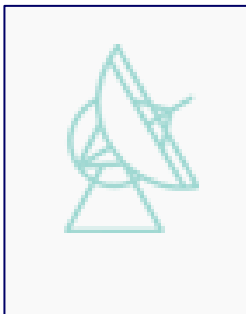


Vienna Institute of Astronomy - 16 May 2011

**From  
Cluster-Forming Region Properties  
to Galaxy Evolution  
with Star Clusters**

**Geneviève Parmentier**



**Max-Planck-Institut für Radioastronomie  
Argelander-Institut für Astronomie**



**Bonn, Deutschland**

# Image Credit

- **Elliptical galaxy M87** (APOD 16.06.2004):
  - Canada-France Hawaii Telescope, J.-C. Cuillandre
- **Globular Cluster M10** (APOD 30.06.2001):
  - Till Credner, Sven Kohle (Bonn University), Hoher List Observatory
- **Orion Nebula Mosaic** (HST – WFPC2):
  - O'Dell and S.K. Wong (Rice University), NASA
- **Open Cluster Pleiades M45** (APOD 01.12.2002):
  - Anglo-Australian Observatory/Royal Observatory, Edinburgh
- **Open Cluster Hyades:**
  - <http://stars.astro.illinois.edu/sow/hyades-p.html> , by Jim Kaler
- **Spiral galaxy NGC3370** (APOD 14.05.2005):
  - Hubble Heritage Team, A. Riess (STScI) NASA

# Star Clusters: at the crossroad between star formation and galaxy evolution

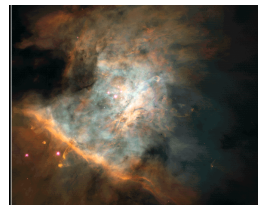
a few kpc - 100kpc:  
systems of  
star clusters  
and galaxies



10pc:  
individual  
gas-free  
star clusters



1-pc:  
star formation  
in embedded  
star clusters



# Setting the Scene: Star Clusters (SC) as Powerful Tracers of Galaxy Evolution

## Star Clusters (SC):

- Compact groups of coeval stars bound together by gravity
- Identified on a one-by-one basis against the background of their host galaxy

## Multi-band imaging of SC systems

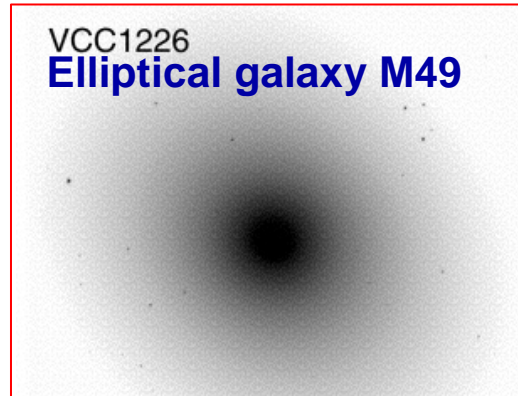
- (→ cluster magnitudes, colours)
- feasible out to Virgo Galaxy Cluster distances ( $\approx 20\text{Mpc}$ )
- combined to Simple Stellar Population models  
→ estimates of **cluster age, mass, metallicity**

## Comprehensive view of galaxy-:

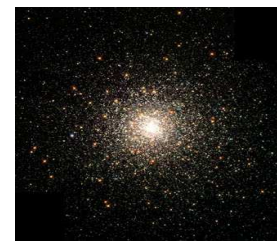
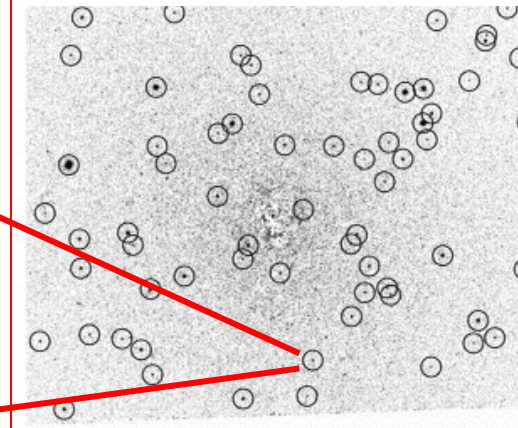
- chemical enrichment history,
  - interaction history,
  - star formation history
- over the past Hubble-Time**

