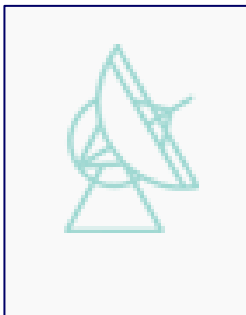


Geneva Observatory - 14 June 2011

**From  
Cluster-Forming Region Properties  
to Galaxy Evolution  
with Star Clusters**

**Geneviève Parmentier**



**Max-Planck-Institut für Radioastronomie  
Argelander-Institut für Astronomie**



**Bonn, Deutschland**

# Image Credit

- **Elliptical galaxy M87** (APOD 16.06.2004):
  - Canada-France Hawaii Telescope, J.-C. Cuillandre
- **Globular Cluster M10** (APOD 30.06.2001):
  - Till Credner, Sven Kohle (Bonn University), Hoher List Observatory
- **Orion Nebula Mosaic** (HST – WFPC2):
  - O'Dell and S.K. Wong (Rice University), NASA
- **Open Cluster Pleiades M45** (APOD 01.12.2002):
  - Anglo-Australian Observatory/Royal Observatory, Edinburgh
- **Open Cluster Hyades:**
  - <http://stars.astro.illinois.edu/sow/hyades-p.html> , by Jim Kaler
- **Spiral galaxy NGC3370** (APOD 14.05.2005):
  - Hubble Heritage Team, A. Riess (STScI) NASA

# Star Clusters: at the crossroad between star formation and galaxy evolution

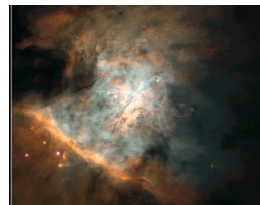
a few kpc - 100kpc:  
systems of  
star clusters  
and galaxies



10pc:  
individual  
gas-free  
star clusters



1-pc:  
star formation  
in embedded  
star clusters



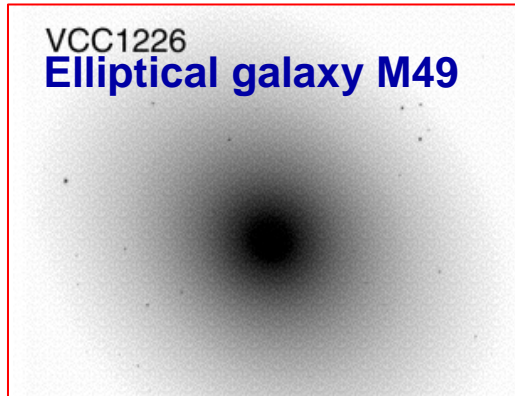
# Setting the Scene: Star Clusters (SC) as Powerful Tracers of Galaxy Evolution

## Star Clusters (SC):

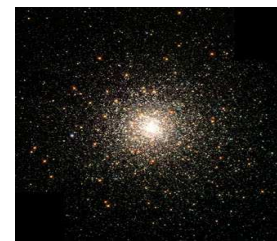
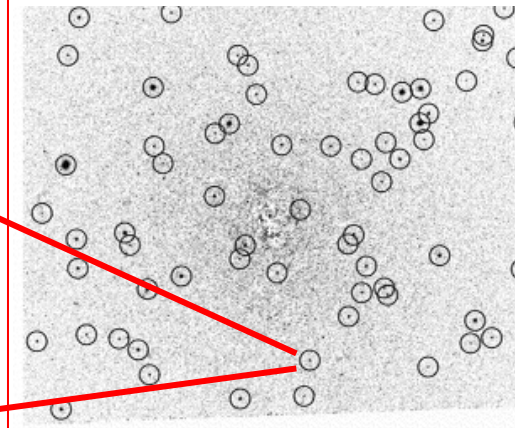
- Compact groups of coeval stars bound together by gravity
- Identified on a one-by-one basis against the background of their host galaxy

Jordan+04 (Virgo Galaxy Cluster ACS Survey II, fig6)

VCC1226  
Elliptical galaxy M49



Background-subtracted image



# Setting the Scene: Star Clusters (SC) as Powerful Tracers of Galaxy Evolution

## Star Clusters (SC):

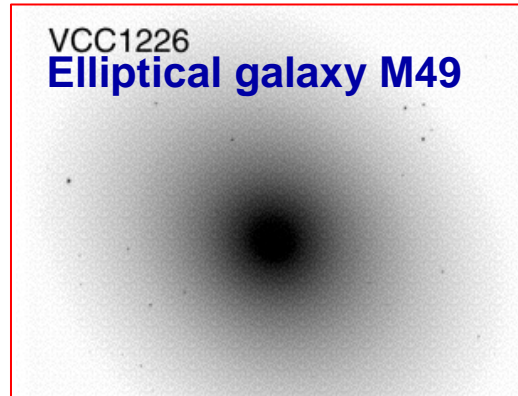
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## Multi-band imaging of SC systems

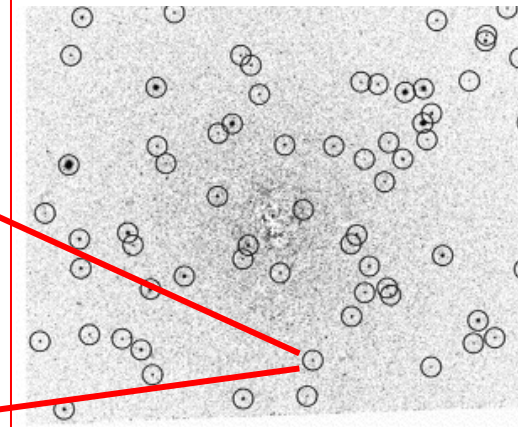
- (→ cluster magnitudes, colours)
- feasible out to Virgo Galaxy Cluster distances ( $\approx 20\text{Mpc}$ )
- combined to Simple Stellar Population models  
→ estimates of **cluster age, mass, metallicity**

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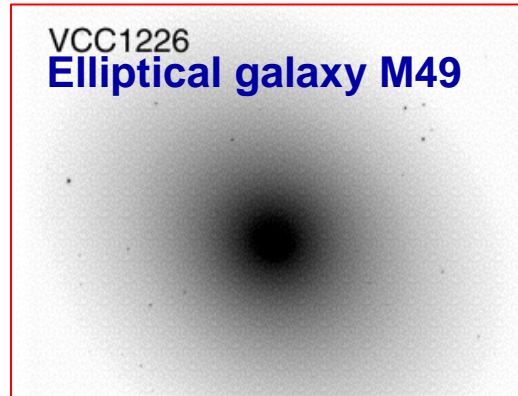
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## Comprehensive view of galaxy-:

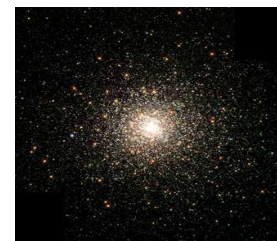
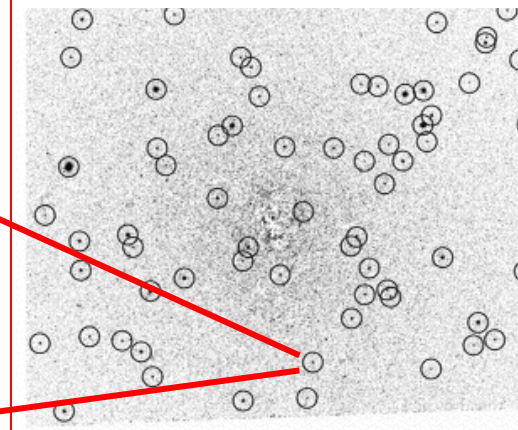
- chemical enrichment history,
  - interaction history,
  - star formation history
- over the past Hubble-Time**

Jordan+04 (Virgo Galaxy Cluster ACS Survey II, fig6)

VCC1226  
Elliptical galaxy M49



Background-subtracted image



**Star clusters are at the very heart of many astrophysical topics**

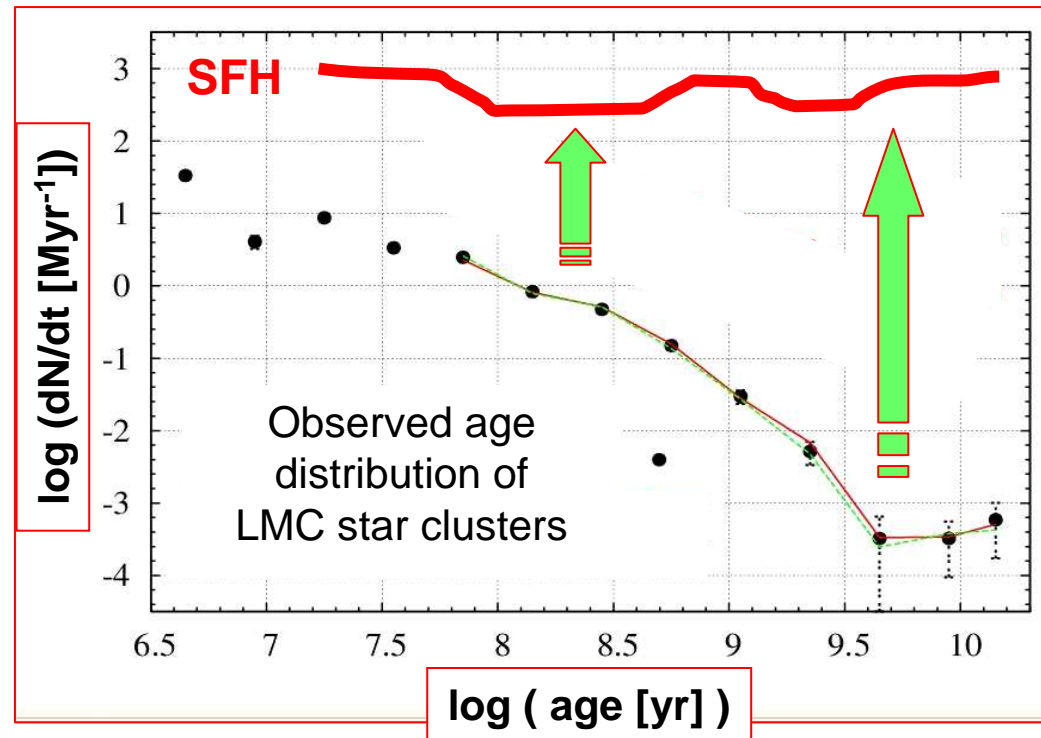
# The Big Issue: SCs versus field stars

Most stars in our Galaxy:

- ✿ are born in **SCs** → young SCs tell us about star formation
- ✿ but are observed as **field stars**
- ✿ SCs start losing stars as soon as they are born ...

Star clusters have the potential of tracing

➤ galaxy star formation histories



# The Big Issue: SCs versus field stars

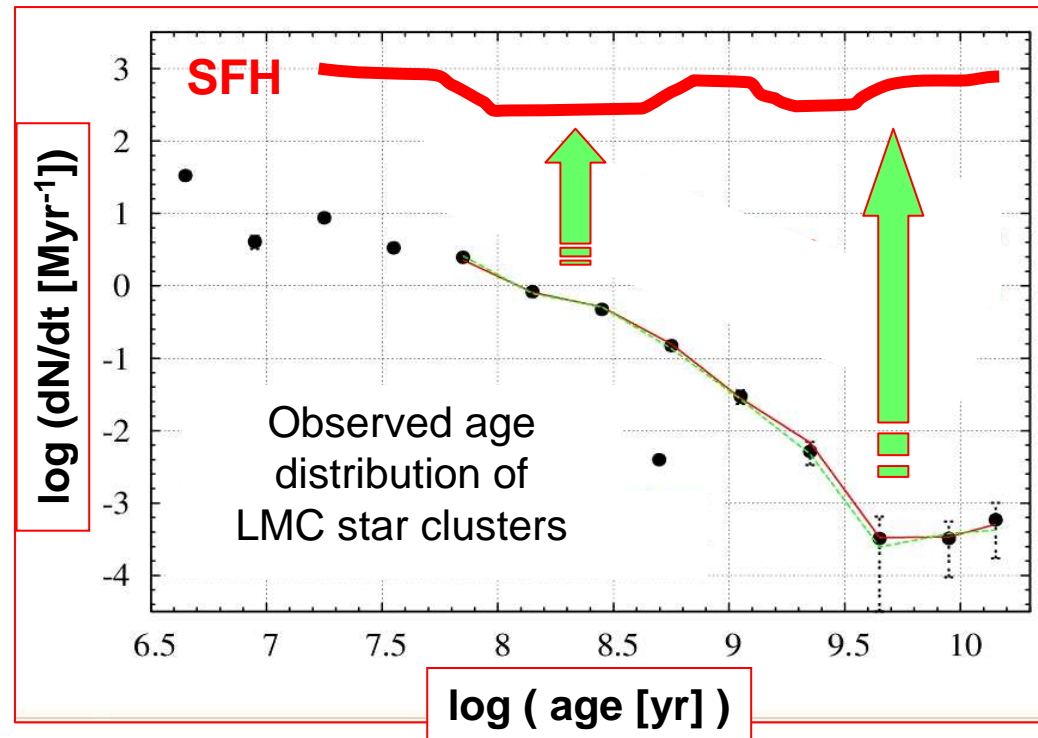
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provided we get a firm handle on the ratio of star formation still residing in (observed) star clusters as a function of age





# The Big Issue: SCs versus field stars

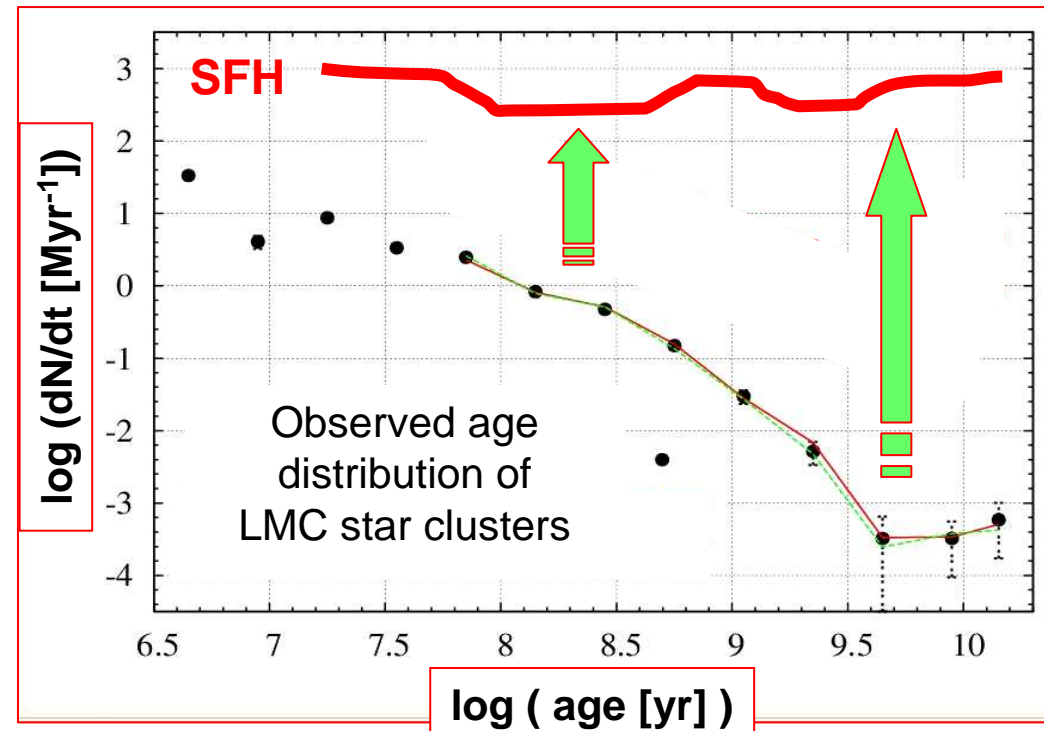
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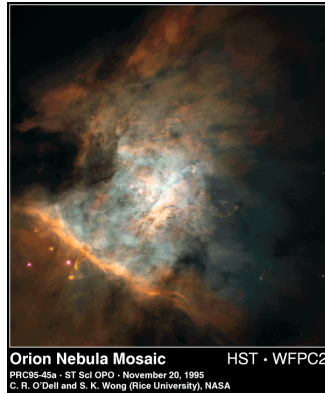
provided we get a firm handle on the ratio of star formation still residing in (observed) star clusters as a function of age



**Violent relaxation = Most traumatizing phase**

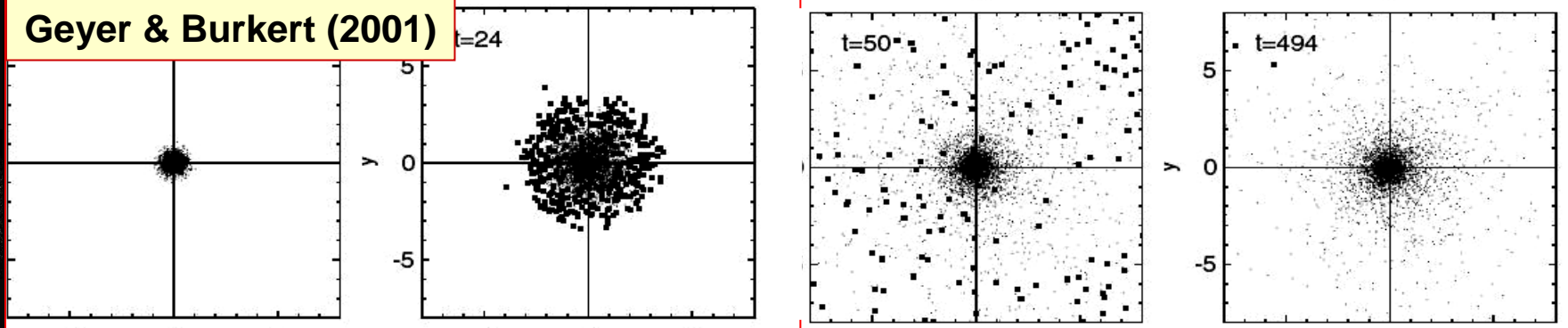
- Very short (10-50 Myr)
- SC Dynamical response to residual star-forming gas expulsion

