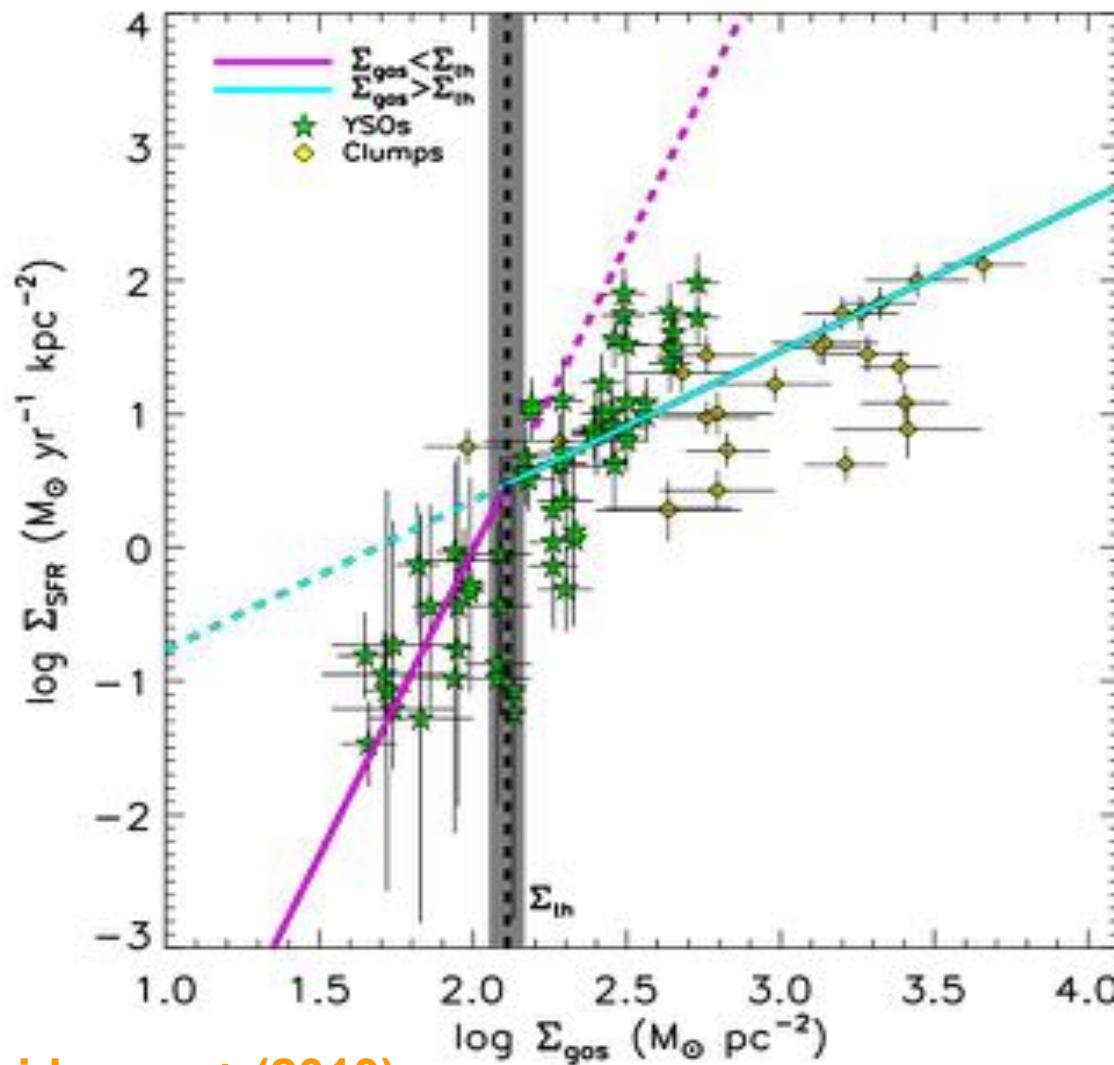


Fig. 10, Heiderman+ (2010)