Jordan+04 (Virgo Galaxy Cluster ACS Survey II, fig6)

VCC1226  
Elliptical galaxy M49



Background-subtracted image



**Star clusters are at the very heart of many astrophysical topics**

# The Big Issue: SCs versus field stars

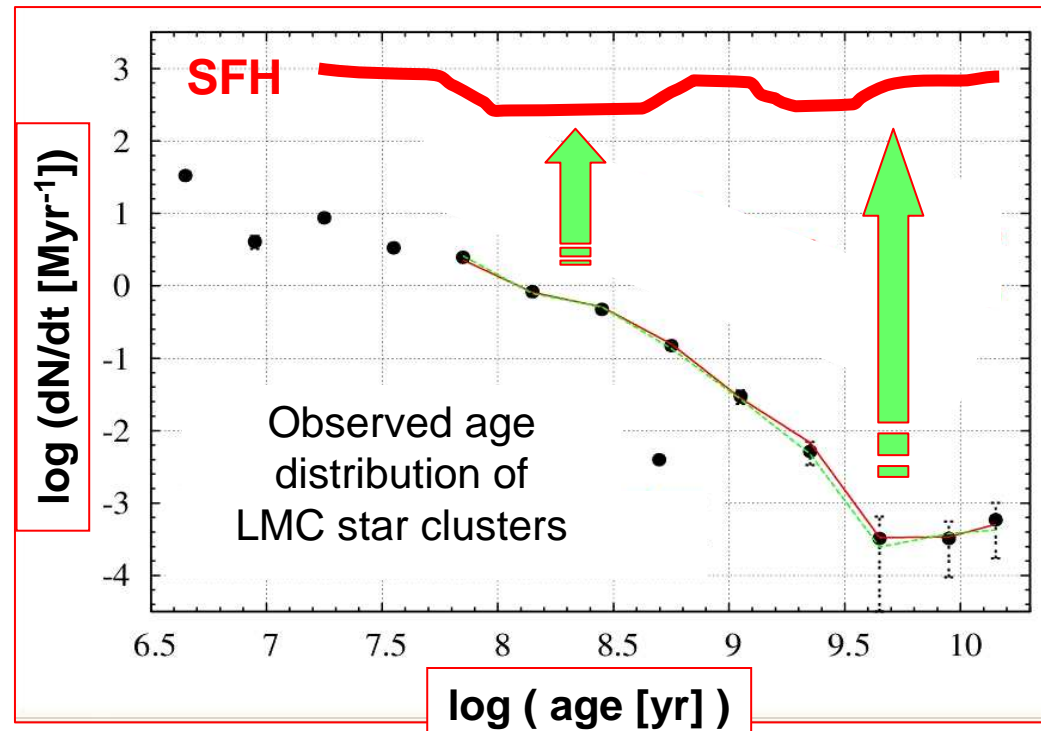
Most stars in our Galaxy:

- ✿ are born in **SCs** → young SCs tell us about star formation
- ✿ but are observed as **field stars**
- ✿ SCs start losing stars as soon as they are born ...

Star clusters have the potential of tracing

➤ galaxy star formation histories

provided we get a firm handle on the ratio of star formation still residing in (observed) star clusters as a function of age

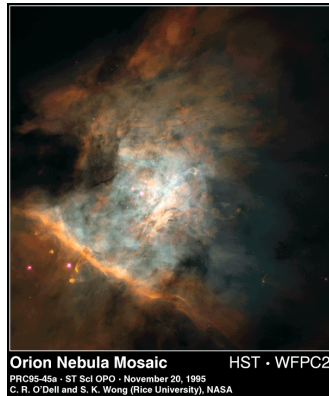


**Violent relaxation = Most traumatizing phase**

- Very short (10-50 Myr)
- SC Dynamical response to residual star-forming gas expulsion