# Intra-Cluster Gas-Expulsion and Violent Relaxation



time →

Geyer & Burkert (2001)



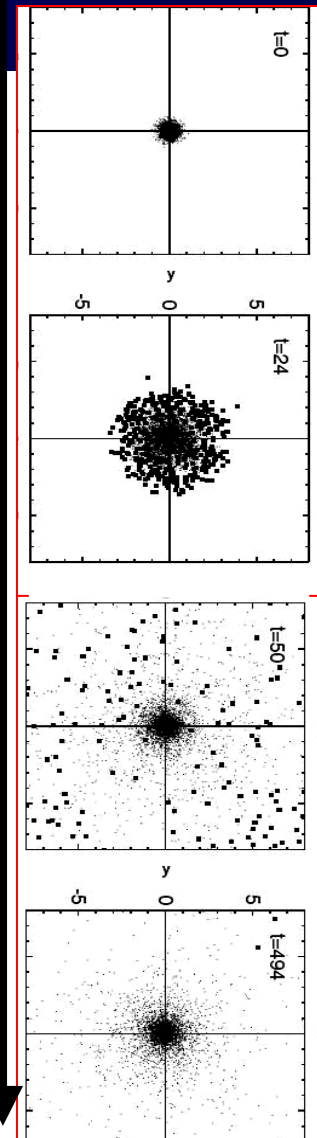
## Effects of gas expulsion - VIOLENT RELAXATION

- ☀ Cluster expansion
- ☀ Star loss (infant weight-loss), or
- ☀ Cluster dissolution (infant mortality)

# Violent Relaxation (VR): Observable Signatures and Prime Parameters

## Effects of gas expulsion - VIOLENT RELAXATION

- ☀ Cluster expansion
- ☀ Cluster infant weight-loss and infant mortality



Geyer & Burkert (2001)

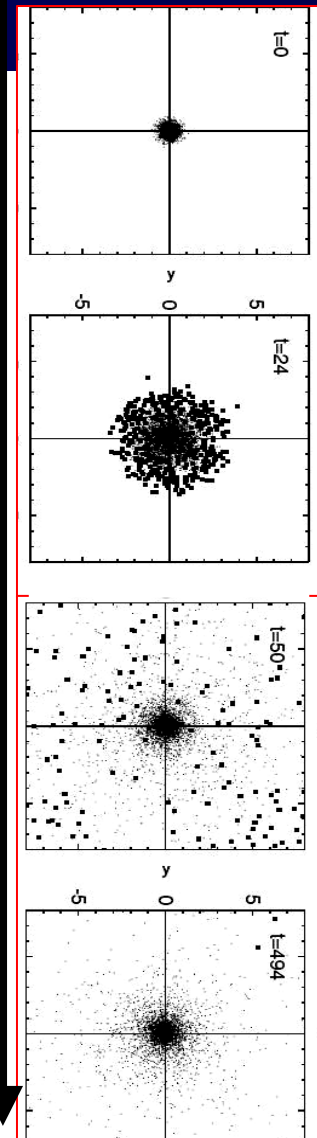
# Violent Relaxation (VR): Observable Signatures and Prime Parameters

## Effects of gas expulsion - VIOLENT RELAXATION

- ☀ Cluster expansion
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## Observable Imprints upon Star Cluster Systems :

- Cluster mass distribution,
- Cluster age distribution,
- Cluster radius distribution,



time

Geyer & Burkert (2001)

# Violent Relaxation (VR): Observable Signatures and Prime Parameters

## Effects of gas expulsion - VIOLENT RELAXATION

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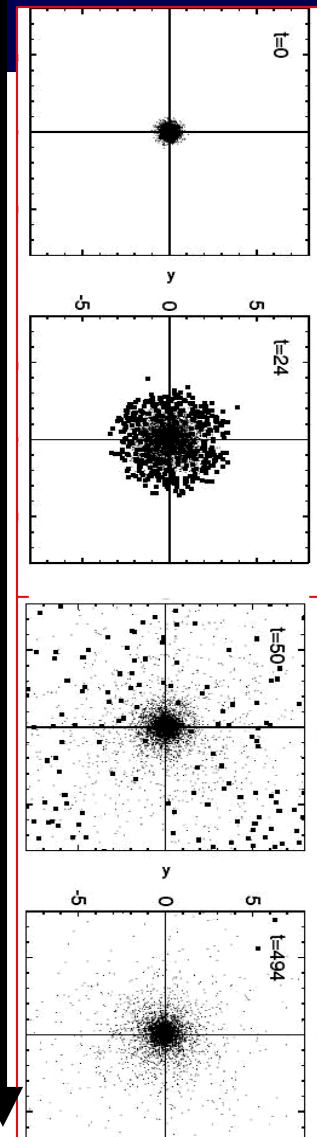
## Observable Imprints upon Star Cluster Systems :

- Cluster **mass** distribution,
- Cluster **age** distribution,
- Cluster **radius** distribution,

## Prime parameters: (e.g. Baumgardt & Kroupa 2007)

- **SFE** in cluster-forming region (CFRg)
- Gas expulsion time-scale:  $\tau_{\text{GExp}} / \tau_{\text{cross}}$
- **Impact** of external **tidal field** (environment)

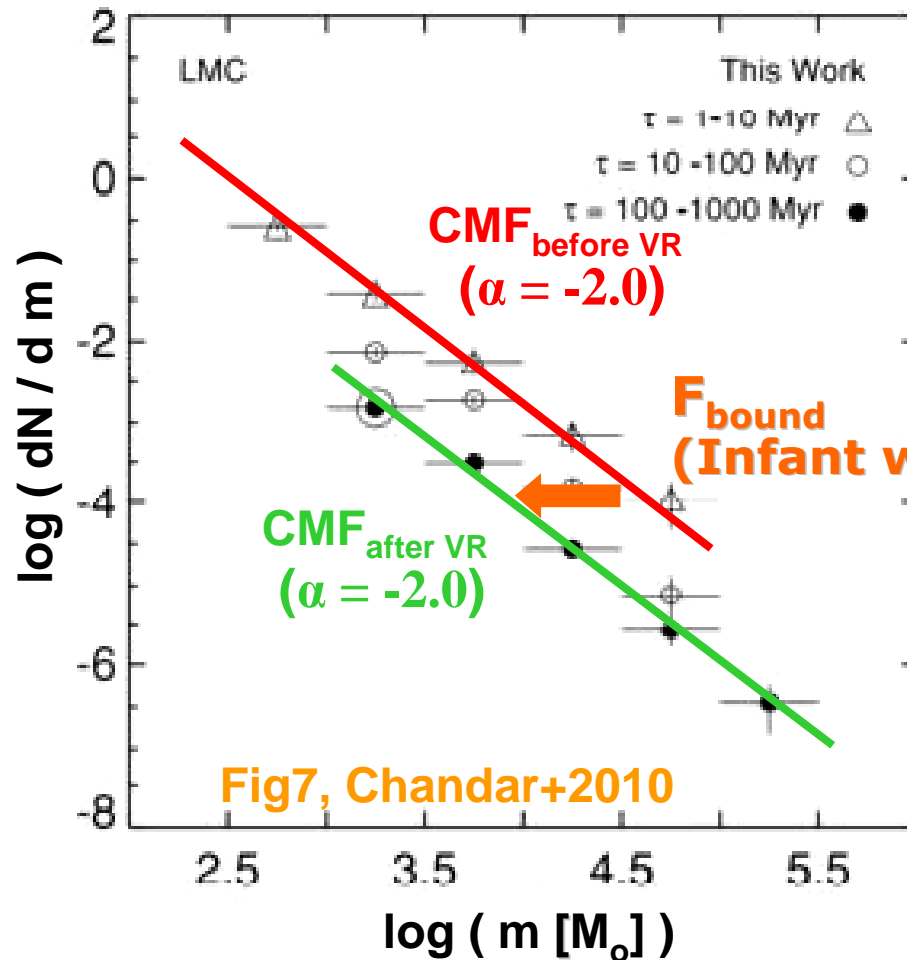
See also Adams (2000), Vesperini et al (2009), ...



Geyer & Burkert (2001)

# Violent Relaxation (VR): SC Mass Functions

Time-Evolution of SC Mass Functions: What observers tell us ...  
 No evolution of the MF shape over the first few 10Myr



$$\frac{dN}{dm} \propto m^{-2}$$

$$\equiv \frac{dN}{d \log m} \propto m^{-1}$$

$$m_{cluster} \text{ (end of VR)}$$

$$= F_{bound} \times m_{ecl} \text{ (at Gas Exp)}$$

**$F_{bound}$  is mass-independent**

Note: what happens after 100Myr remains disputed ...

# SFE and SC Mass Functions

$$m_{cluster}(\text{end of VR}) = F_{bound}(SFE) \times SFE \times m_{CFRg}$$

$$F_{bound}(SFE)$$

**SFE**

= fraction of gas ending up in stars

**$F_{bound}$**

= fraction of stars remaining bound to the cluster at the end of VR

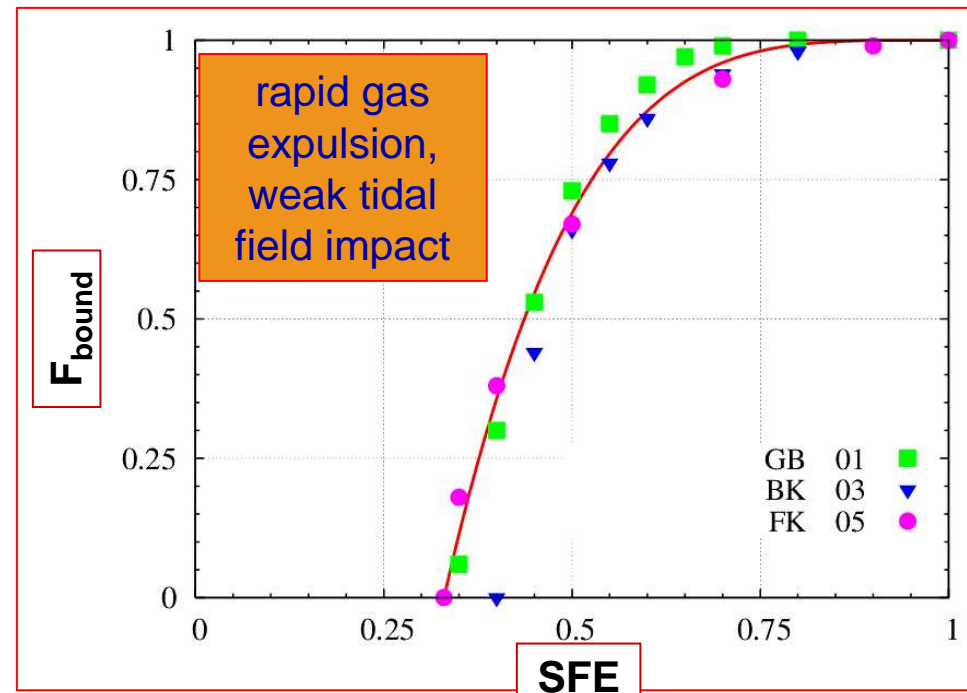


Fig1, Parmentier & Gilmore (2007)

**$F_{bound}$  is mass-independent**  
→ **SFE is mass-independent**

# $\tau_{GExp}/\tau_{cross}$ and SC Mass Functions

$$F_{bound} \left( \text{SFE}, \frac{\tau_{GExp}}{\tau_{cross}} \right)$$

**Constant radius:**  
**more massive star cluster progenitors have**

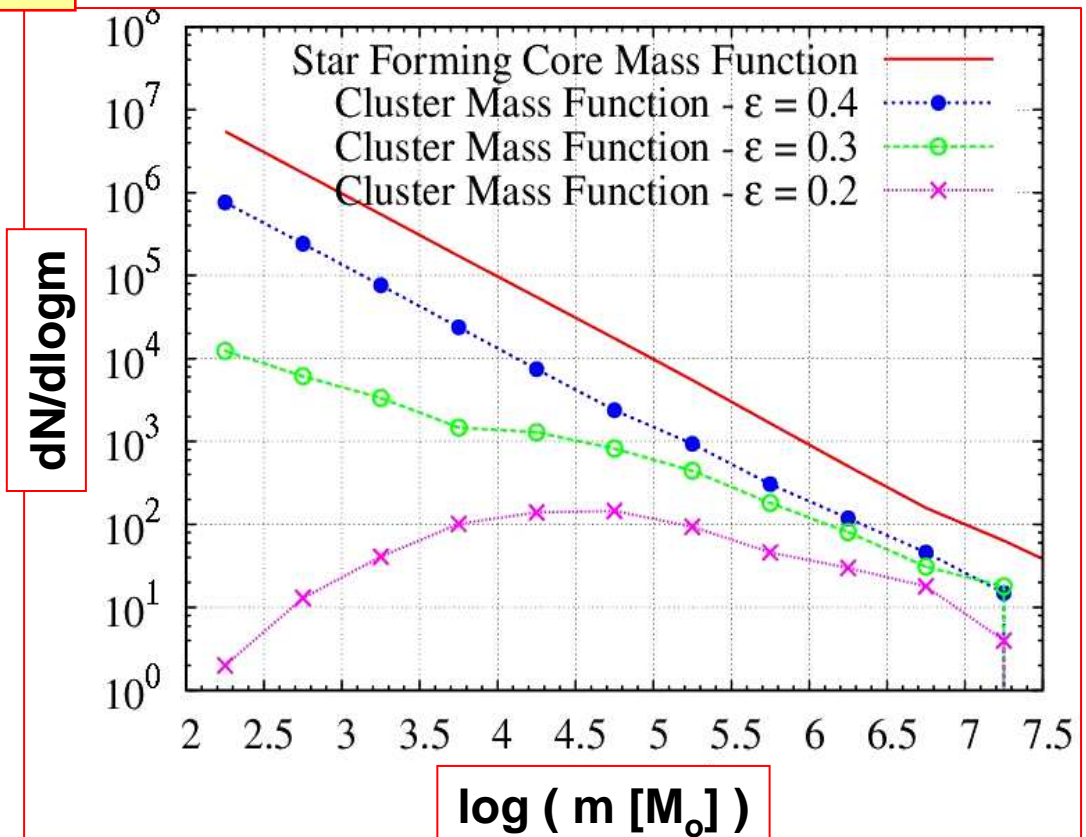
- a deeper potential well
- a slower gas-expulsion t-s
- can survive despite a **low SFE** of, say, 20%

**$F_{bound}$  is mass-independent**

**$\rightarrow \tau_{GExp}/\tau_{cross}$  is mass-independent**

**but looser constrain**

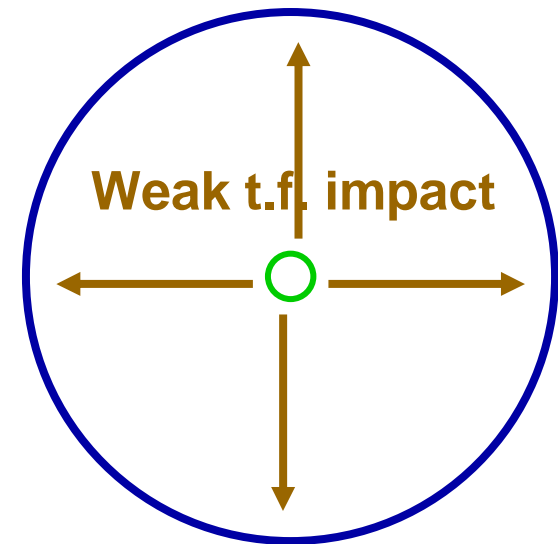
Parmentier, Goodwin et al. (2008), Fig2a





# Tidal Field Impact

$$F_{bound} \left( \mathbf{SFE}, \frac{\tau_{GExp}}{\tau_{cross}}, \frac{r_{half-mass}}{r_{tidal}} \right)$$



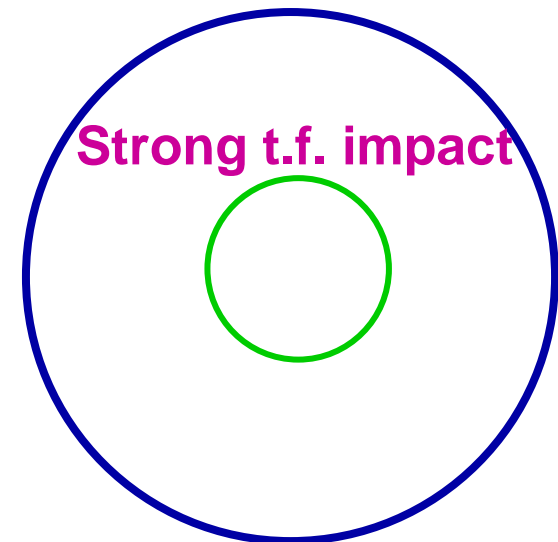
$$\text{Half - mass radius : } r_{half-mass} \propto r_{CFRg}$$

Limiting tidal radius :

$$r_{tidal} = (m_{ecl})^{1/3} \left( \frac{G D_{gal}^2}{2 V_c^2} \right)^{1/3} \propto (SFE \cdot m_{CFRg})^{1/3}$$