# Break-Point in Composite SF Relation

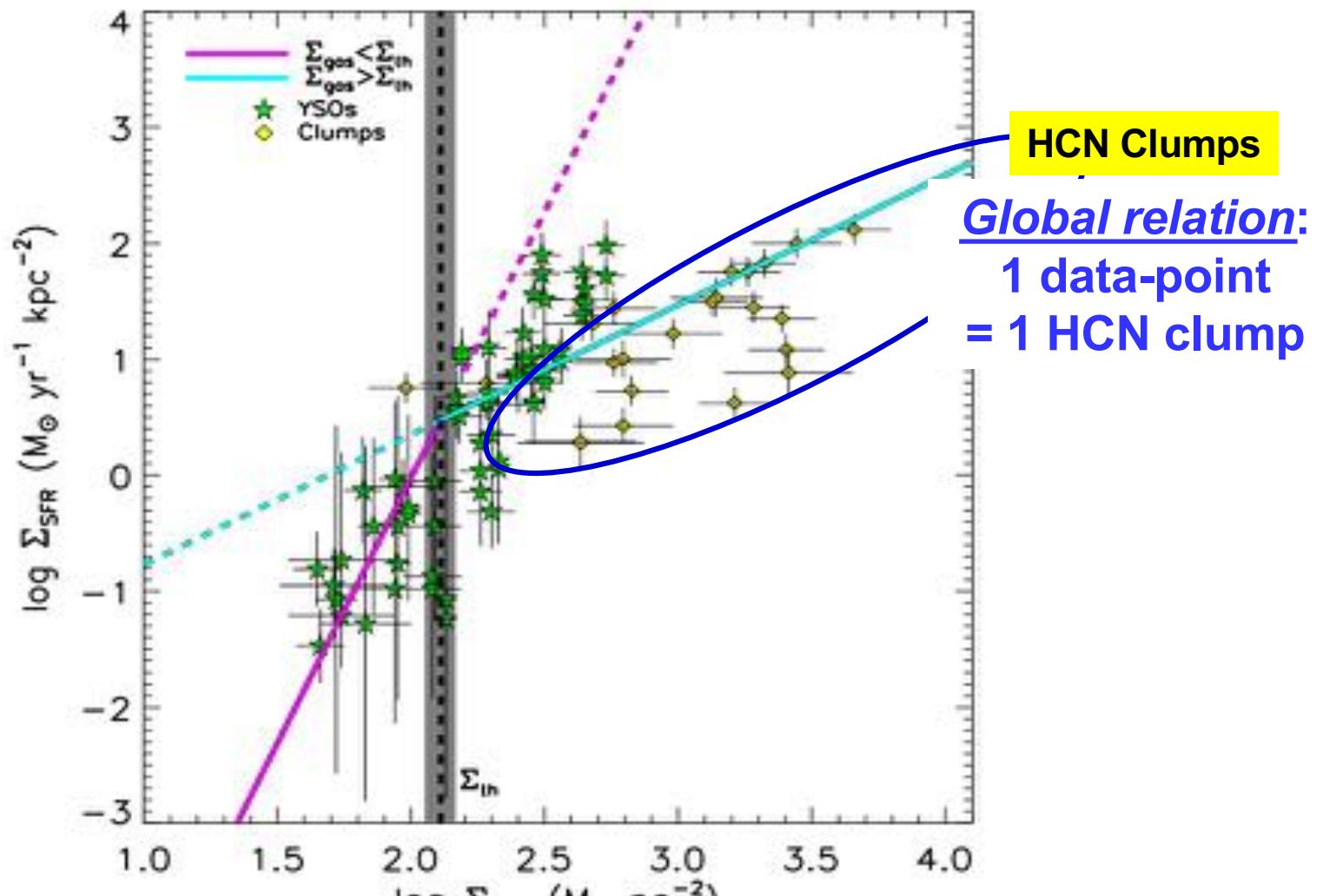


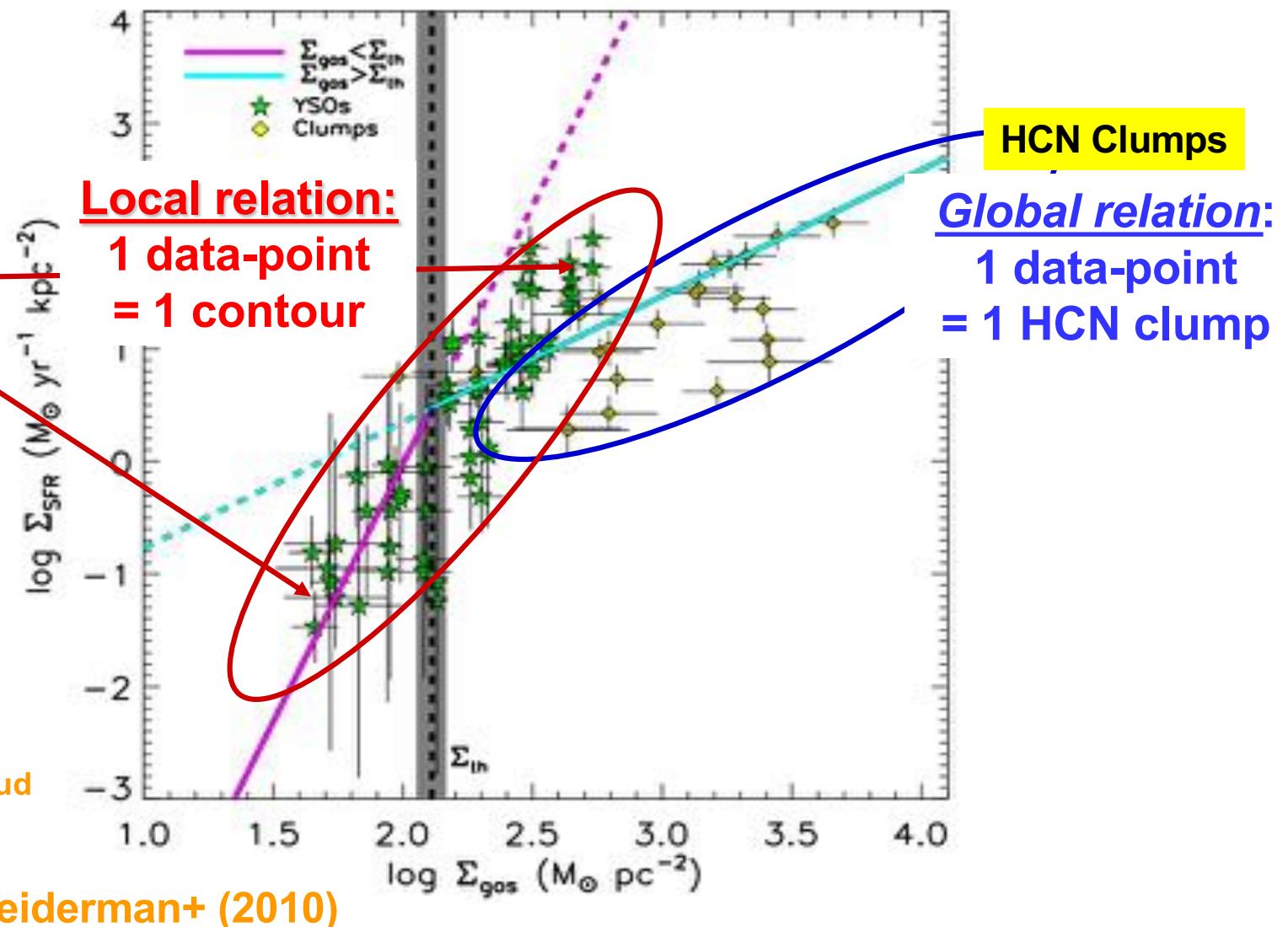
Fig. 10, Heiderman+ (2010)



# Break-Point in Composite SF Relation



Perseus molecular cloud



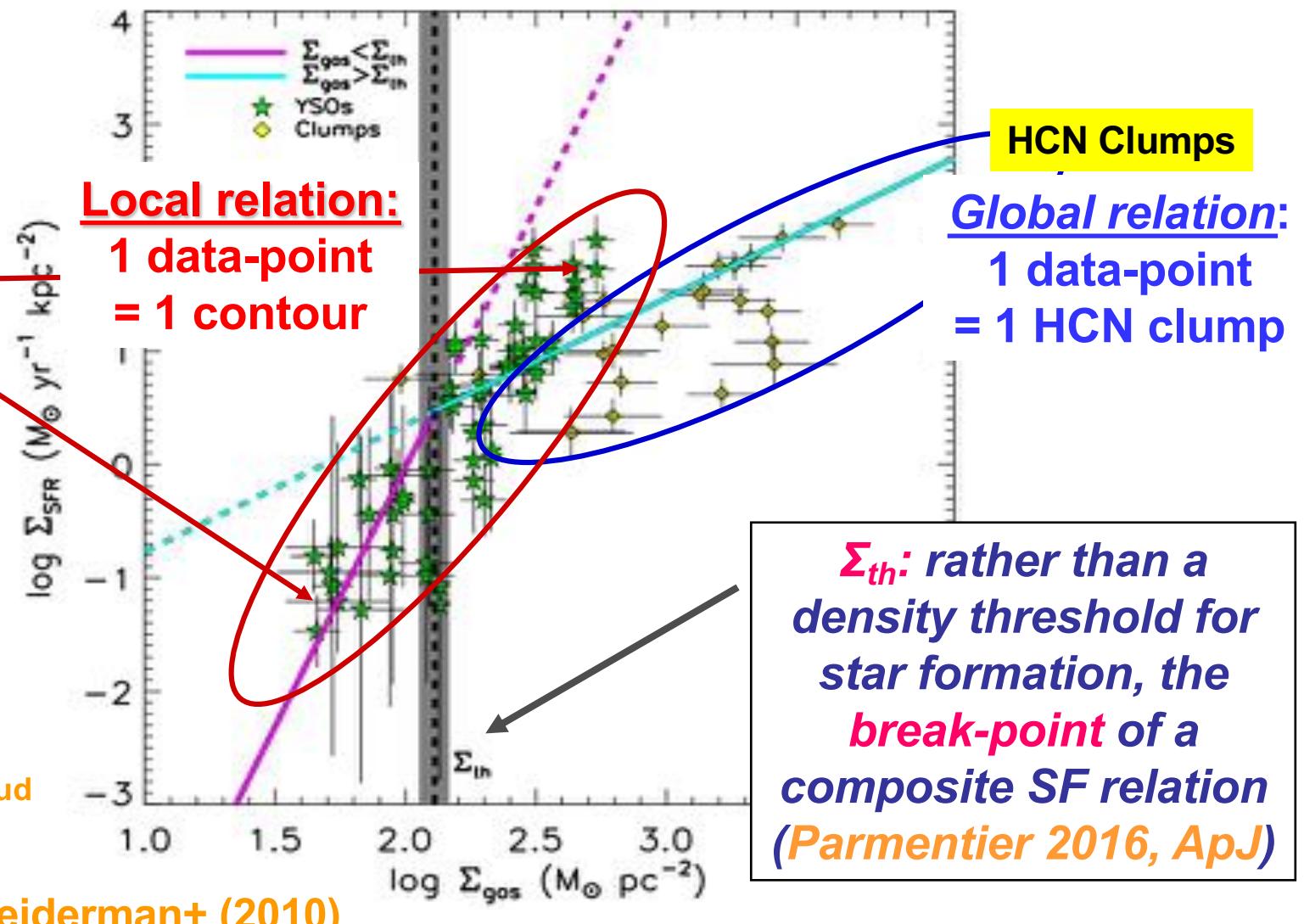
Figs 2 & 10, Heiderman+ (2010)