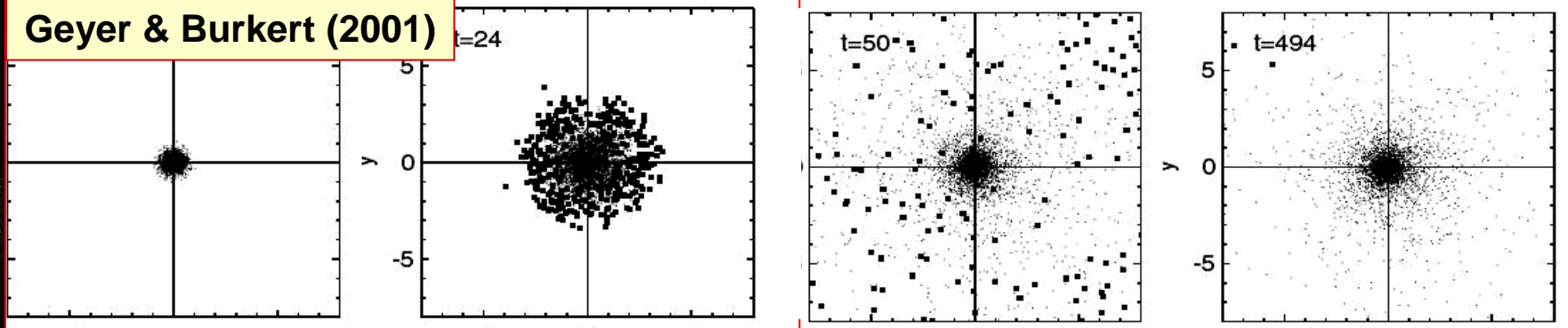


# Intra-Cluster Gas-Expulsion and Violent Relaxation



time

Geyer & Burkert (2001)



## Effects of gas expulsion - VIOLENT RELAXATION

- ☀ Cluster expansion
- ☀ Star loss (infant weight-loss), or
- ☀ Cluster dissolution (infant mortality)

# Violent Relaxation (VR): Observable Signatures And Prime Parameters

## Effects of gas expulsion - VIOLENT RELAXATION

- ☀ Cluster expansion
- ☀ Cluster infant weight-loss and infant mortality

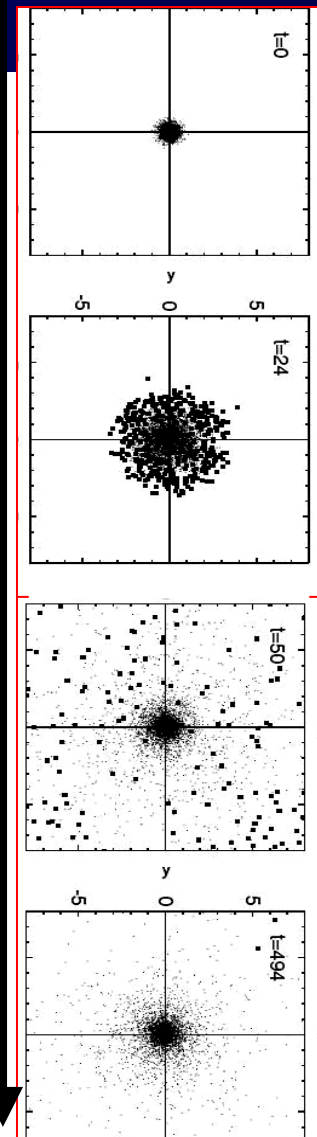
## Observable Imprints upon Star Cluster Systems :

- Cluster **mass** distribution,
- Cluster **age** distribution,
- Cluster **radius** distribution,

## Prime parameters: (e.g. Baumgardt & Kroupa 2007)

- **SFE** in cluster-forming region (CFRg)
- Gas expulsion time-scale:  $\tau_{\text{GExp}} / \tau_{\text{cross}}$
- **Impact** of external **tidal field** (environment)