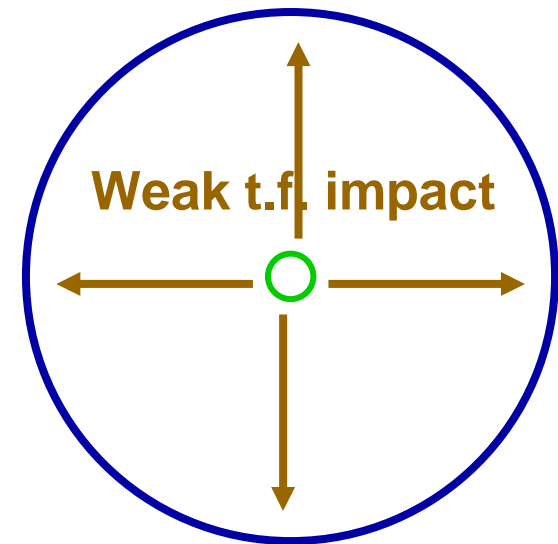
Embedded  
cluster  
mass

SC  
environment



# Tidal Field Impact

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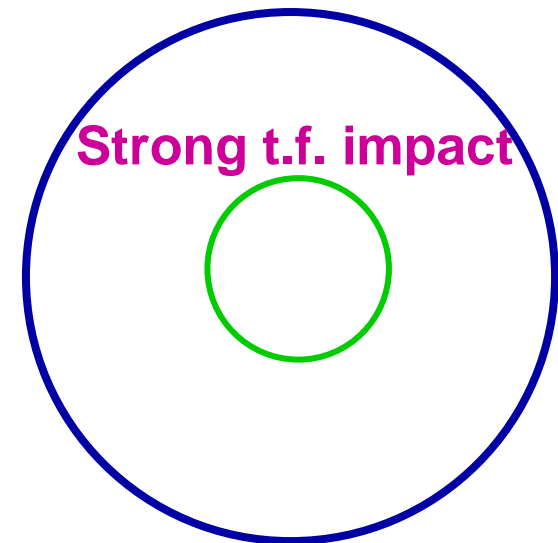
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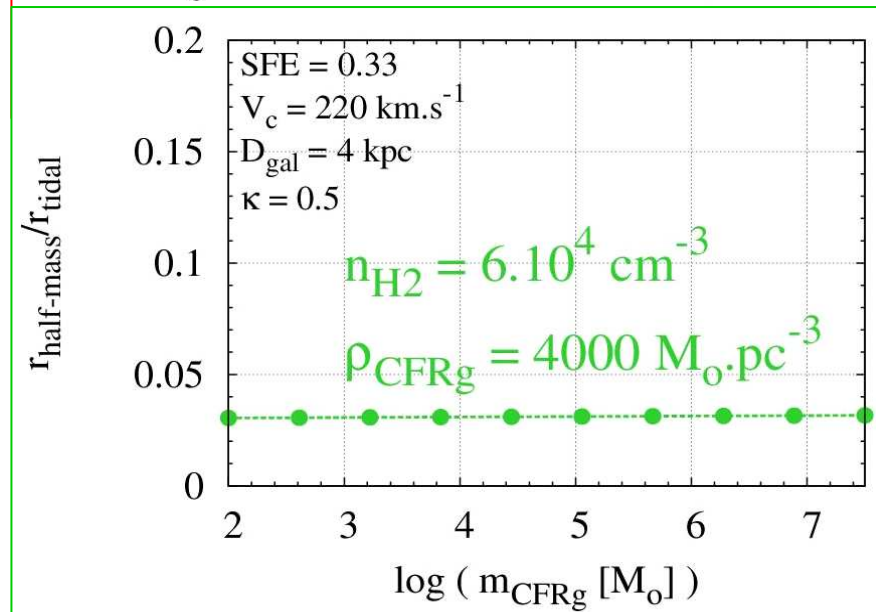
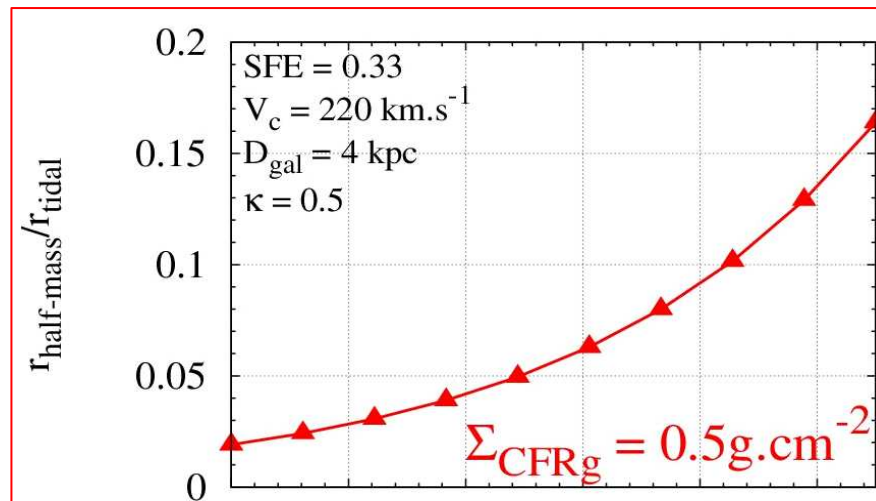
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Embedded cluster mass

SC environment



# Half-Mass Radius—to—Tidal Radius Ratio



$$r_{half-mass} \propto r_{CFRg} \propto m_{CFRg}^{1/2}$$

$$r_{tidal} \propto m_{ecl}^{1/3} \propto m_{CFRg}^{1/3}$$

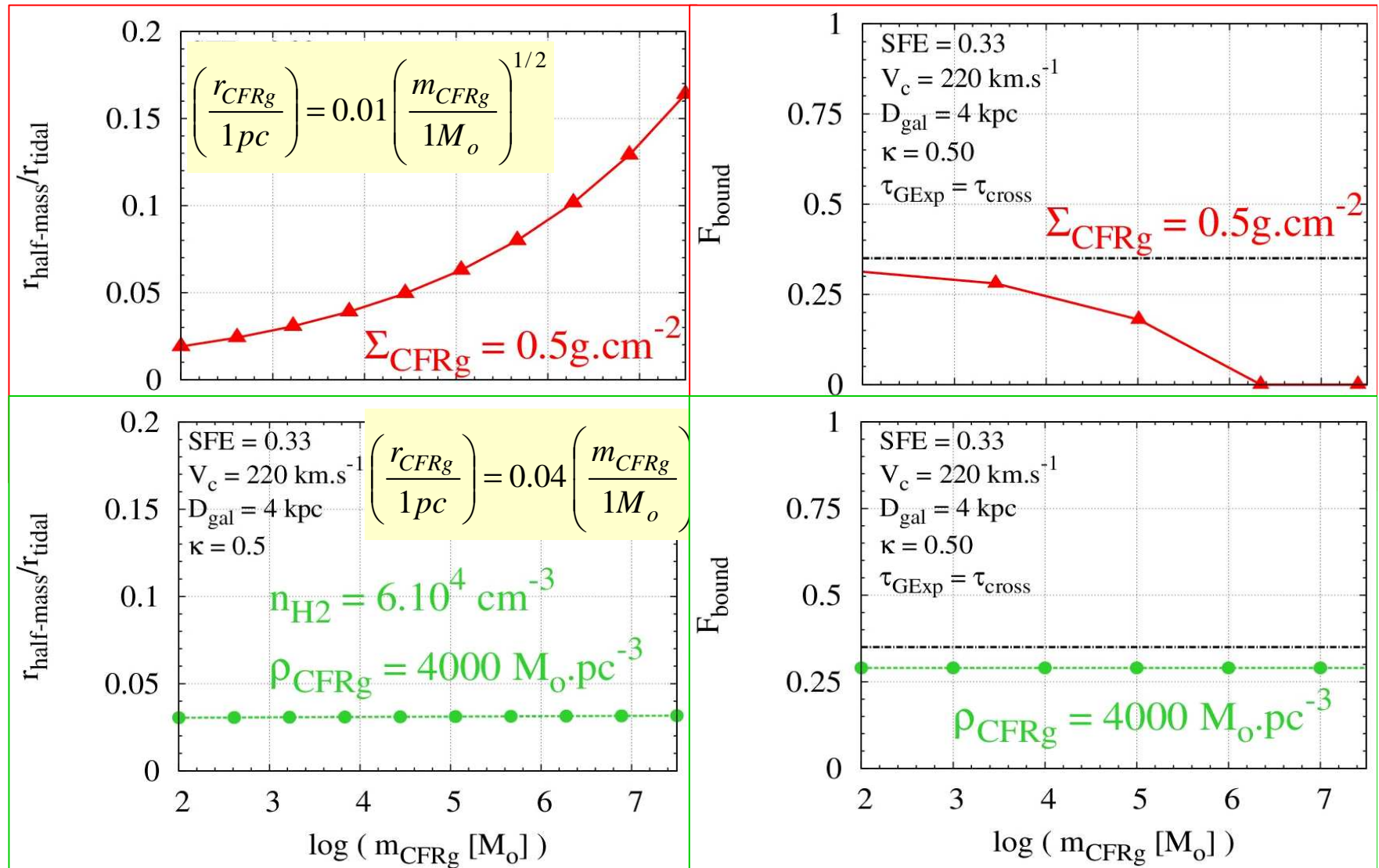
$$\frac{r_{half-mass}}{r_{tidal}} \propto m_{CFRg}^{1/6}$$

$$r_{half-mass} \propto r_{CFRg} \propto m_{CFRg}^{1/3}$$

$$r_{tidal} \propto m_{ecl}^{1/3} \propto m_{CFRg}^{1/3}$$

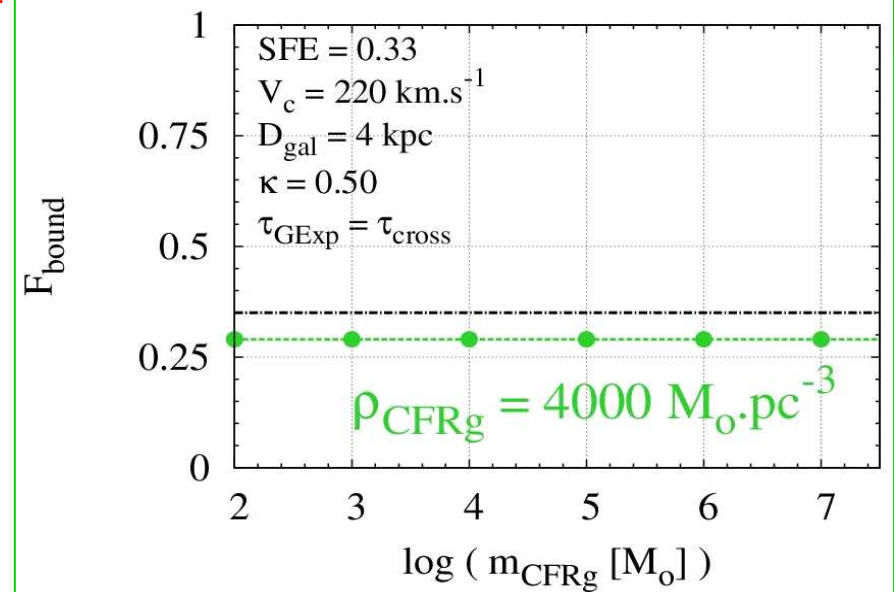
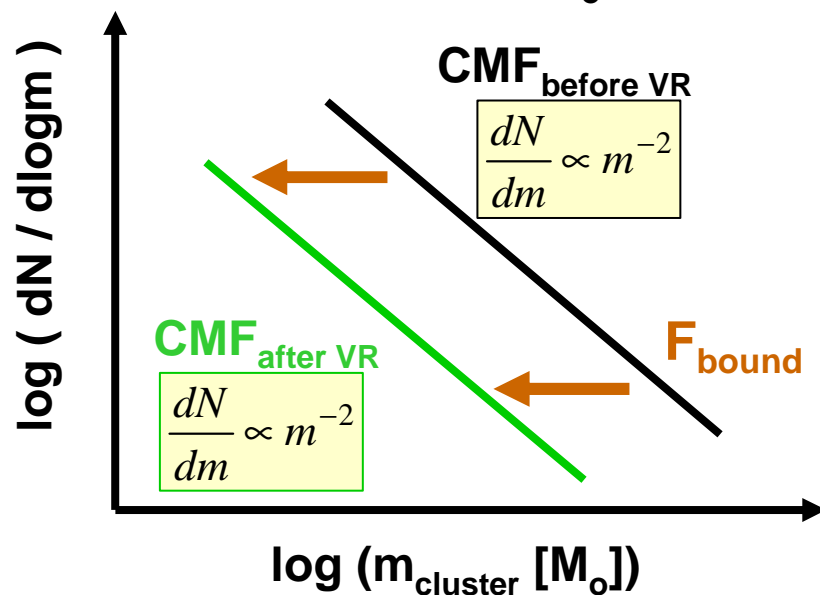
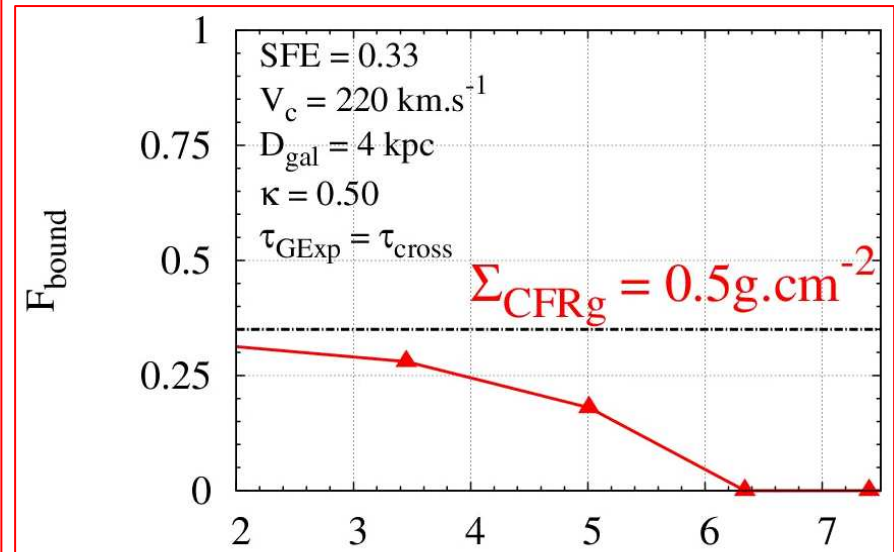
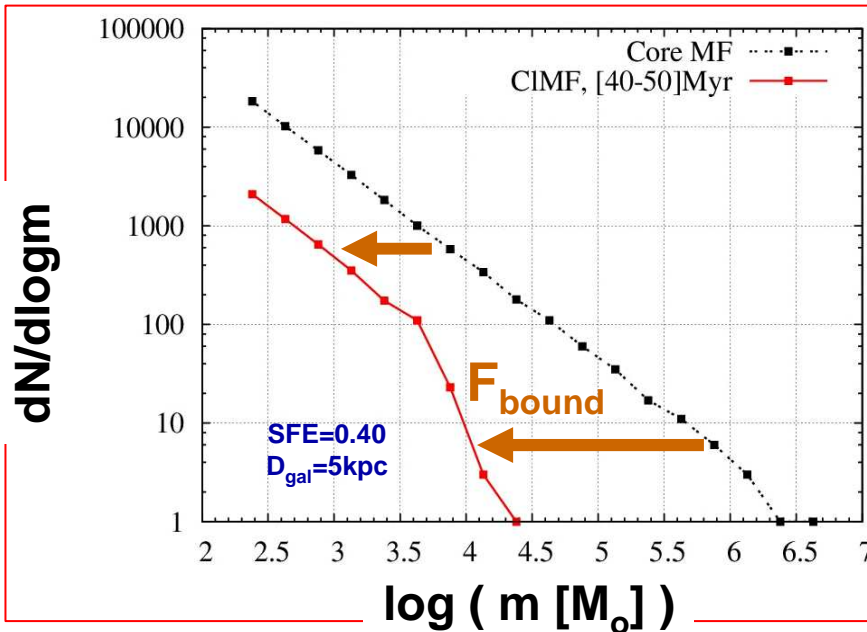
$$\frac{r_{half-mass}}{r_{tidal}} \propto m_{CFRg}^0$$

# Bound Fractions at the End of Violent Relaxation

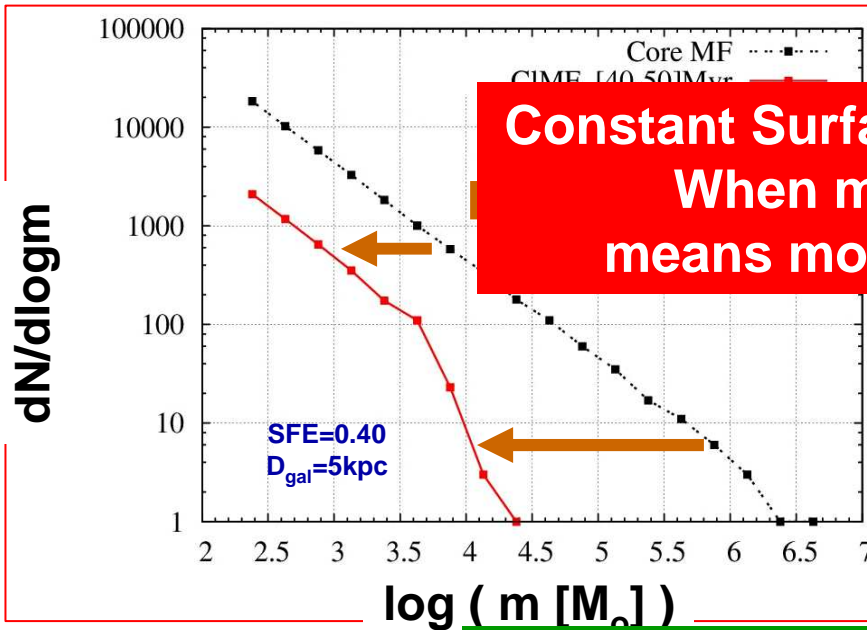


Parmentier & Kroupa (2011)