# Interpretation of Break-Point



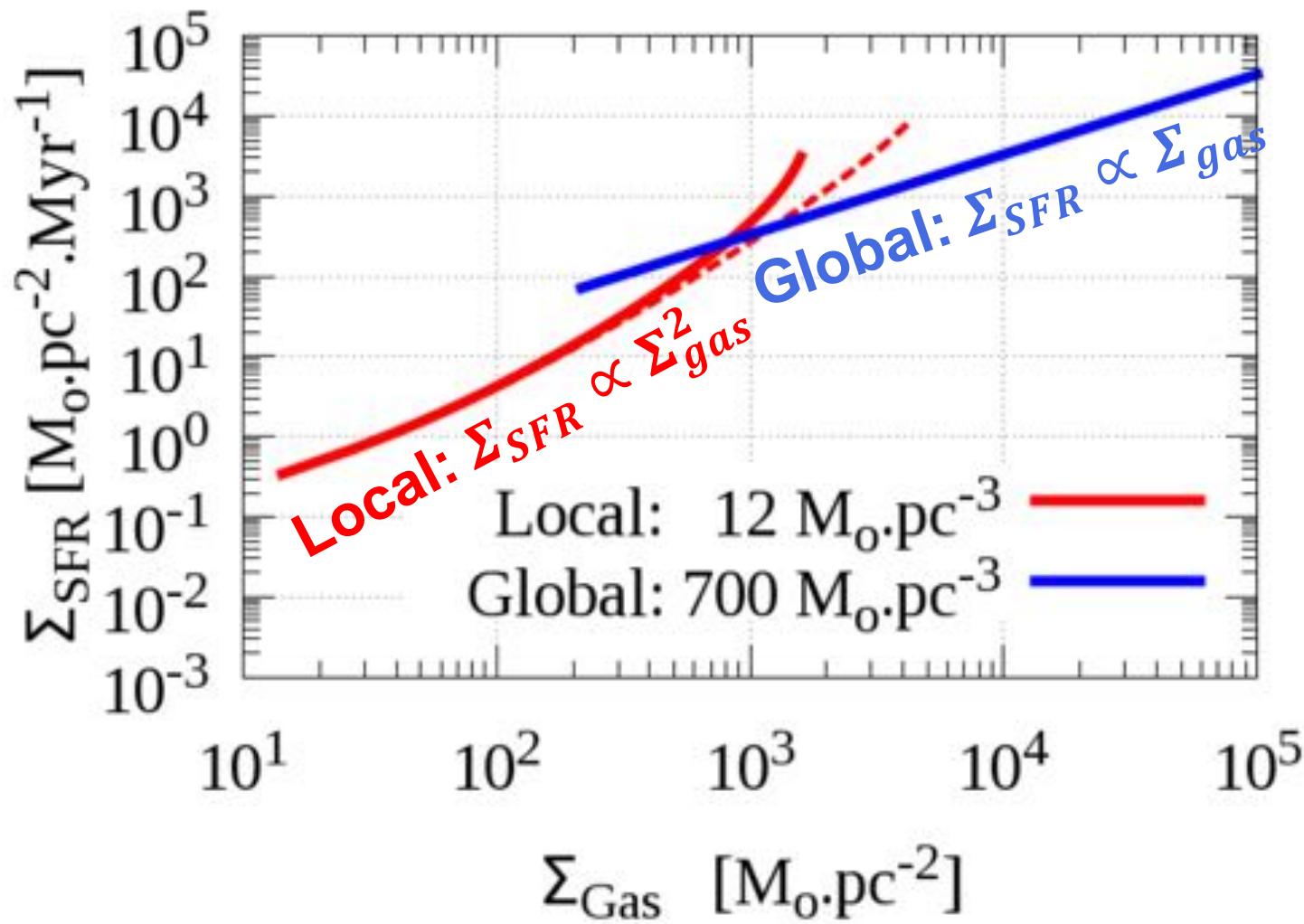
Perseus molecular cloud



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# Composite SF Relation: II + III