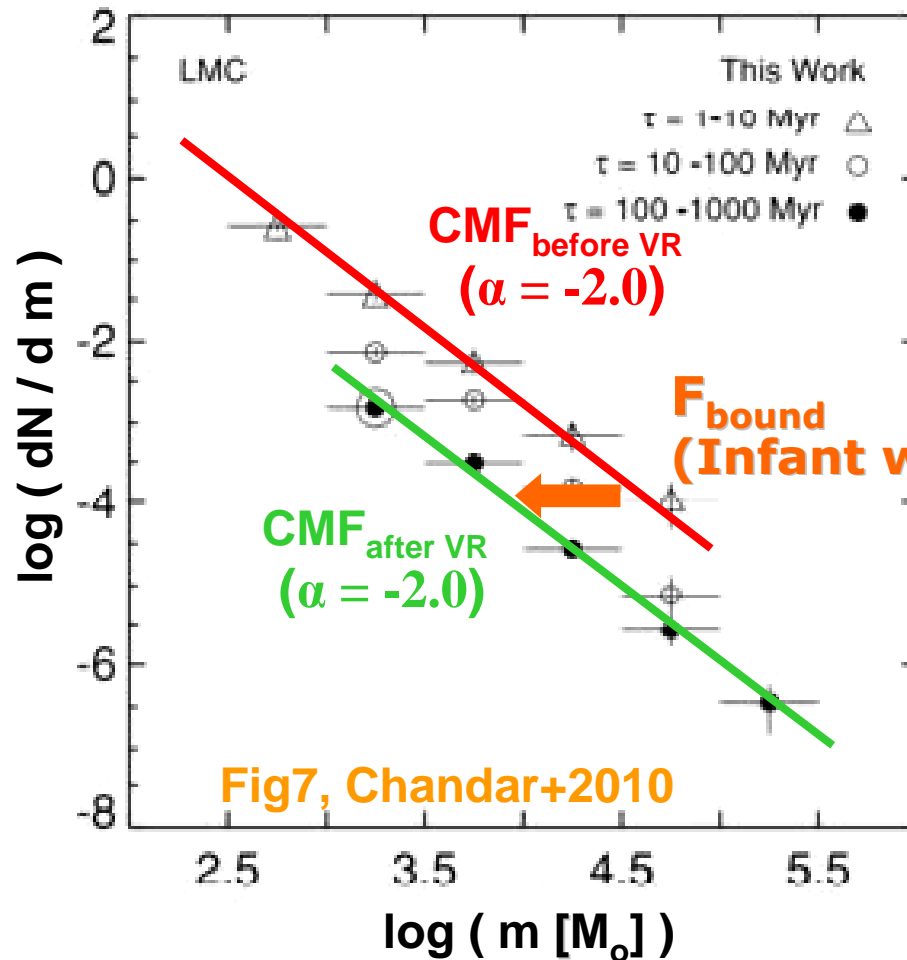
See also Adams (2000), Vesperini et al (2009), ...



Geyer & Burkert (2001)

# Violent Relaxation (VR): SC Mass Functions

Time-Evolution of SC Mass Functions: What observers tell us ...  
 No evolution of the MF shape over the first few 10Myr



$$\frac{dN}{dm} \propto m^{-2}$$

$$\equiv \frac{dN}{d \log m} \propto m^{-1}$$

$$m_{cluster} \text{ (end of VR)}$$

$$= F_{bound} \times m_{ecl} \text{ (at Gas Exp)}$$

**$F_{bound}$  is mass-independent**

Note: what happens after 100Myr remains disputed ...