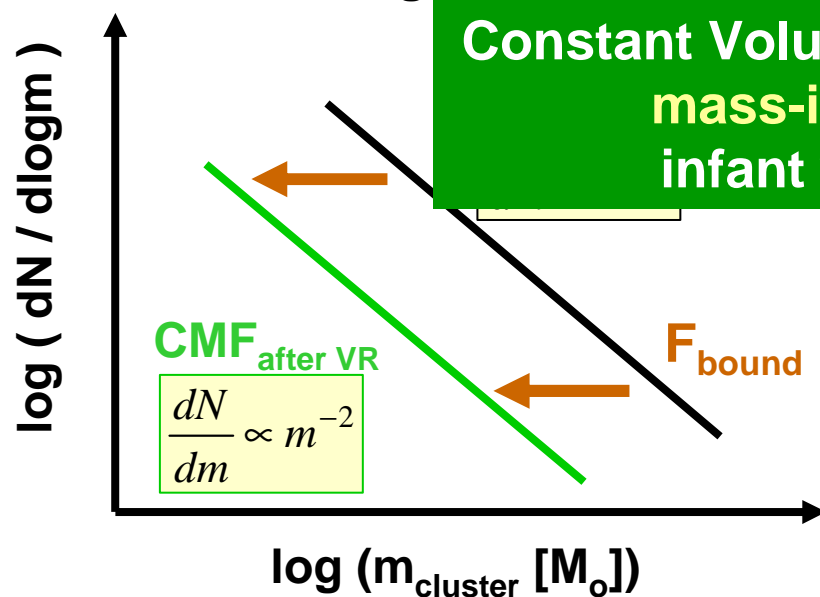
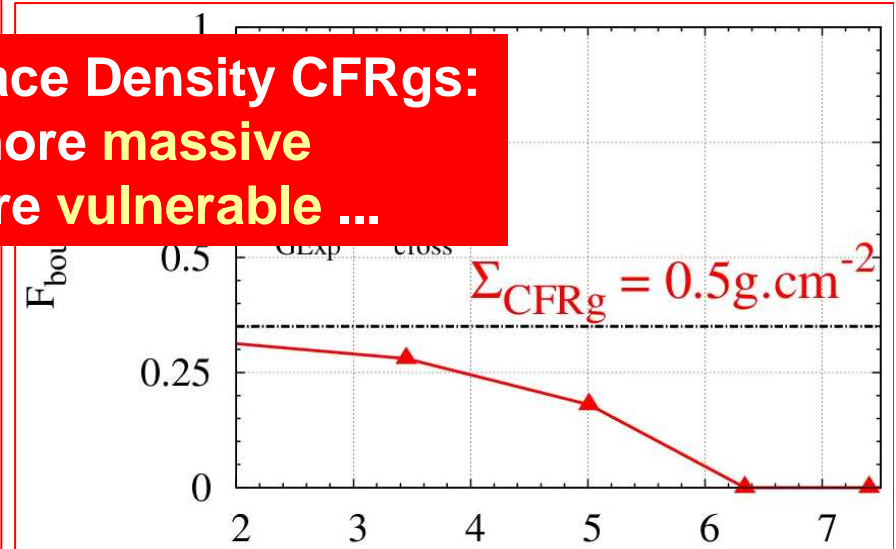
# Young SC Mass Functions



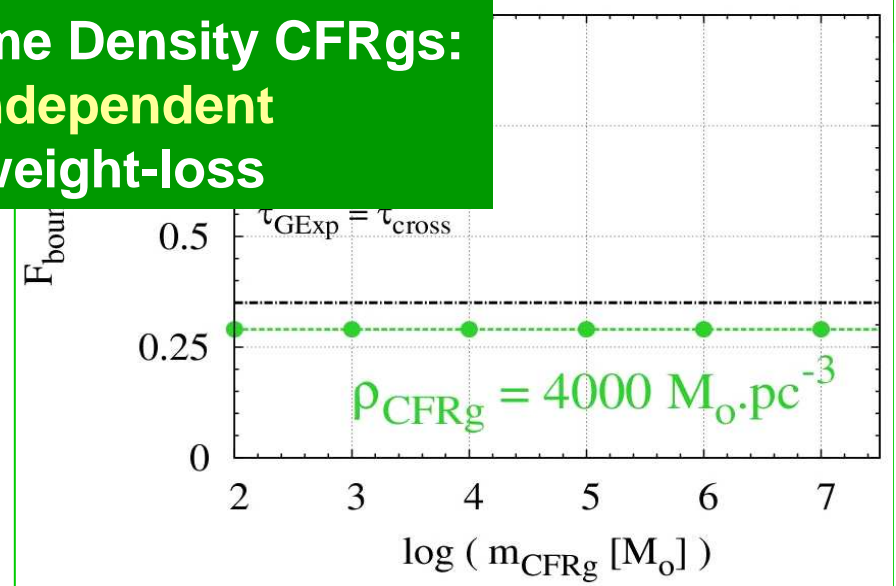
# Young SC Mass Functions



**Constant Surface Density CFRGs:**  
When more massive  
means more vulnerable ...



**Constant Volume Density CFRGs:**  
mass-independent  
infant weight-loss



# A Volume Density Threshold for the Star-Forming Gas

© Gao & Solomon (2004), Wu+2005

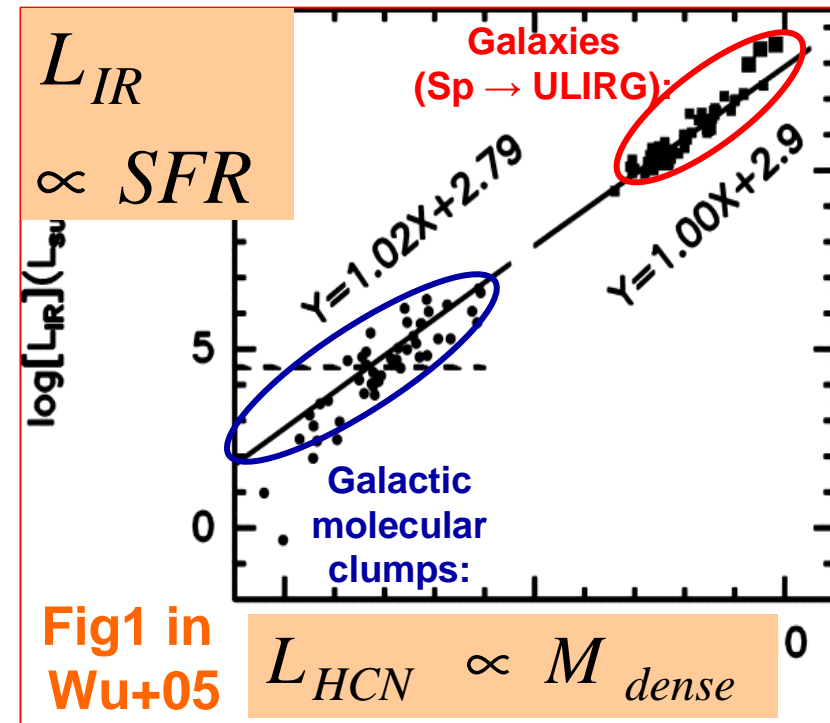
→ HCN mapping of entire galaxies  
+ Galactic individual molec clumps

➔ the SFR scales as the mass of  
dense molecular gas:  $n_{\text{H}_2} > 3 \cdot 10^4 \text{cm}^{-3}$

© Lada, Lombardi & Alves (2010)

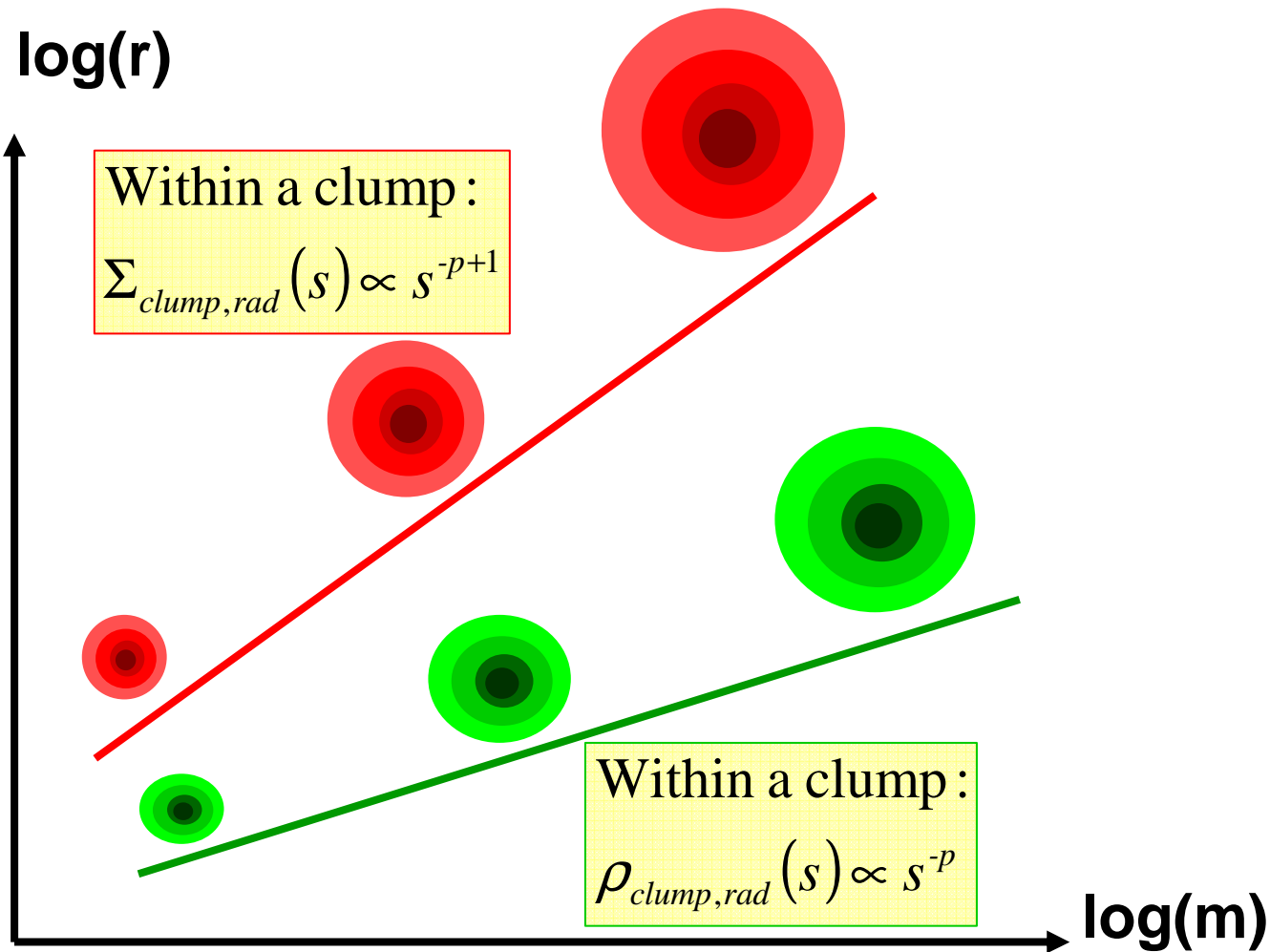
→ comparison of IR extinction maps  
of molecular clouds with their  
census of Young Stellar Objects

➔ the SFR scales as the mass of  
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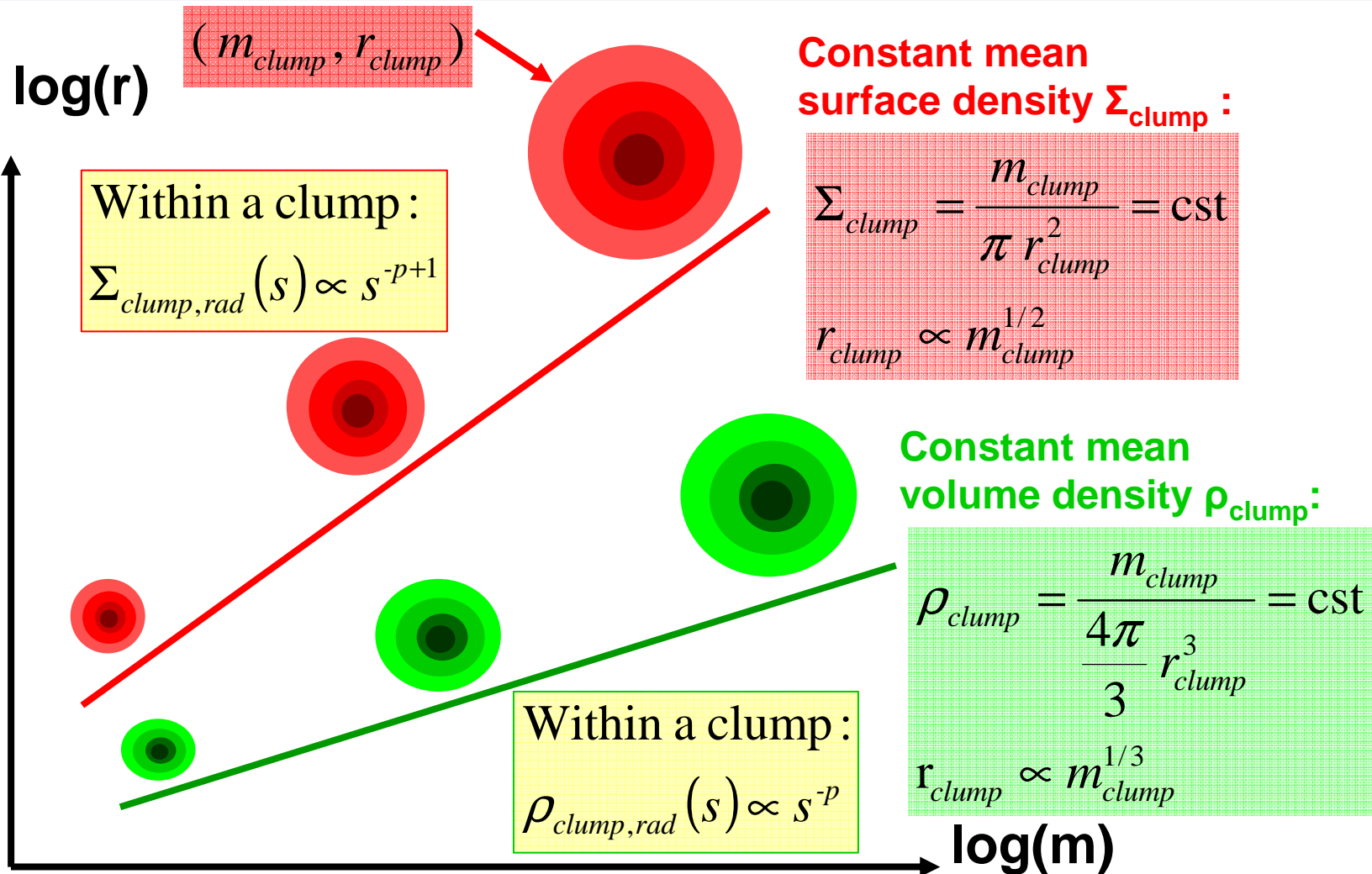
- CFRGs of about constant mean volume density ( $n_{\text{H}_2} = \text{few } n_{\text{th}}$ )
- Conclusion identical as for the tidal field impact analysis (Parmentier & Kroupa 2011)