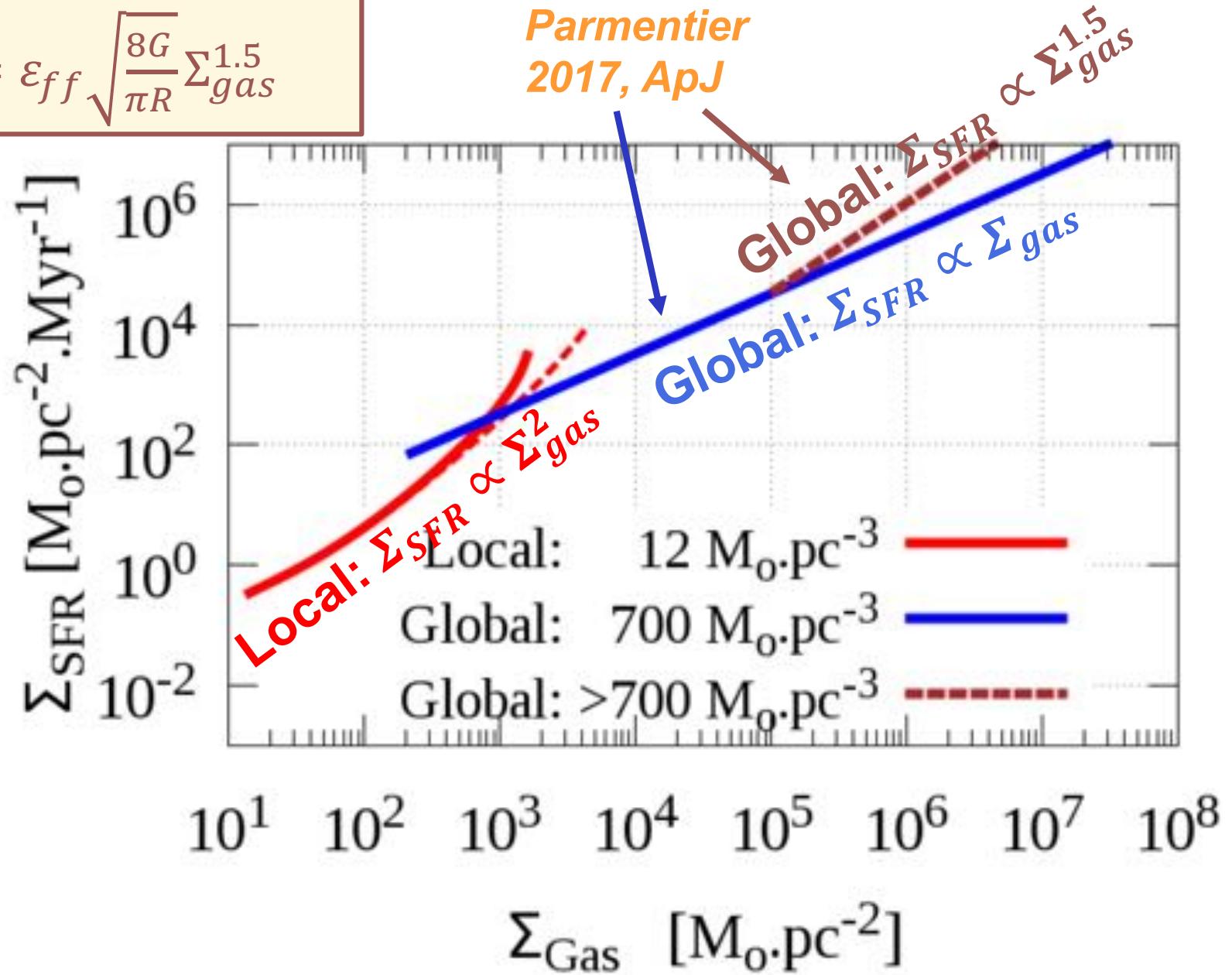




## Fourth SF Relation (the very dense gas)

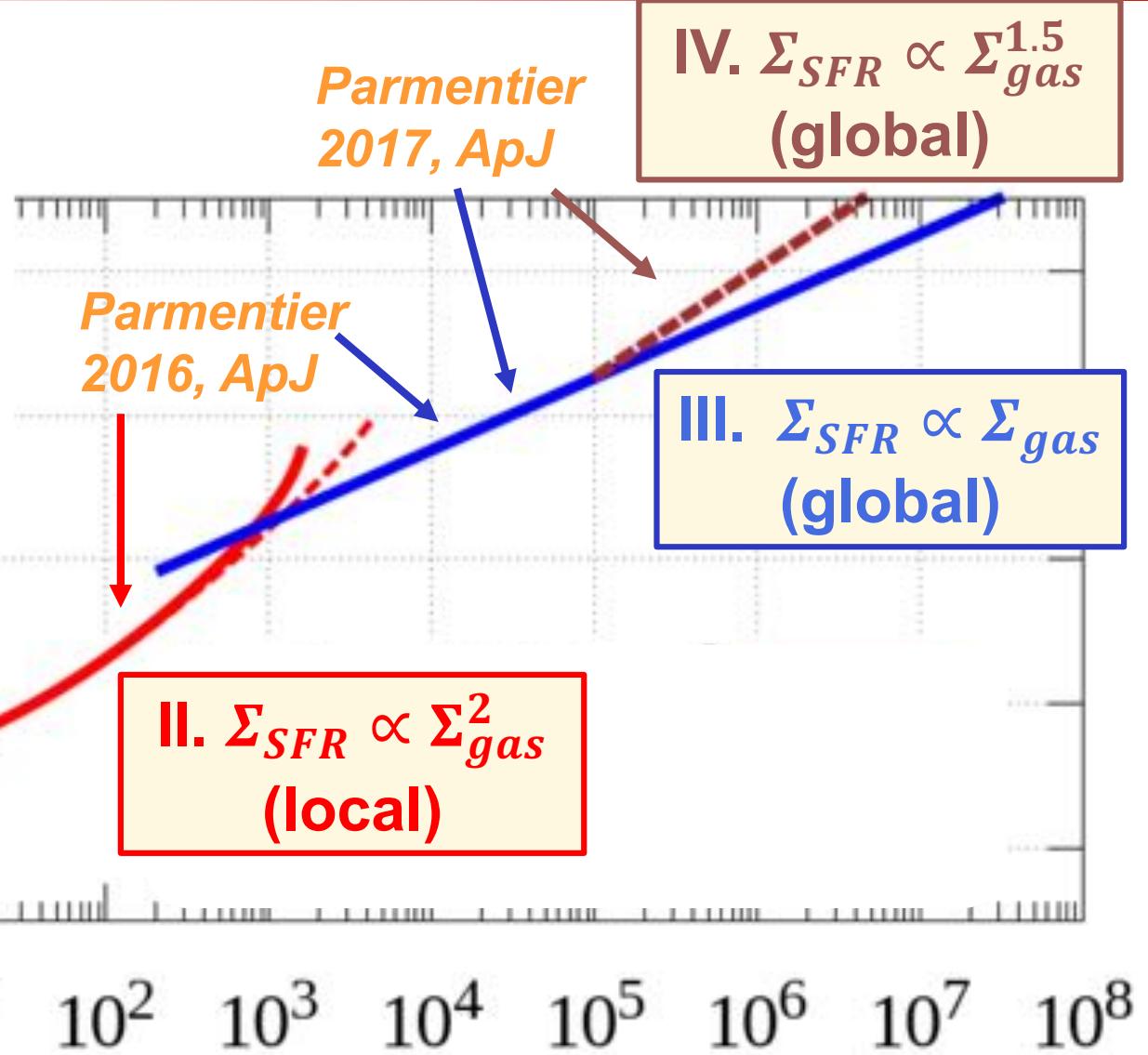
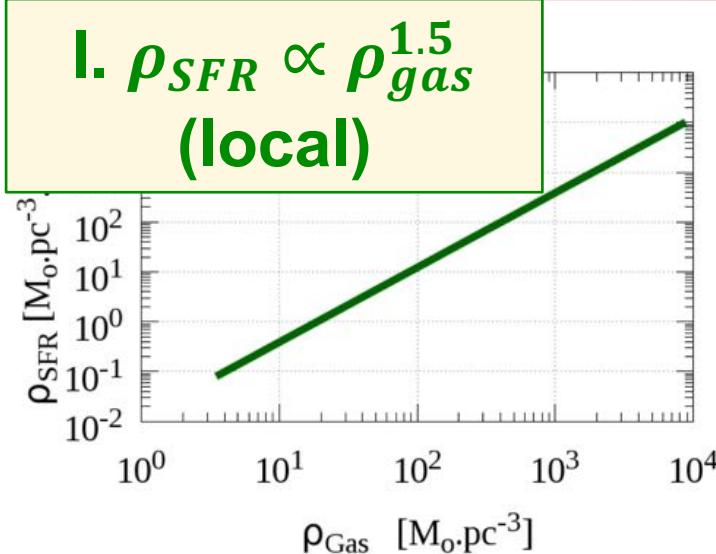
$$\text{IV. } \Sigma_{SFR} = \varepsilon_{ff} \sqrt{\frac{8G}{\pi R}} \Sigma_{gas}^{1.5}$$