# SFE and SC Mass Functions

$$m_{cluster}(\text{end of VR}) = F_{bound}(SFE) \times SFE \times m_{CFRg}$$

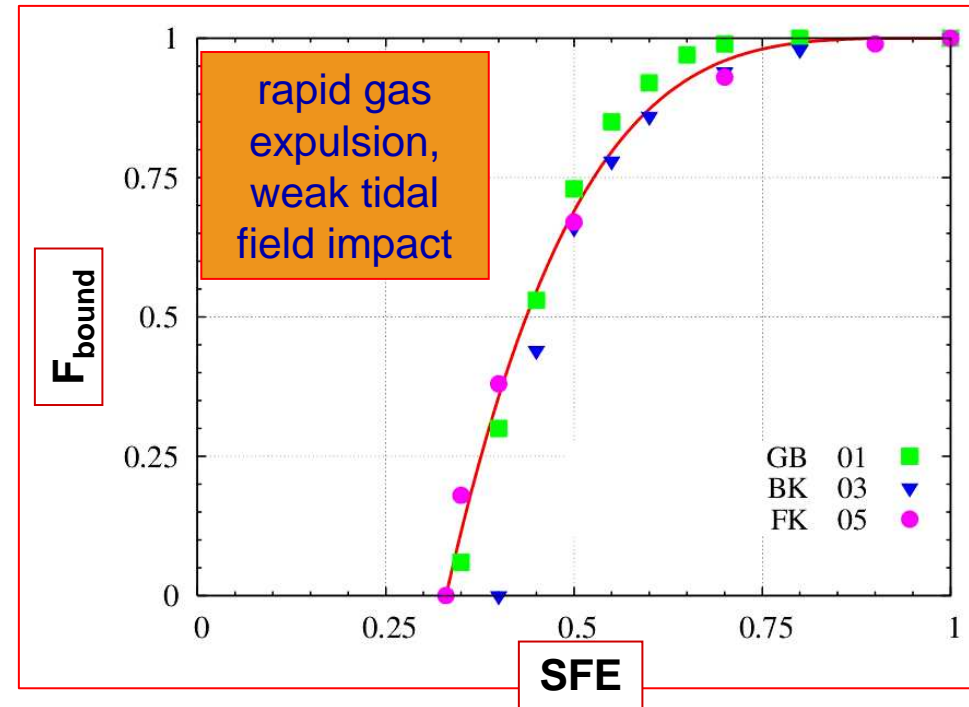
$$F_{bound}(SFE \ \varepsilon)$$

**SFE**

= fraction of gas ending up in stars

**$F_{bound}$**

= fraction of stars remaining bound to the cluster at the end of VR



**$F_{bound}$  is mass-independent**  
→ **SFE is mass-independent**

# $\tau_{GExp}/\tau_{cross}$ and SC Mass Functions

$$F_{bound} \left( \text{SFE } \varepsilon, \frac{\tau_{GExp}}{\tau_{cross}} \right)$$

Parmentier, Goodwin et al. (2008)  
Kroupa & Boily (2002)

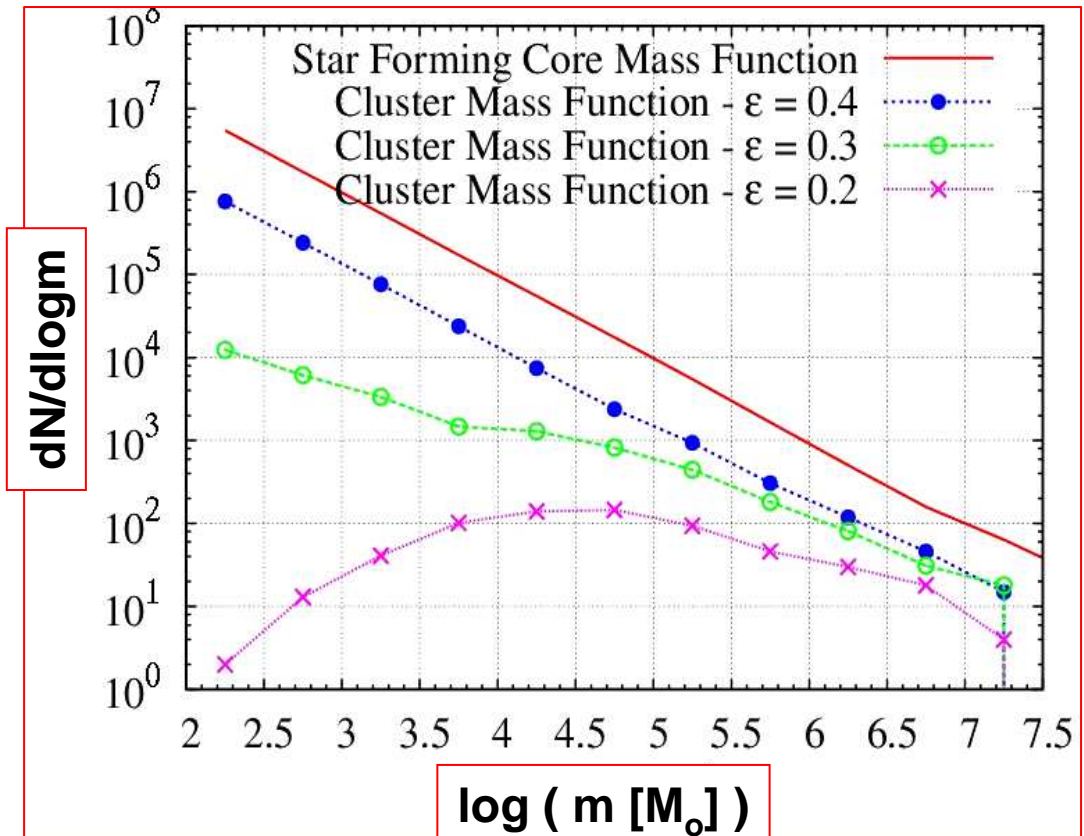
**Constant radius:**  
more massive star cluster progenitors have