# Constant 'mean' volume or surface density, NOT 'uniform' volume or surface density

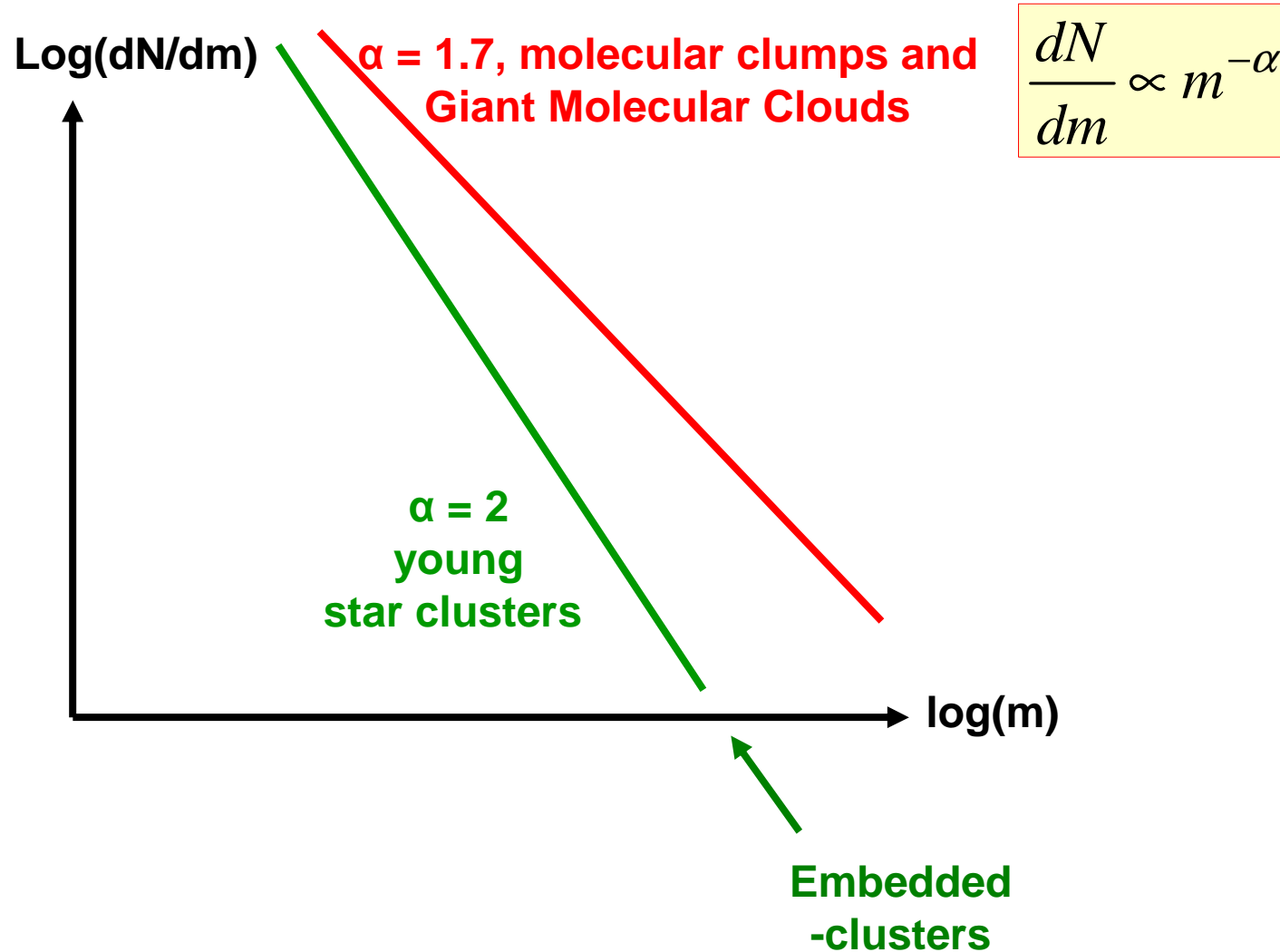




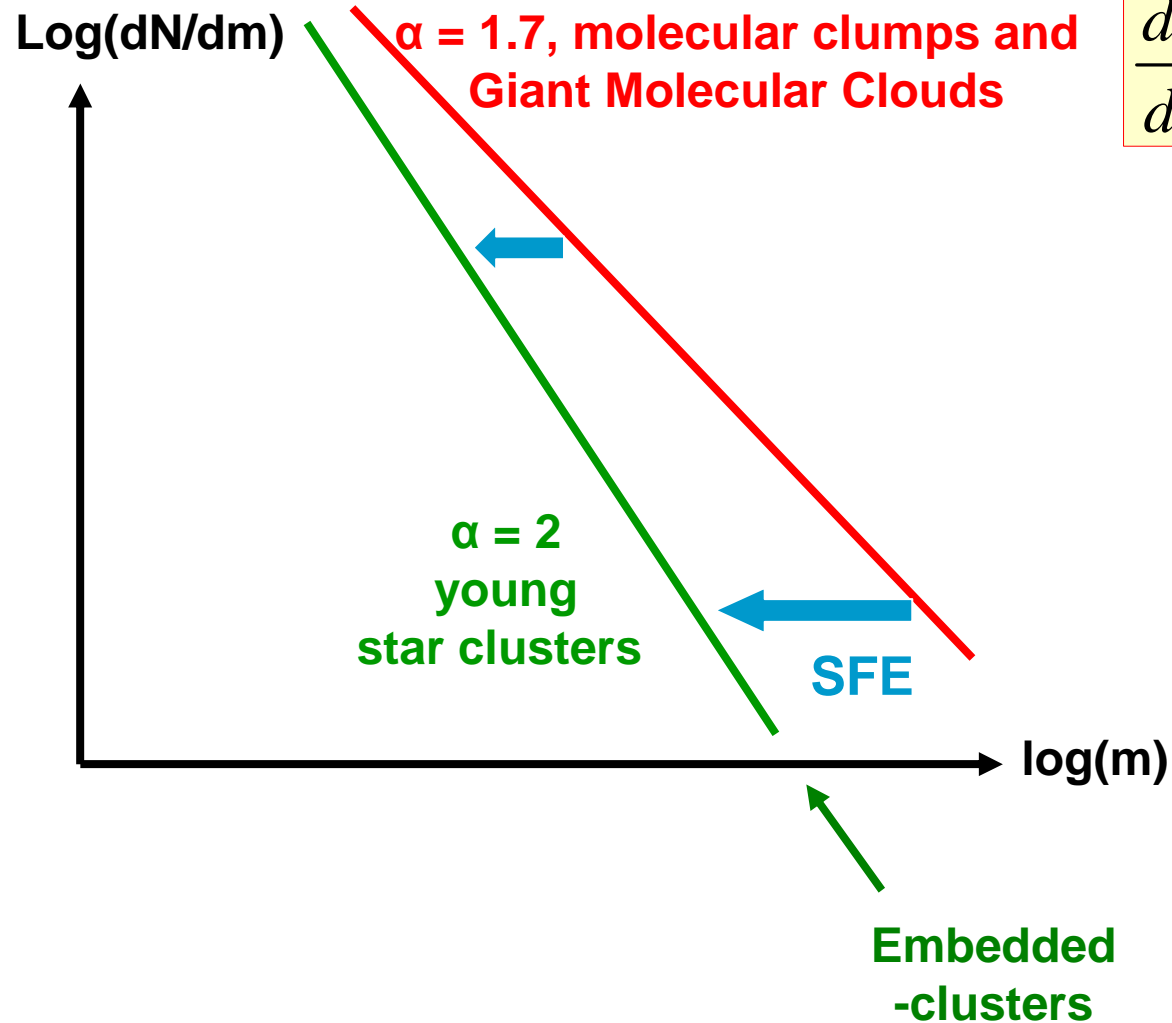
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# From the mass function of GMCs/clumps to that of gas-free star clusters ...



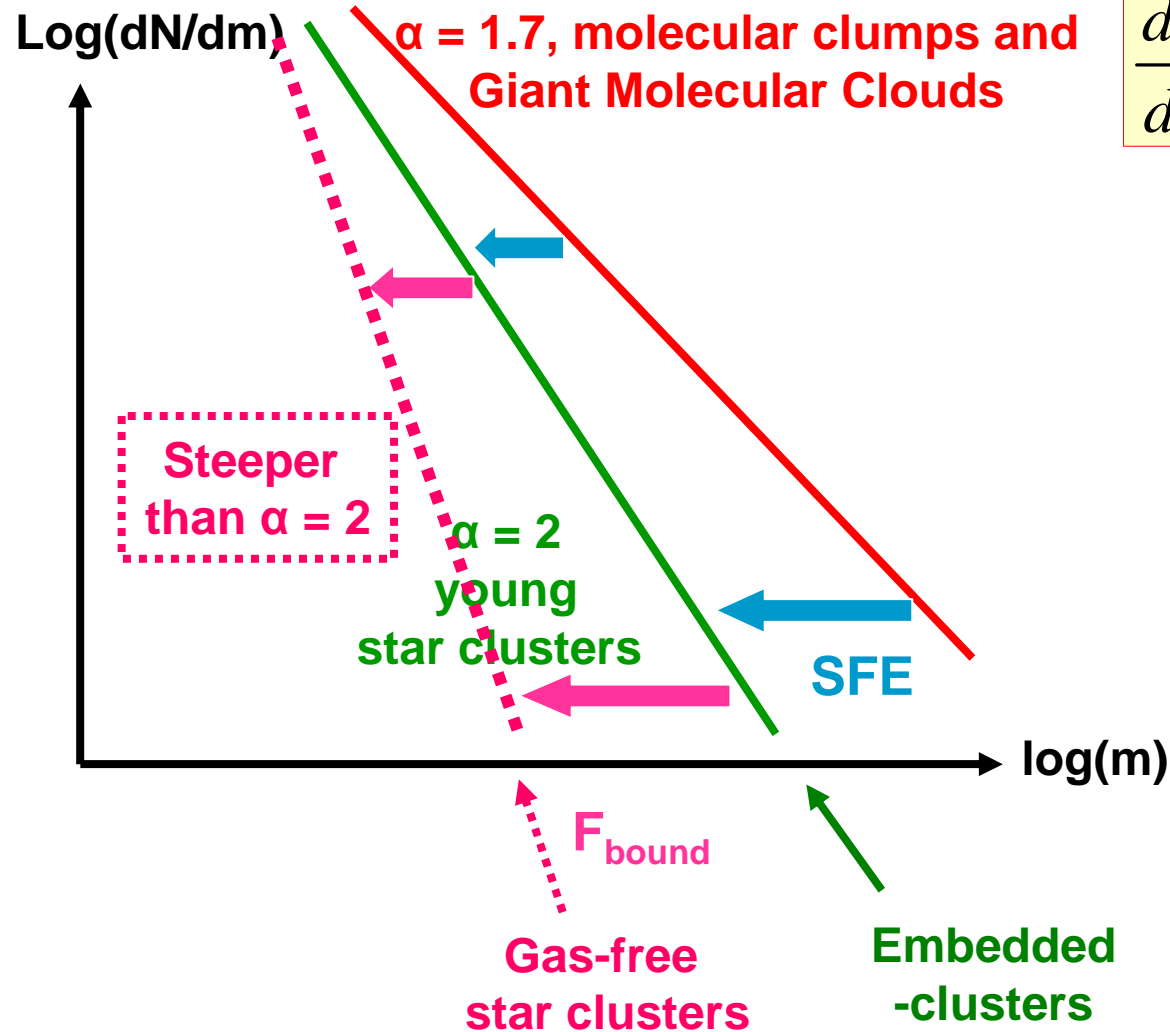
# From the mass function of GMCs/clumps to that of gas-free star clusters ...



$$\frac{dN}{dm} \propto m^{-\alpha}$$

Mass-varying SFE:  
lower SFE at higher  
cloud/clump mass ??

# From the mass function of GMCs/clumps to that of gas-free star clusters ...



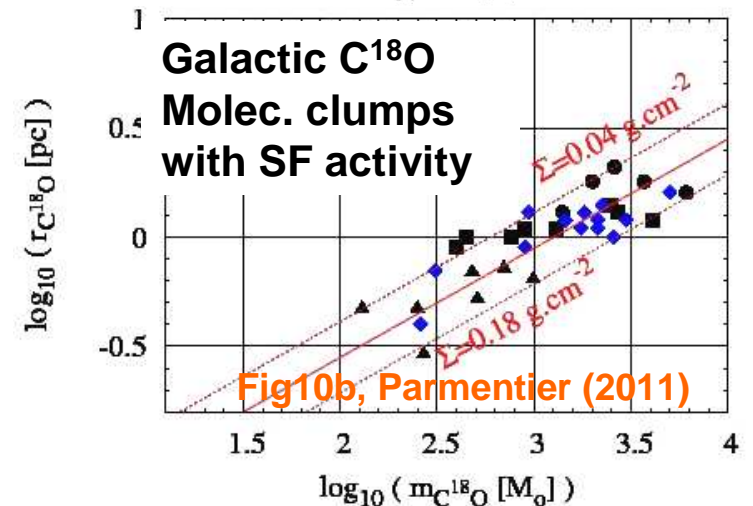
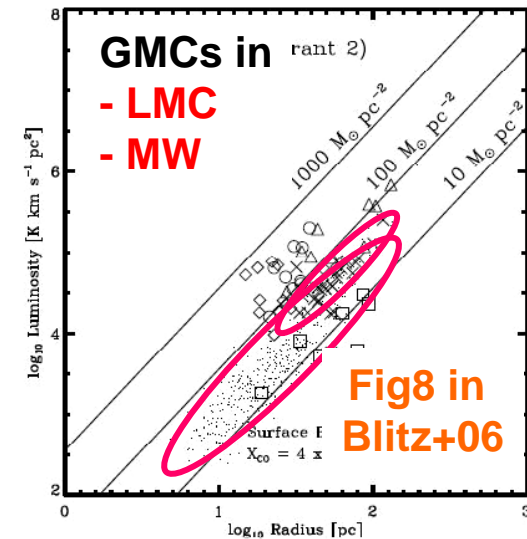
$$\frac{dN}{dm} \propto m^{-\alpha}$$

Mass-varying SFE:  
lower SFE at higher  
cloud/clump mass ??

But then  
mass-varying  
 $F_{\text{bound}}$  too ??

# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

- Cluster-forming regions:
  - constant mean volume density
  - (tidal field impact analysis)



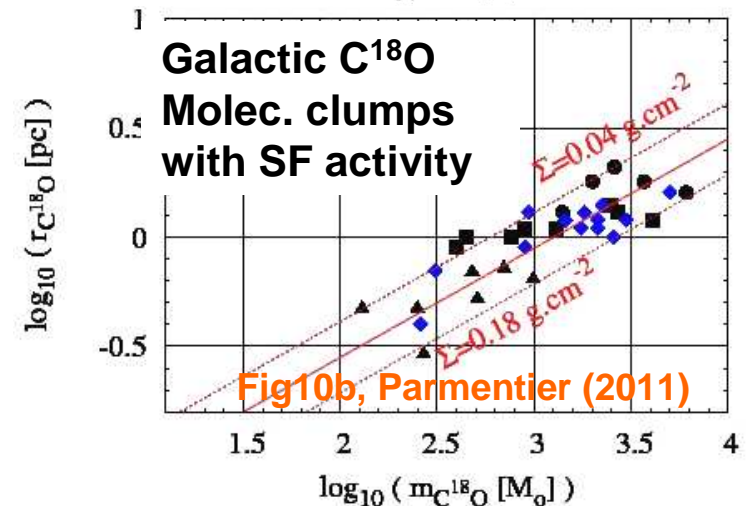
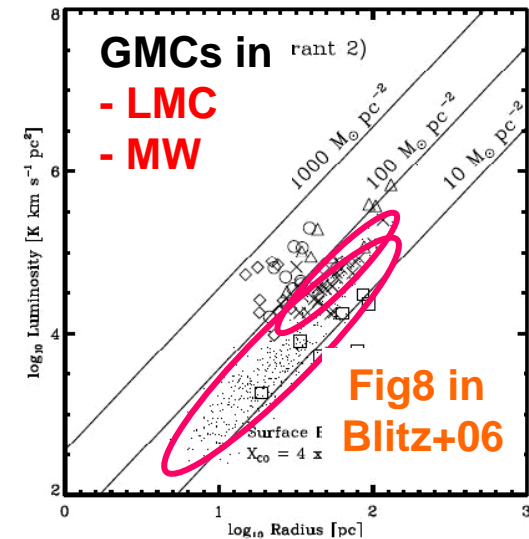
# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

➤ Cluster-forming regions:  
**constant mean volume density**  
 (tidal field impact analysis)

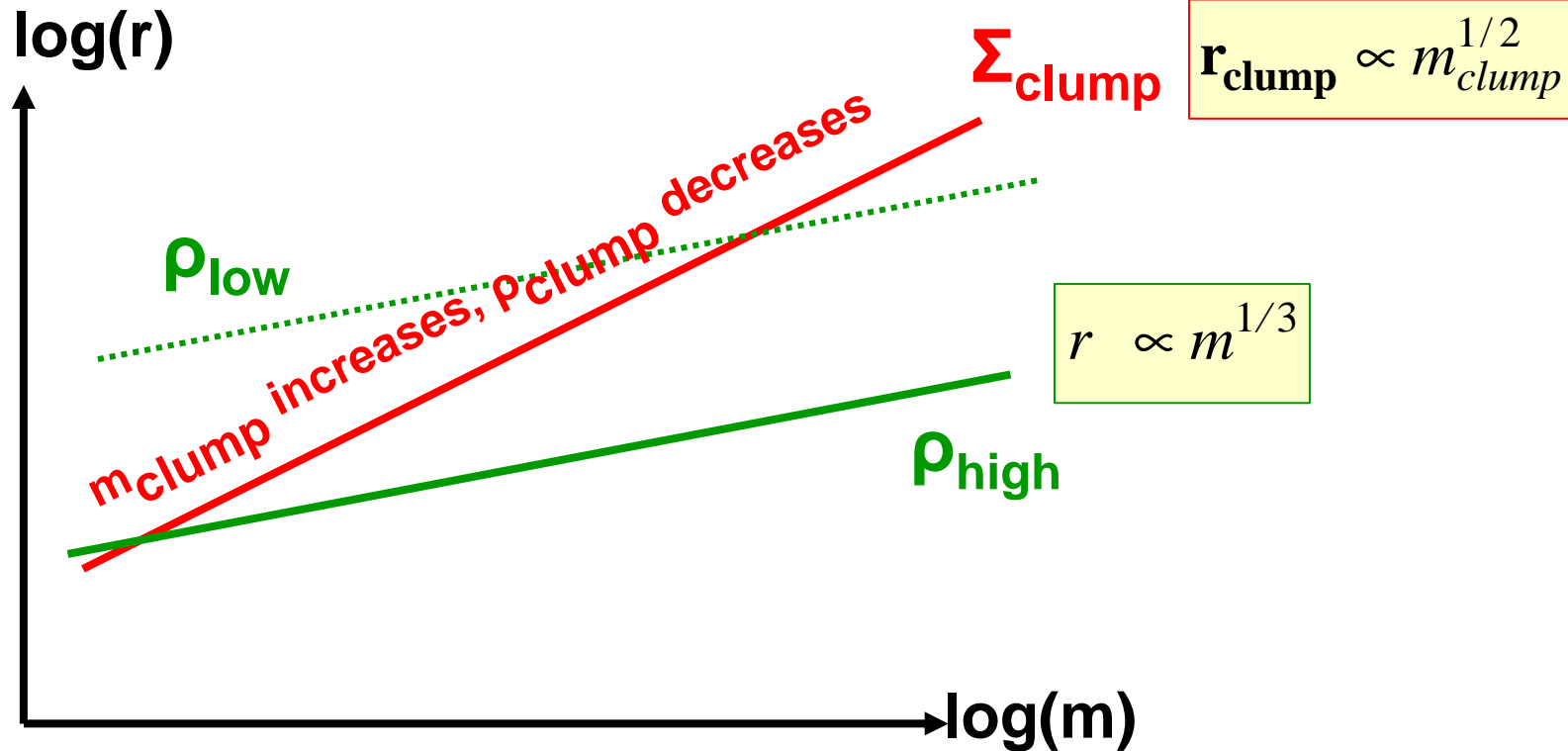
➤ GMCs and Molecular clumps  
 with signs of SF activity:  
**constant mean surface density**