Parmentier  
2017, ApJ





# 4 Star Formation Relations for Molecular Clumps



See also

Elmegreen 2018, ApJ

$\Sigma_{Gas} [M_\odot \cdot pc^{-2}]$



# Star Formation Relations and Co.

Shell – by – shell :

$$\rho_{SFR} \approx \varepsilon_{ff} \frac{\rho_{gas}}{\tau_{ff}} \propto \varepsilon_{ff} \frac{\rho_{gas}}{(\rho_{gas})^{-1/2}} \propto \rho_{gas}^{3/2}$$

Contour – by – contour :

$$\Sigma_{SFR} \approx \Sigma_{gas}^2$$

Clump-by-clump (constant  $\langle \rho_{gas} \rangle$ ):

$$\langle \Sigma_{SFR} \rangle \propto \langle \Sigma_{gas} \rangle^1$$

Clump-by-clump (increasing  $\langle \rho_{gas} \rangle$ ):

$$\langle \Sigma_{SFR} \rangle \propto \langle \Sigma_{gas} \rangle^{3/2}$$



# Star Formation Relations and Co.

Shell – by – shell :

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Contour – by – contour :

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Clump-by-clump (constant  $\langle \rho_{gas} \rangle$ ):

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Clump-by-clump (increasing  $\langle \rho_{gas} \rangle$ ):

$$\langle \Sigma_{SFR} \rangle \propto \langle \Sigma_{gas} \rangle^{3/2}$$

- Constant  $\epsilon_{ff}$ : the slope is not necessarily 1.5
- Slope  $\neq 1.5$  does **not** necessarily discard a scenario in which star formation proceeds with a constant  $\epsilon_{ff}$



# Star Cluster Evolution after Gas Expulsion

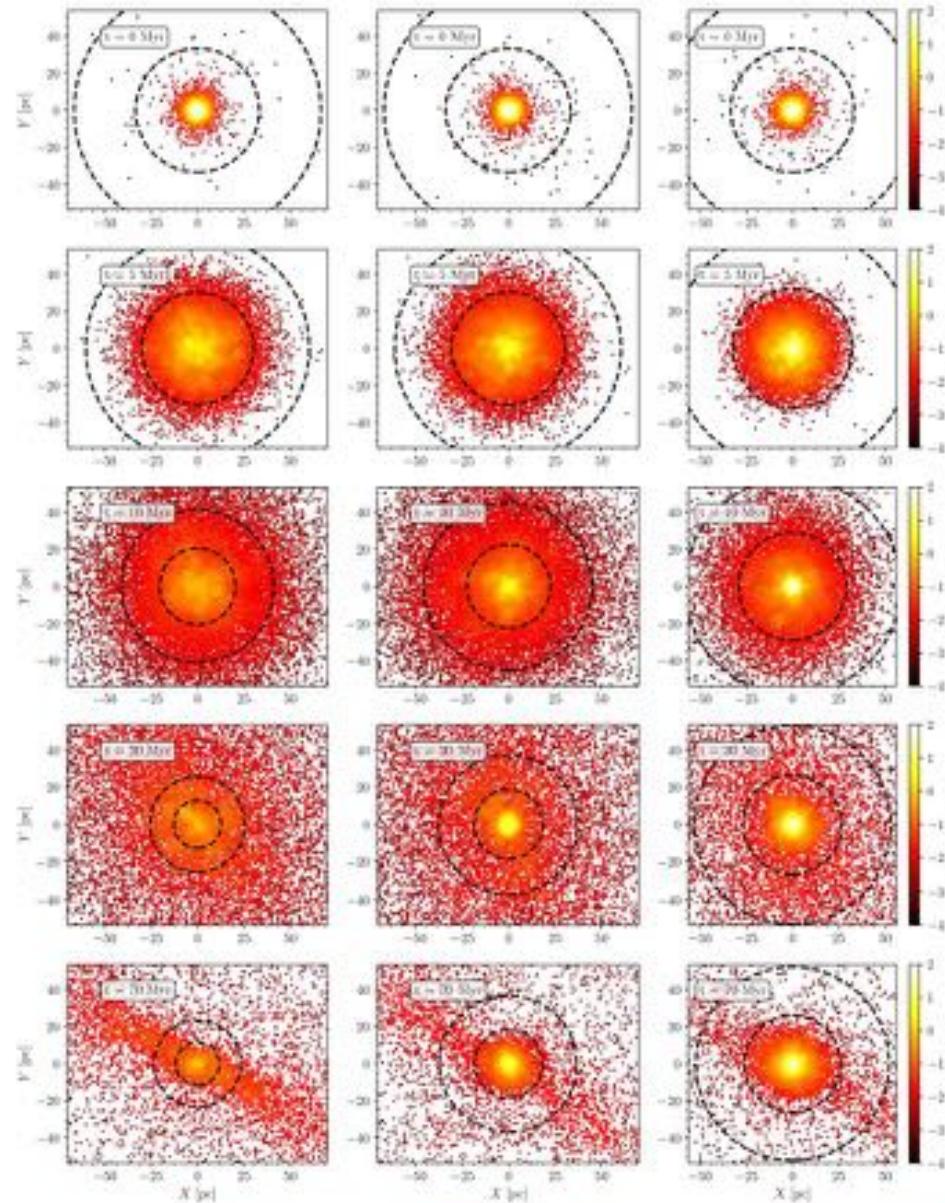
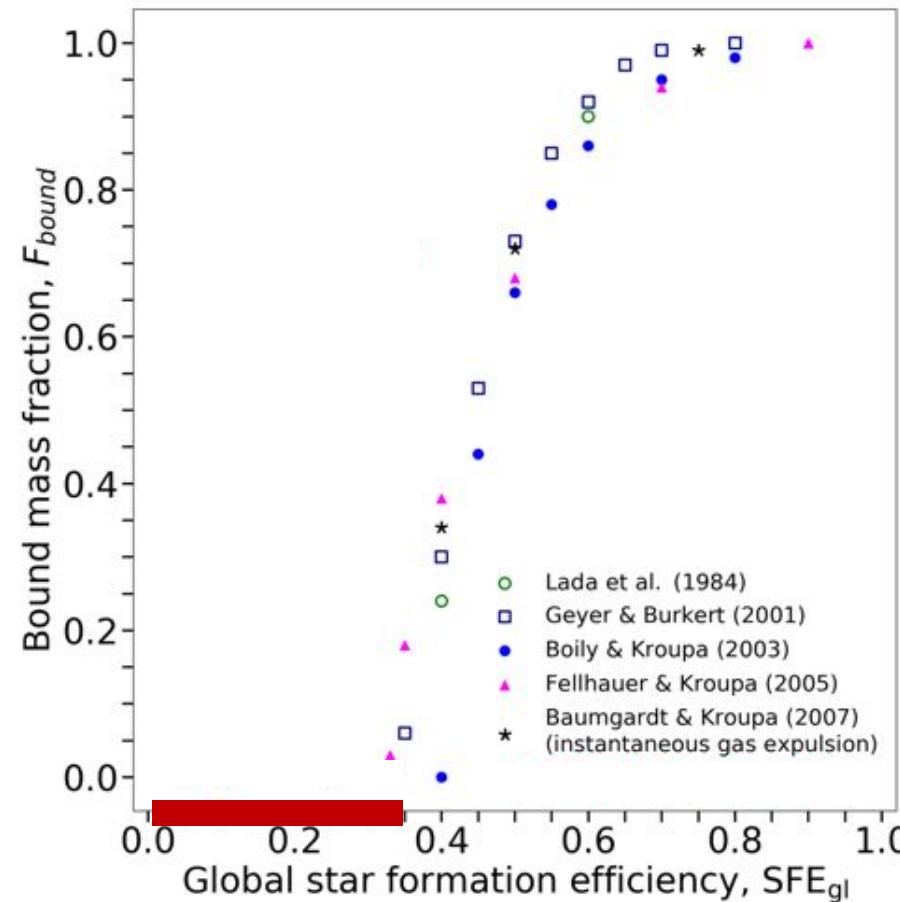


Fig 1,  
Shukirgaliyev,  
Parmentier,  
Just & Berczik  
(2018)



# Short-Term Evolution

## Instantaneous gas expulsion



- A decade ago: star clusters formed with an SFE less than 1/3 do not survive (aka cluster infant mortality)



# Back to the Second (Local) SF Relation

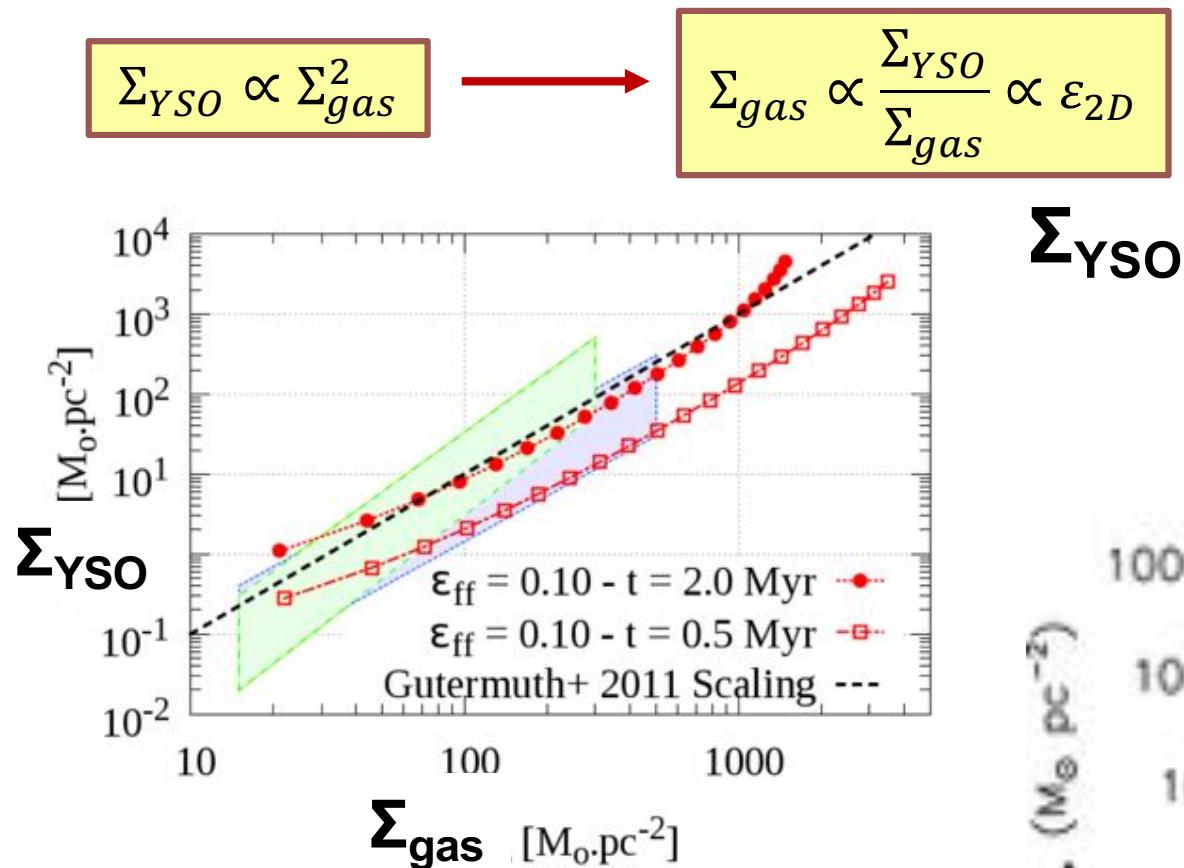


Fig 3, Parmentier & Pfalzner (2013)