- Larson 1981
- Blitz+ 2006
- Heyer+ 2009

➔ **Mass-dependent effect**



# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

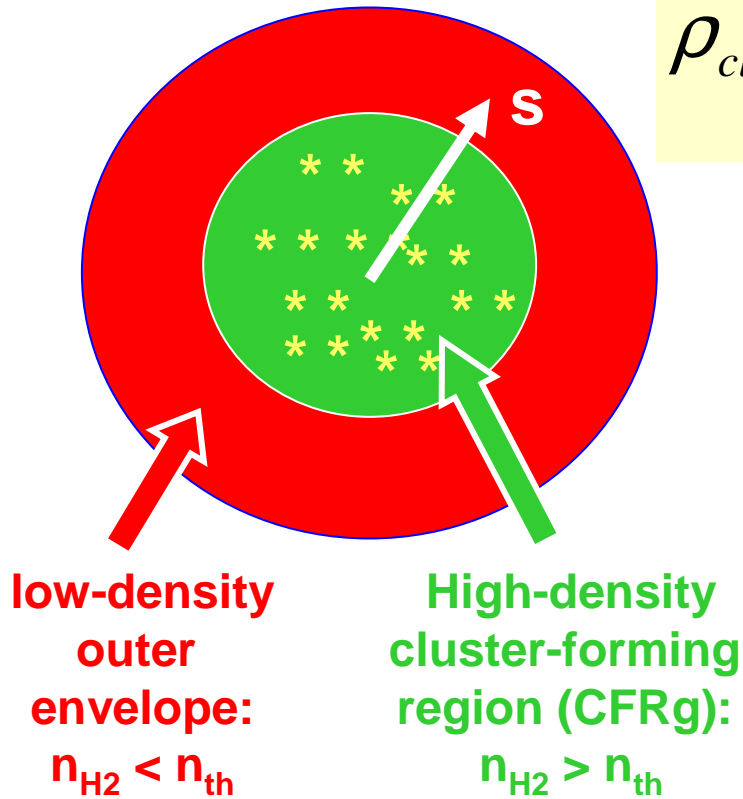


- Constant mean **surface** density clumps  
 → a clump of **higher mass** has a **lower fraction** of its mass above a given volume density threshold

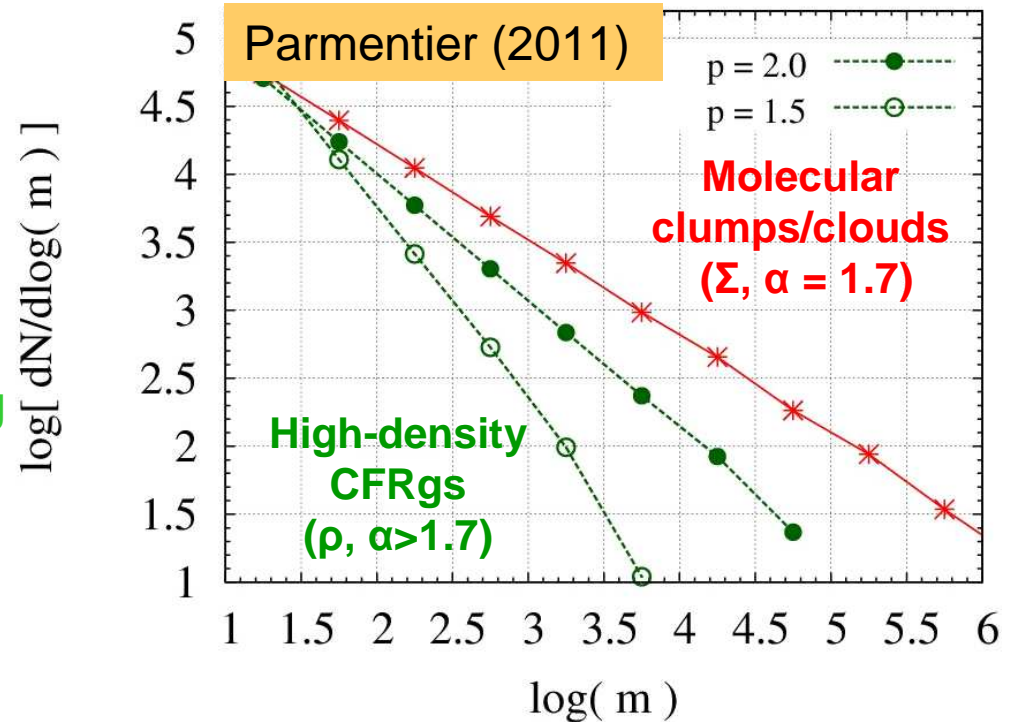
$$\frac{m_{\text{CFRg}}}{m_{\text{clump}}} \propto m_{\text{clump}}^{-?}$$

# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

**Molecular clump:  
2-zone model**



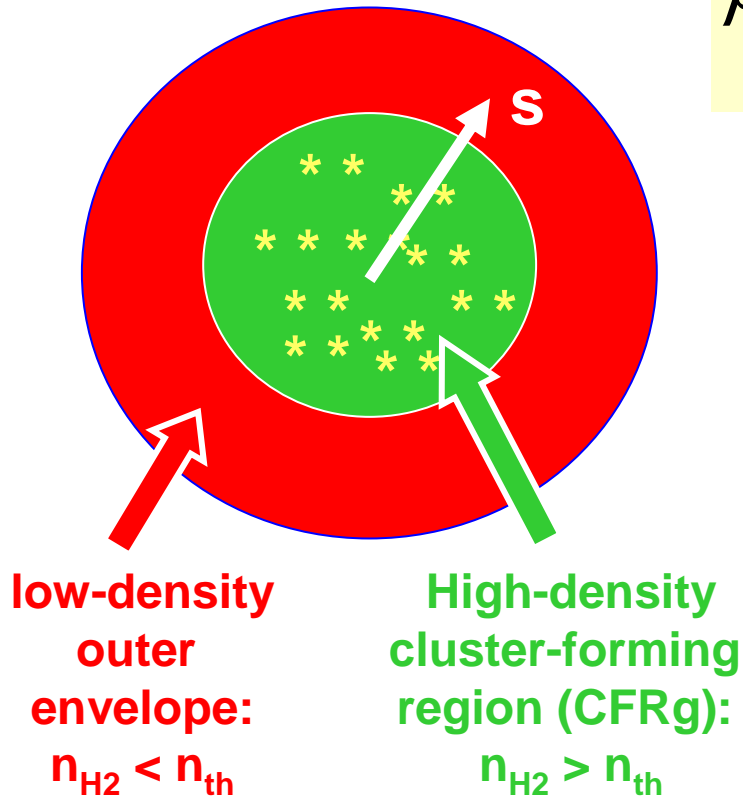
$$\rho_{\text{clump,rad}}(s) \propto s^{-p} : \frac{m_{\text{CFRg}}}{m_{\text{clump}}} \propto m_{\text{clump}}^{-f(p)}$$





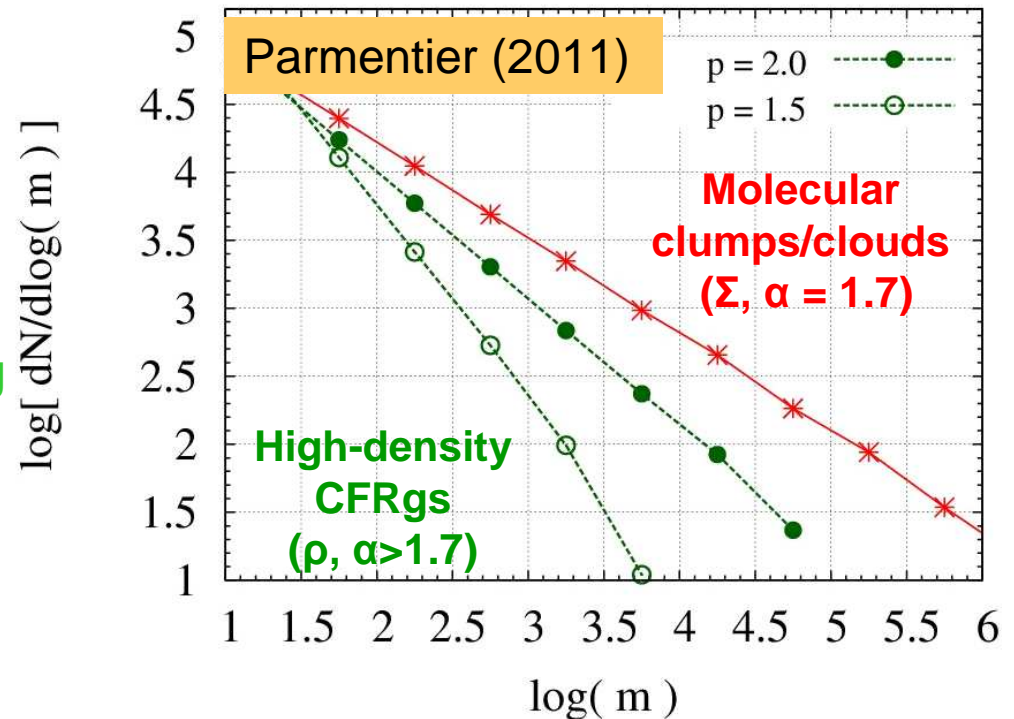
# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

**Molecular clump:  
2-zone model**



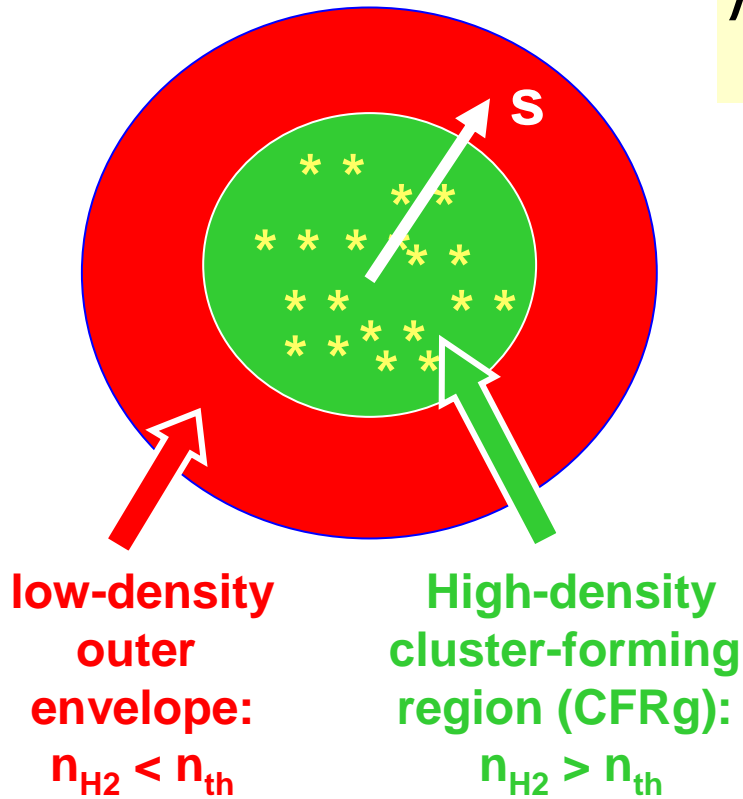
$$\rho_{clump,rad}(s) \propto s^{-1.9} : \frac{m_{CFRg}}{m_{clump}} \propto m_{clump}^{-0.3}$$

**Mueller+02:  
density index  $p \approx 1.8$**



# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

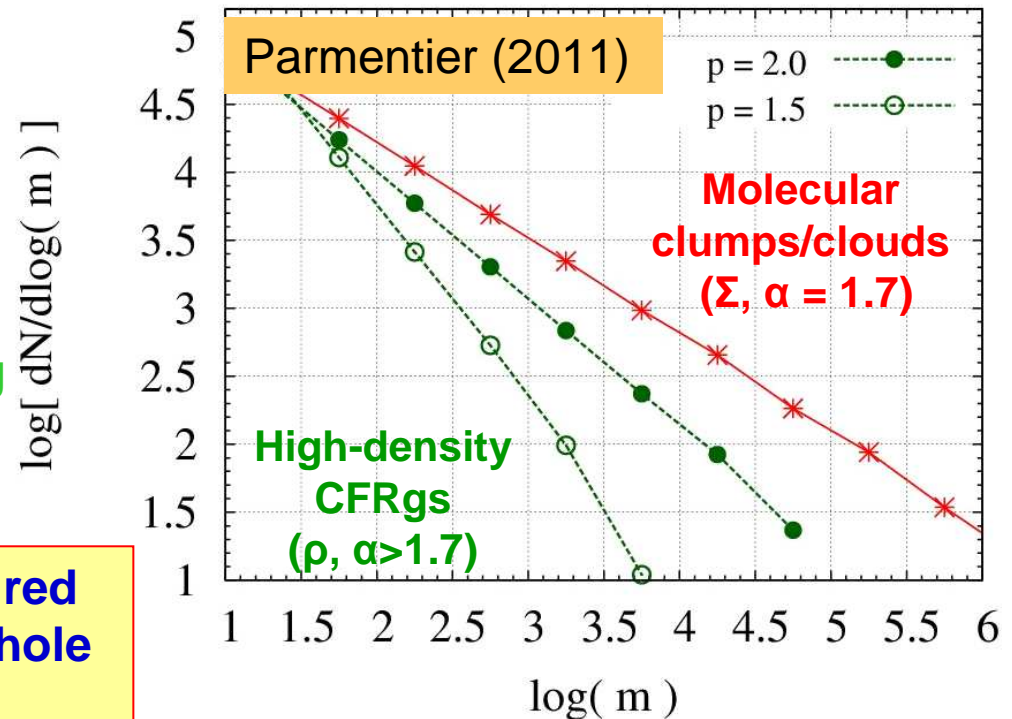
**Molecular clump:  
2-zone model**



**The local SFE must be measured over the CFRg, not over the whole molecular clump**

$$\rho_{clump,rad}(s) \propto s^{-1.9} : \frac{m_{CFRg}}{m_{clump}} \propto m_{clump}^{-0.3}$$

**Mueller+02:**  
density index  $p \approx 1.8$



# Massive Star Formation (MSF) Limit

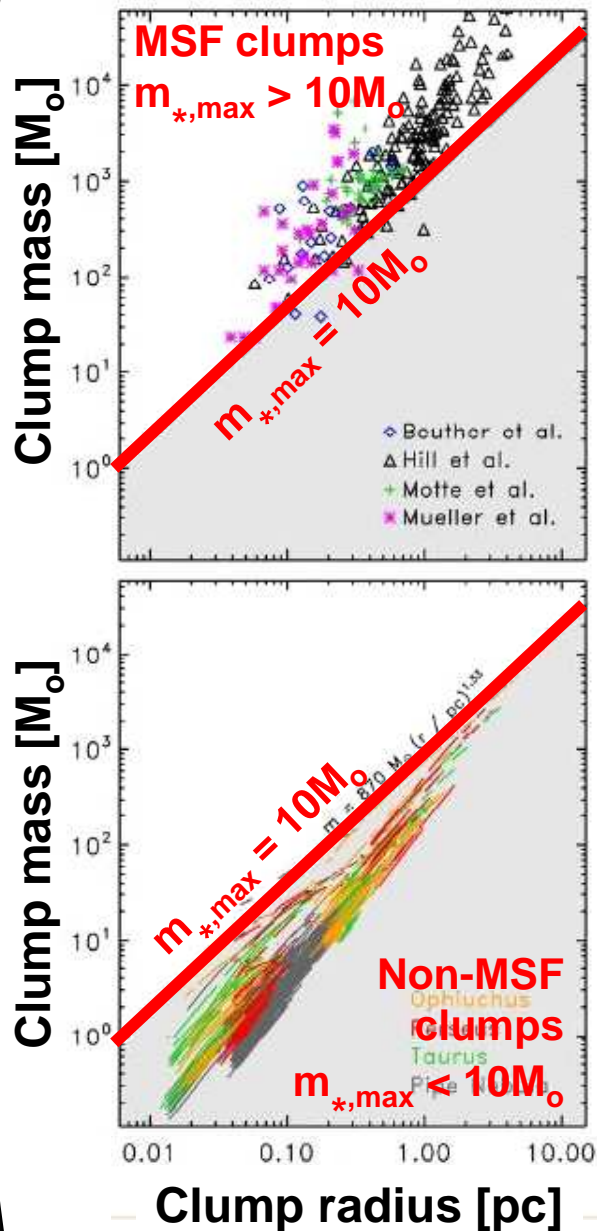


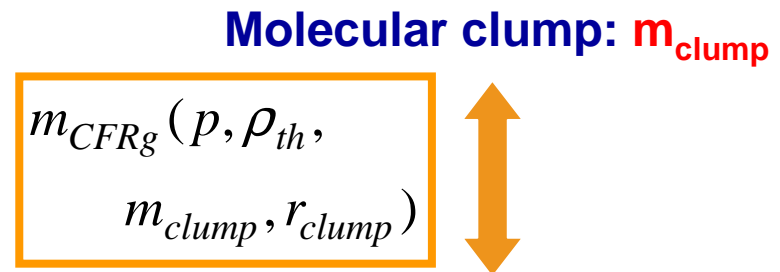
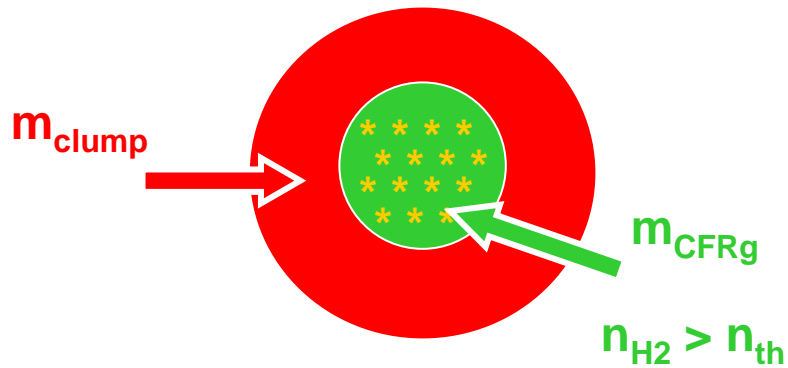
Fig2 and Eq1,  
Kauffmann &  
Pillai (2010)

$$m_{clump} = 870 M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33}$$

Tool to define ALMA targets  
for MSF studies

Intercept and slope?