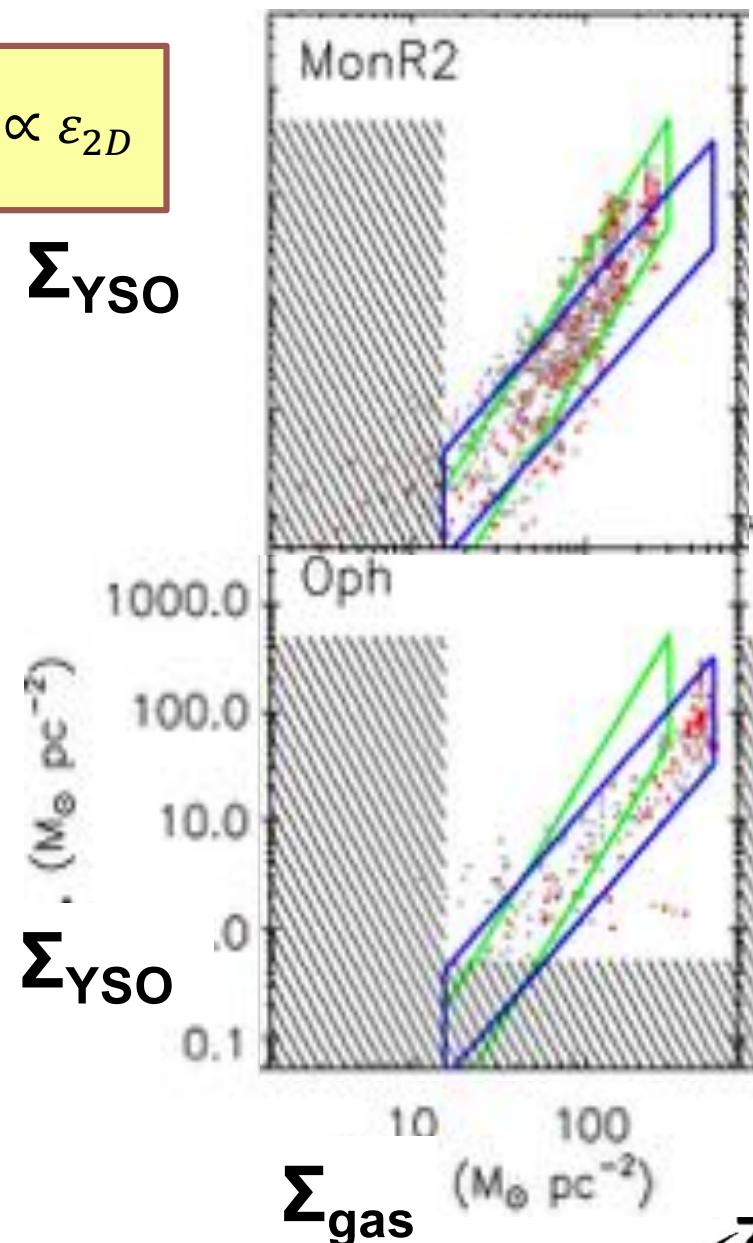
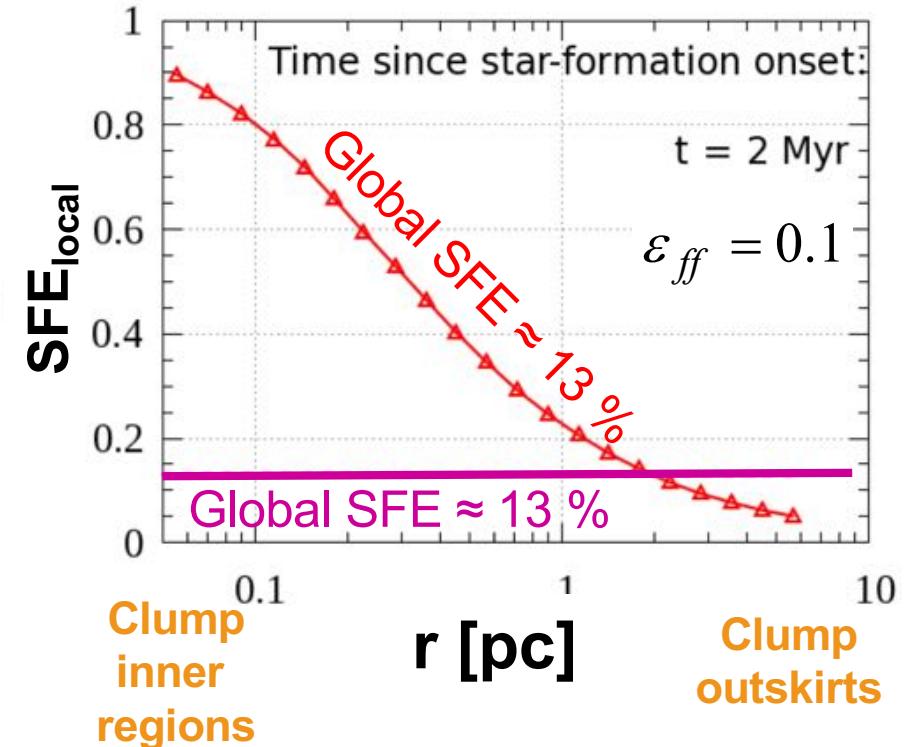
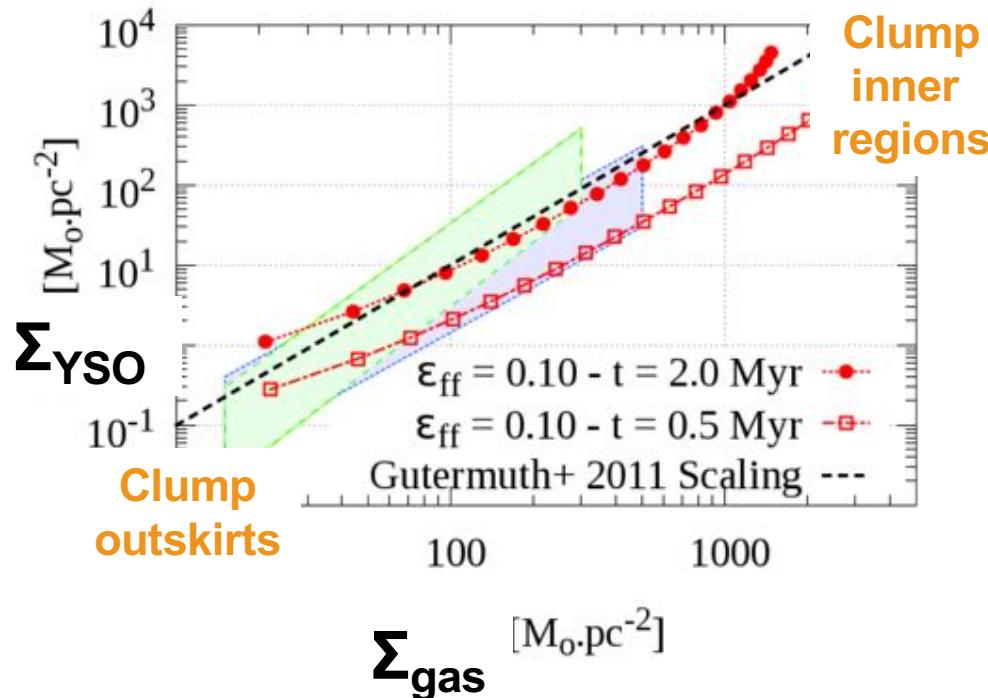


Fig. 9, Gutermuth+ (2011)



# SFE Radial Variations



Local Star Formation Relation:

Superlinear / Quadratic

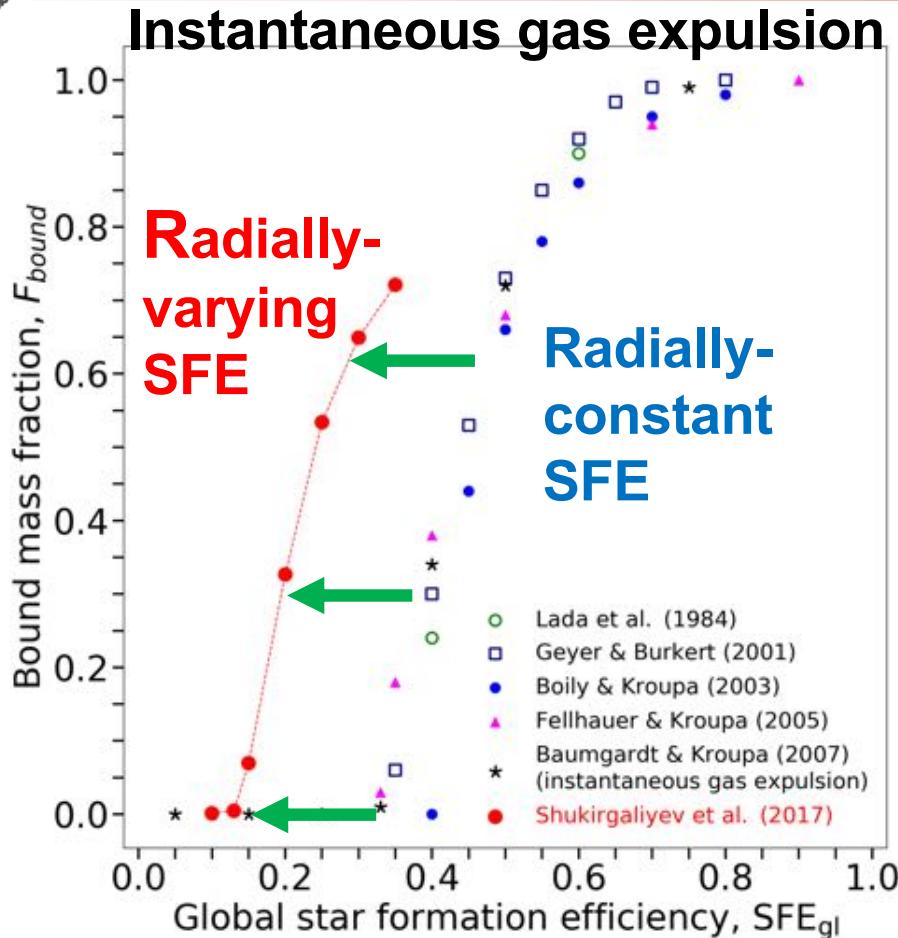
Local star formation efficiency :

$\text{SFE}_{\text{local}}(\text{inner}) > \text{SFE}_{\text{local}}(\text{outer})$

Figs 3 and 10, Parmentier & Pfalzner (2013)



# Violent Relaxation

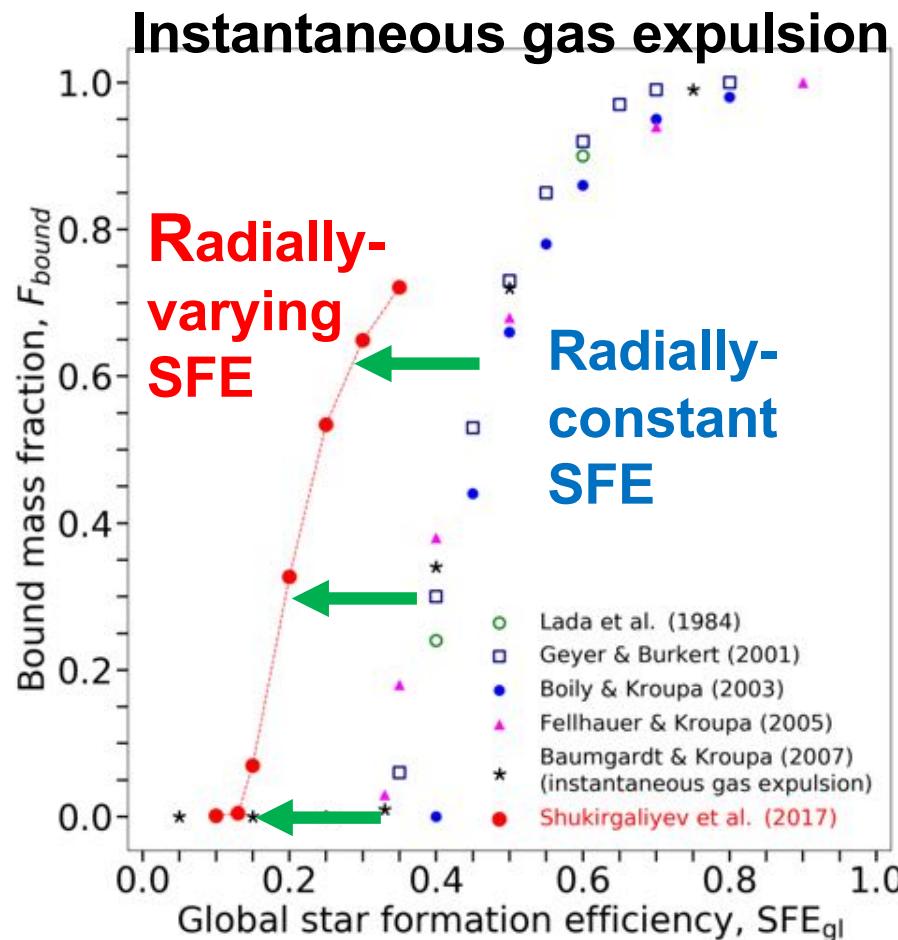


Based on Fig8 in Shukrgaliyev, Parmentier, Berczik & Just (2017)

- Strongly reduced infant mortality
  - Despite solar-neighbourhood tidal field inclusion!
  - One model cluster with a global SFE of 25% and a birth mass of  $15E3 M_{\text{sun}}$  has a dissolution time of 2.9Gyr !
- Clusters reaching a global SFE higher than 13% do survive



# Longer-Term Evolution



- **Cluster Teenage Mortality**
- One model cluster with a global SFE of 25% and a birth mass of  $15E3M_{\text{sun}}$  has a dissolution time of 2.9Gyr !
- Most clusters formed with a global SFE of 15% die within a Gyr

Based on Fig8 in Shukirgaliyev,  
Parmentier, Berczik & Just (2017)



# Long-Term Evolution of the SFE $\geq$ 15% Clusters

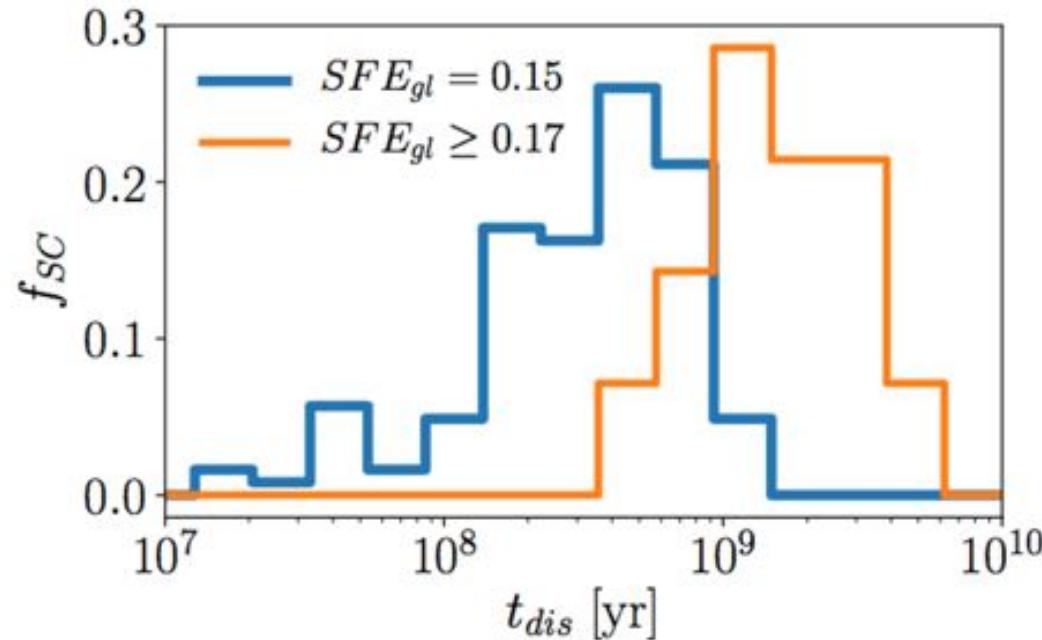


Fig 7, Shukirgaliyev,  
Parmentier, Just  
& Berczik (2018)

- Most clusters formed with a global SFE of 15% die within a Gyr
- Cluster teenage mortality
- Most clusters formed with a global SFE of at least 17% have a life-expectancy longer than 1Gyr: a higher SFE generates a more compact structure by the end of violent-relaxation



# Take-Away Messages

- The slopes of star formation relations measured for molecular clumps depend on:
  - what is measured,
  - how it is measured,
  - on top of SF physics
- When interpreting star formation relations, first thought should be “pitfalls ahead”
- Cluster infant mortality
  - ➡ Cluster teenage mortality