# What do we need to form a $10M_{\odot}$ star?



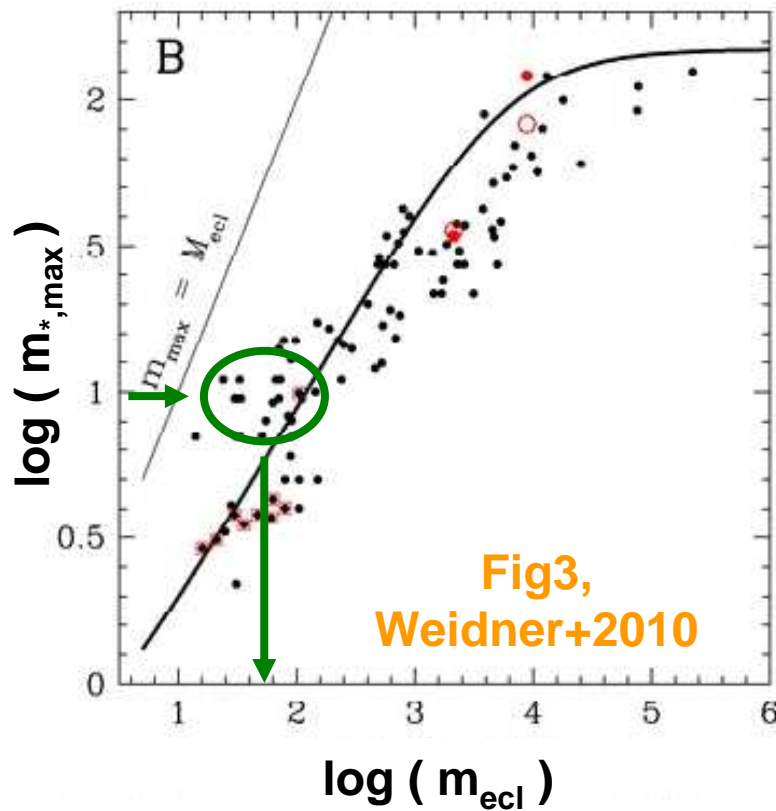
**Star-forming gas:**  
 $m_{\text{CFRg}} > 150M_{\odot}$

**SFE = 0.3**

**Embedded-cluster:**  
 $m_{\text{ecl}} > 50M_{\odot}$

**( $m_{\text{ecl}}, m_{*,\text{max}}$ )  
 relation**

**Most-massive star:**  
 $m_{*,\text{max}} > 10M_{\odot}$



# What do we need to form a $10M_{\odot}$ star?

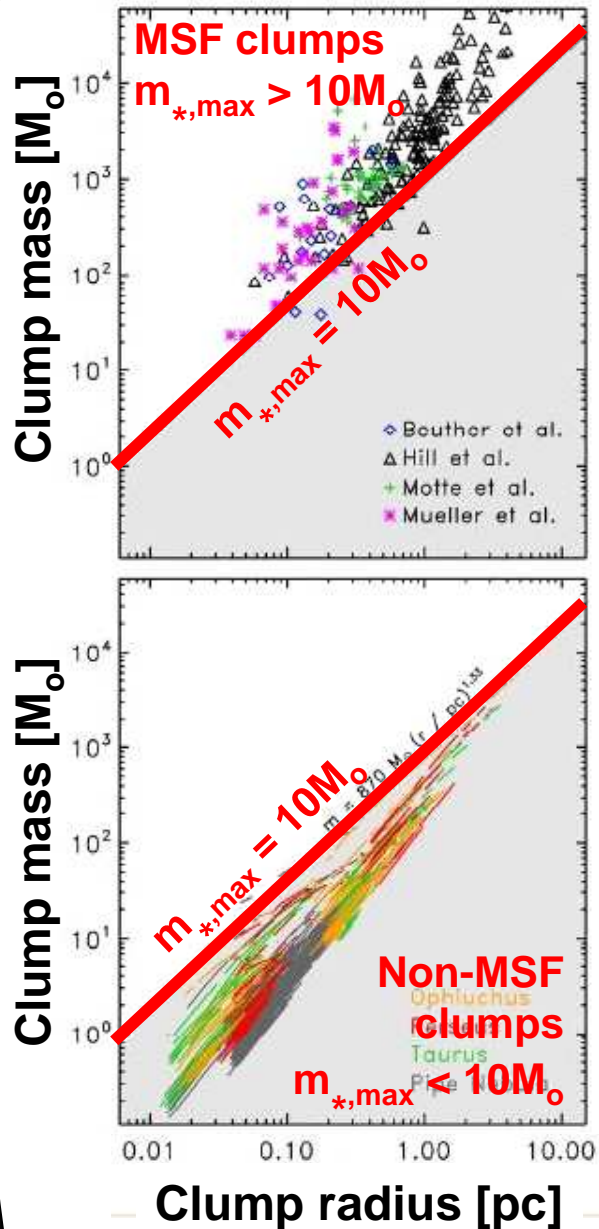


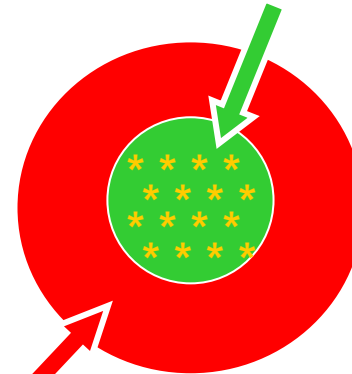
Fig2,  
Kauffmann &  
Pillai (2010)

Volume density threshold  
for overall star formation:

$$n_{\text{H}_2} > n_{\text{th}}$$

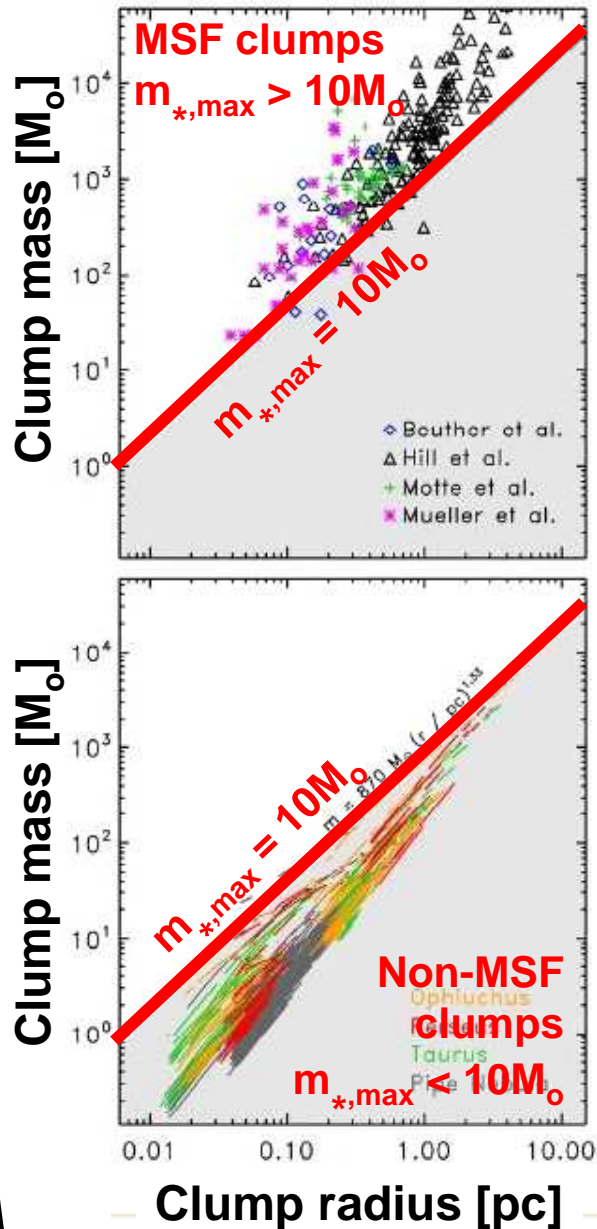
$$m_* = 10M_{\odot} : m_{\text{CFRg}} = \frac{m_{\text{ecl}}}{\text{SFE}} \cong 150M_{\odot}$$

$$\langle n_{\text{CFRg}} \rangle = \text{few} \times n_{\text{th}}$$



$$m_{\text{clump}} = 870M_{\odot} \left( \frac{r_{\text{clump}}}{\text{pc}} \right)^{1.33}$$

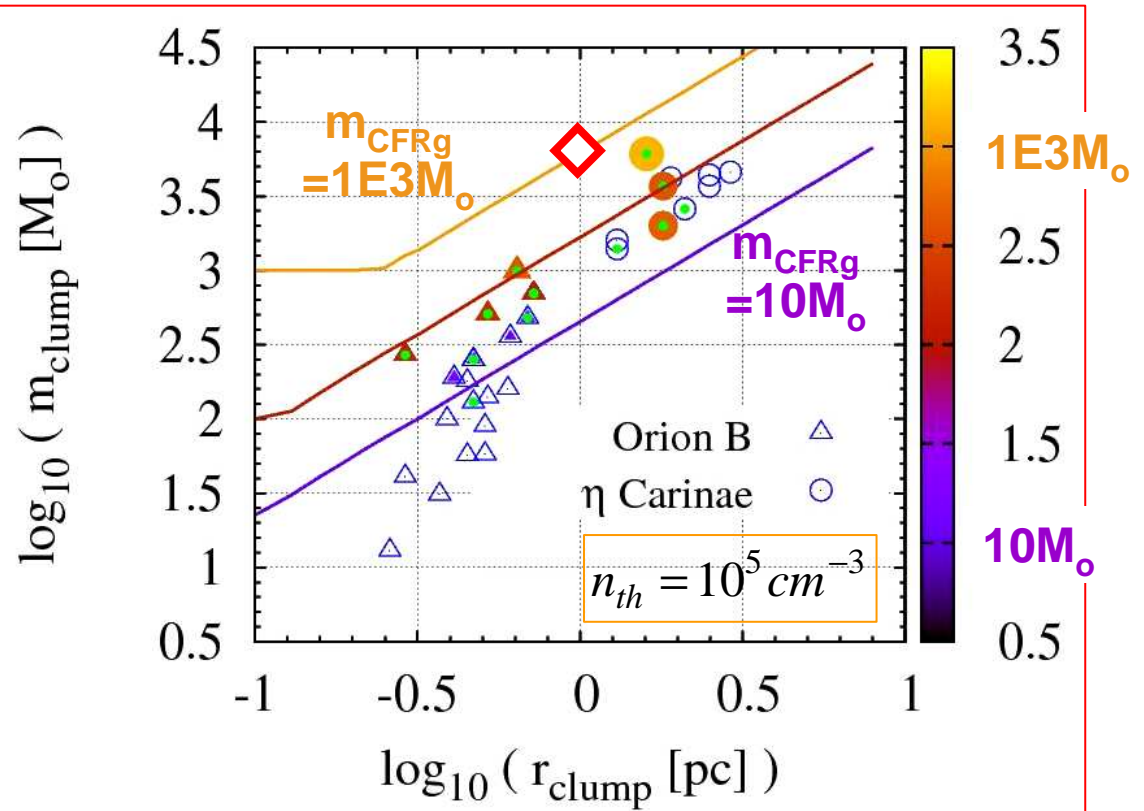
# Iso- $m_{\text{CFRg}}$ in the clump mass-size space



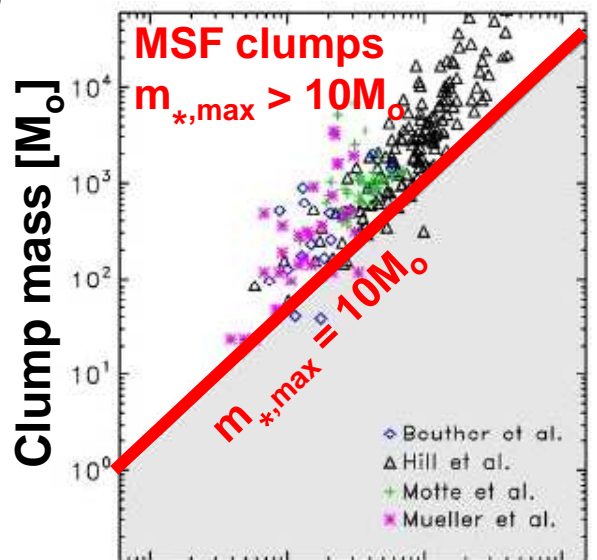
**Fig2,**  
**Kauffmann &**  
**Pillai (2010)**

$$m_{\text{clump}} = \left(m_{\text{CFRg}}\right)^{p/3} \left(\frac{4\pi\rho_{\text{th}}}{3-p}\right)^{(3-p)/3} r_{\text{clump}}^{3-p}$$

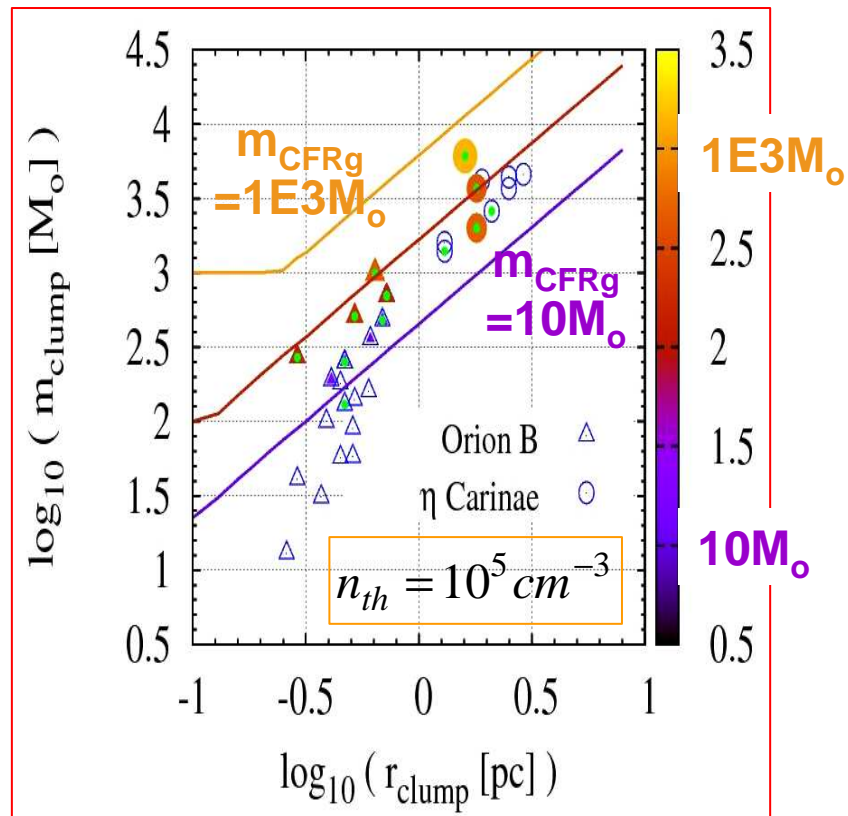
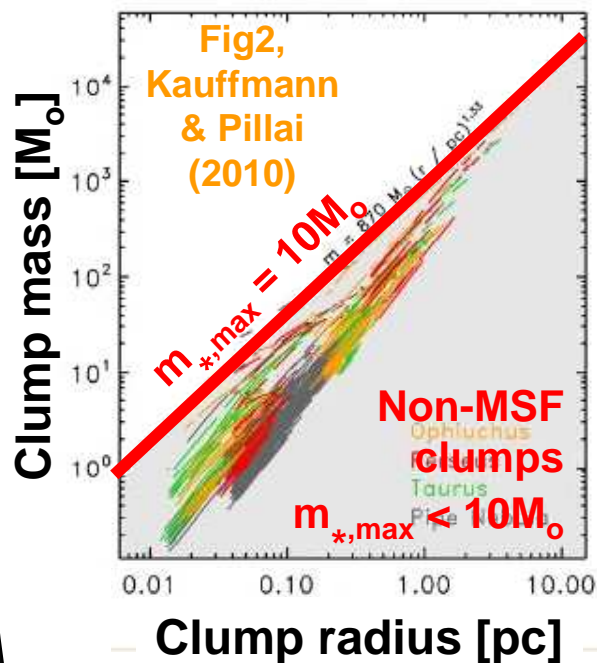
Parmentier (2011), Eq.3



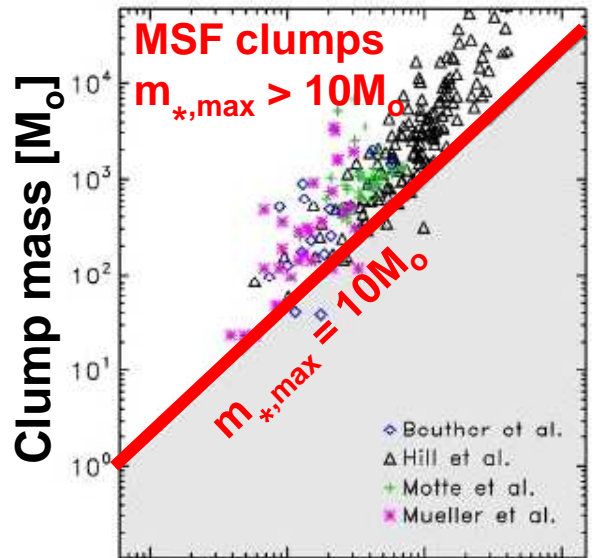
# Iso- $m_{\text{CFRg}}$ in the clump mass-size space



$$m_{\text{clump}} = 870M_{\odot} \left( \frac{r_{\text{clump}}}{\text{pc}} \right)^{1.33} = m_{\text{CFRg}}^{p/3} \left( \frac{4\pi\rho_{\text{th}}}{3-p} \right)^{(3-p)/3} r_{\text{clump}}^{3-p}$$



# Matching Observed MSF Limit & Iso- $m_{\text{CFRG}}$ Model



Matching the slopes:

$$m_{\text{clump}} = 870M_{\odot} \left( \frac{r_{\text{clump}}}{\text{pc}} \right)^{1.33} = m_{\text{CFRG}}^{p/3} \left( \frac{4\pi\rho_{\text{th}}}{3-p} \right)^{(3-p)/3} r_{\text{clump}}^{3-p}$$

MSF limit:

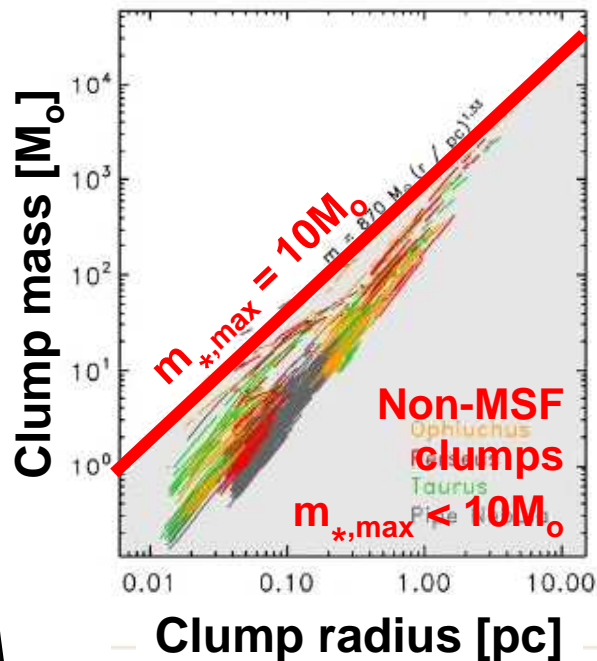
$p=1.7$  (Parmentier+ 2011)

GMC/SC MFs:

$p=1.9$  (Parmentier 2011)

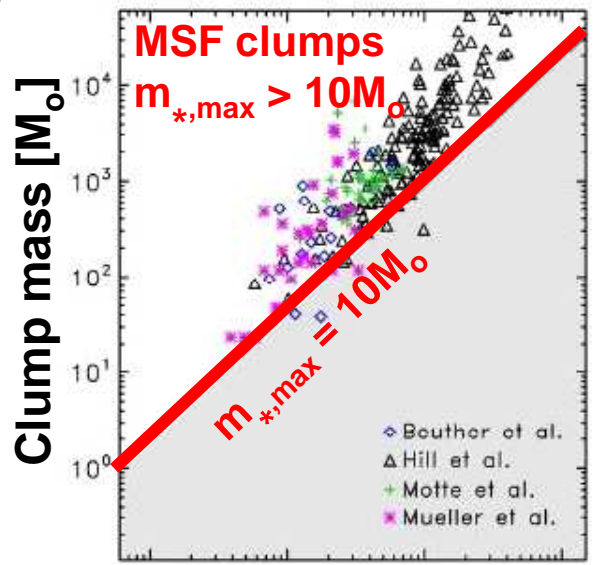
Dust Cont. mapping:

$p=1.8$  (Mueller+ 2002)





# Matching Observed MSF Limit & Iso- $m_{\text{CFRG}}$ Model



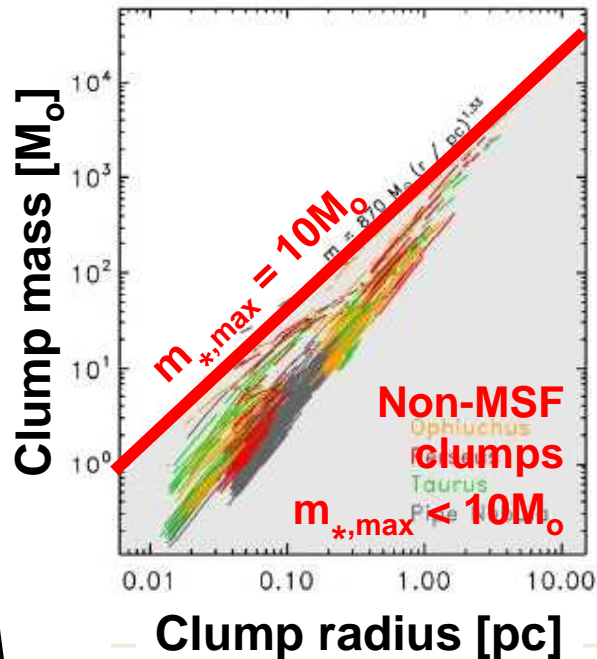
Matching the slopes:

$$m_{clump} = 870 M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33} = m_{CFRg}^{p/3} \left( \frac{4\pi\rho_{th}}{3-p} \right)^{(3-p)/3} r_{clump}^{3-p}$$

**MSF limit:**  $p=1.7$  (Parmentier+ 2011)

**GMC/SC MFs:**  $p=1.9$  (Parmentier 2011)

**Dust Cont. mapping:**  $p=1.8$  (Mueller+ 2002)



Matching the intercepts:

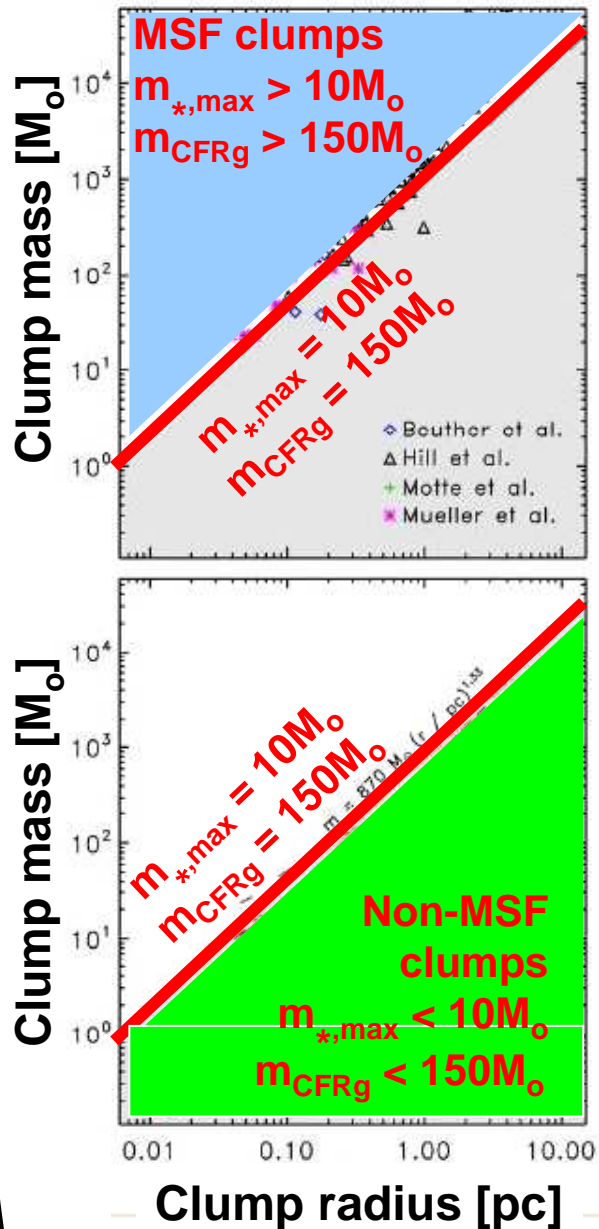
$$m_{clump} = 870 M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33} = m_{CFRg}^{p/3} \left( \frac{4\pi\rho_{th}}{3-p} \right)^{(3-p)/3} r_{clump}^{3-p}$$

▶ Parmentier+ (2011),  $m_{\text{CFRg}} = 150 M_{\odot}$ :

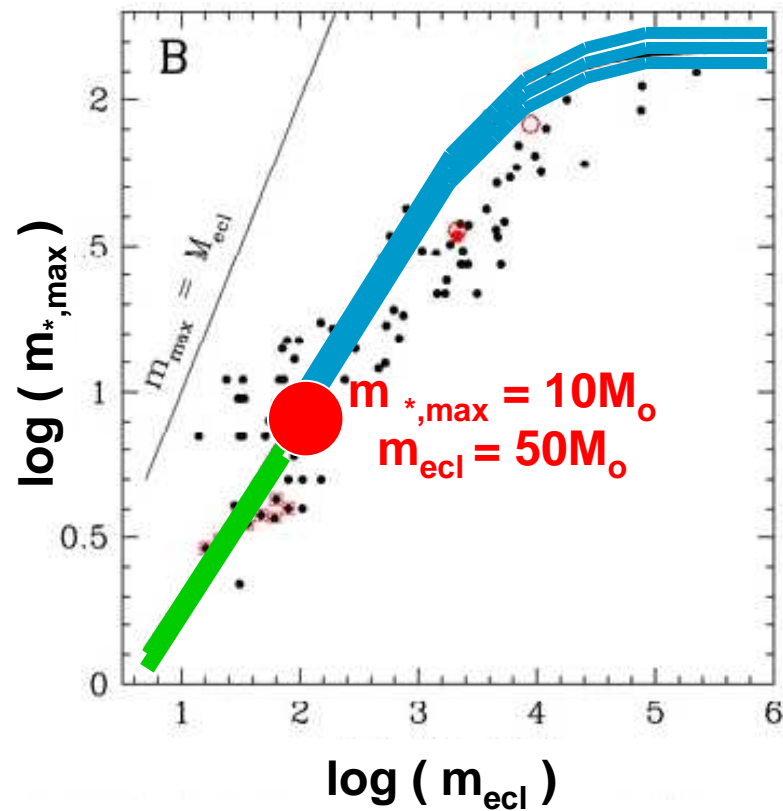
▶ Lada, Lombardi & Alves (2010):

$$n_{\text{th,H2}} = 10^4 \text{ cm}^{-3}$$

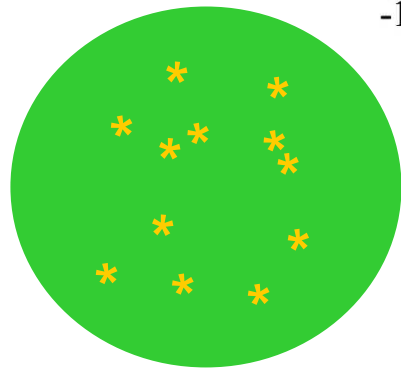
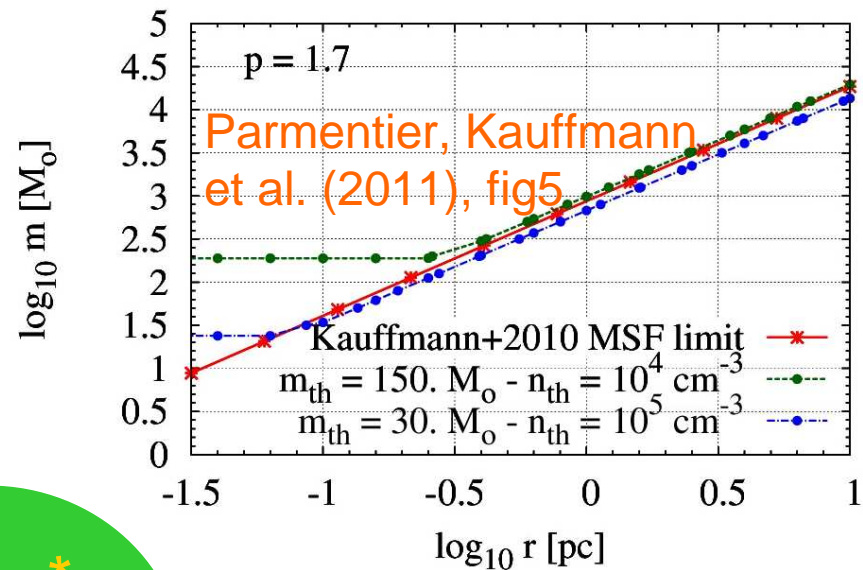
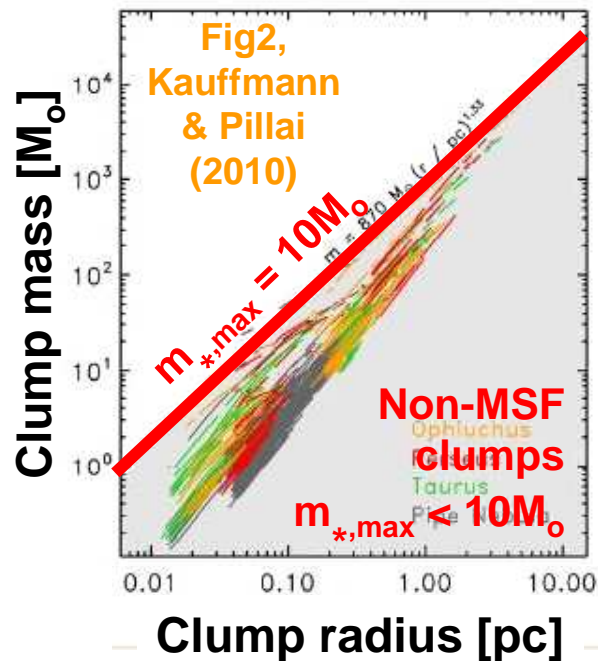
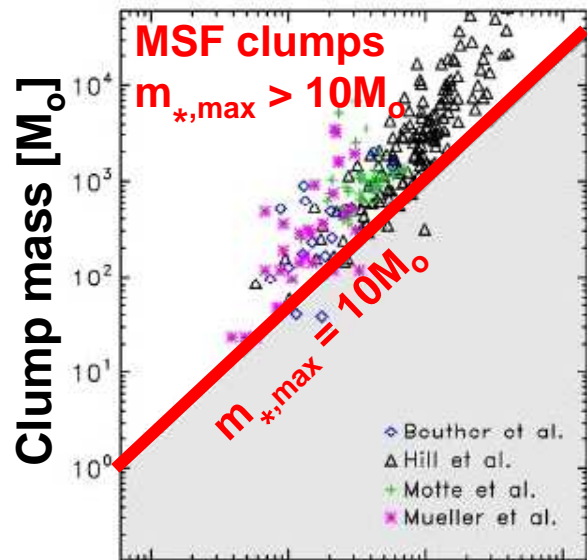
# MSF Limit: Quick overview



The observational MSF limit is consistent with a threshold in SF gas mass beyond which the SF gas reservoir is large enough to allow the formation of massive stars.

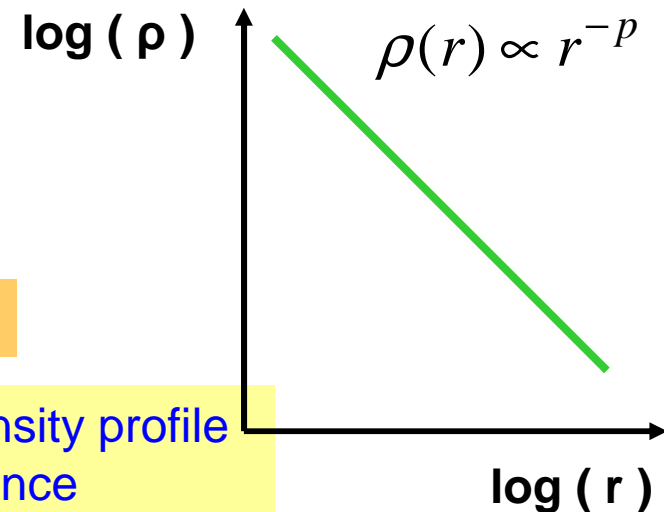


# MSF Limit on Smaller Spatial Scales



Elmegreen (2011):

Mean power-law density profile  
+ supersonic turbulence  
→ Density peaks  $10^5 \text{ cm}^{-3}$   
≡ pre-stellar cores:



# Conclusions

## Properties of young star cluster systems

- sharp insights into the clustered mode of star formation
- star formation conditions determine what mass fraction clusters lose as they age
- information needed to reconstruct galaxy SFH
- time-variations ? (e.g. metallicity)

“Even a long journey starts with a one single step”  
Oriental saying

An exciting era has just started:  
HERSCHEL, ALMA, ...