- a deeper potential well
- a slower gas-expulsion t-s
- can survive despite a **low SFE** of, say, 20%

**$F_{bound}$  is mass-independent**

**$\rightarrow \tau_{GExp}/\tau_{cross}$  is mass-independent**

**but looser constrain**



# Tidal Field Impact

$$F_{bound} \left( \text{SFE } \varepsilon, \frac{\tau_{GExp}}{\tau_{cross}}, \frac{r_{half-mass}}{r_{tidal}} \right)$$

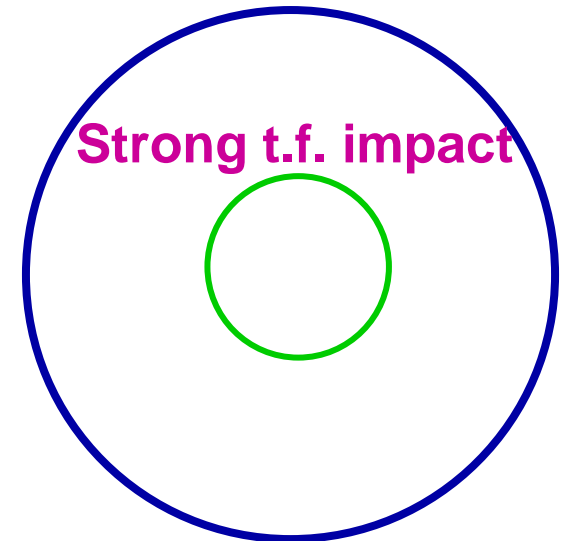
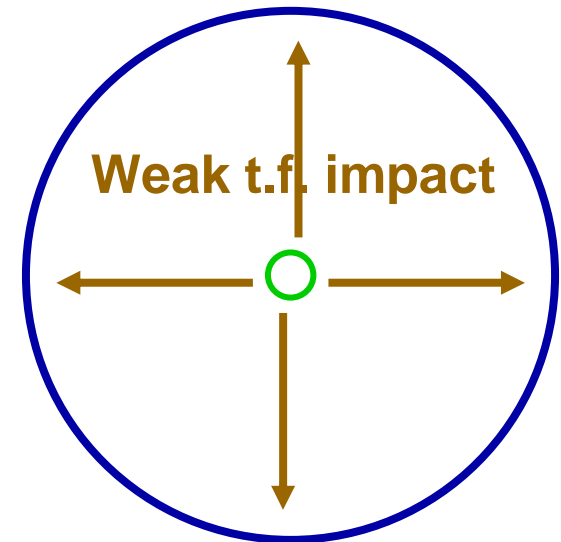
Half-mass radius  $r_{half-mass} \approx r_{CFRg}$

Limiting tidal radius :

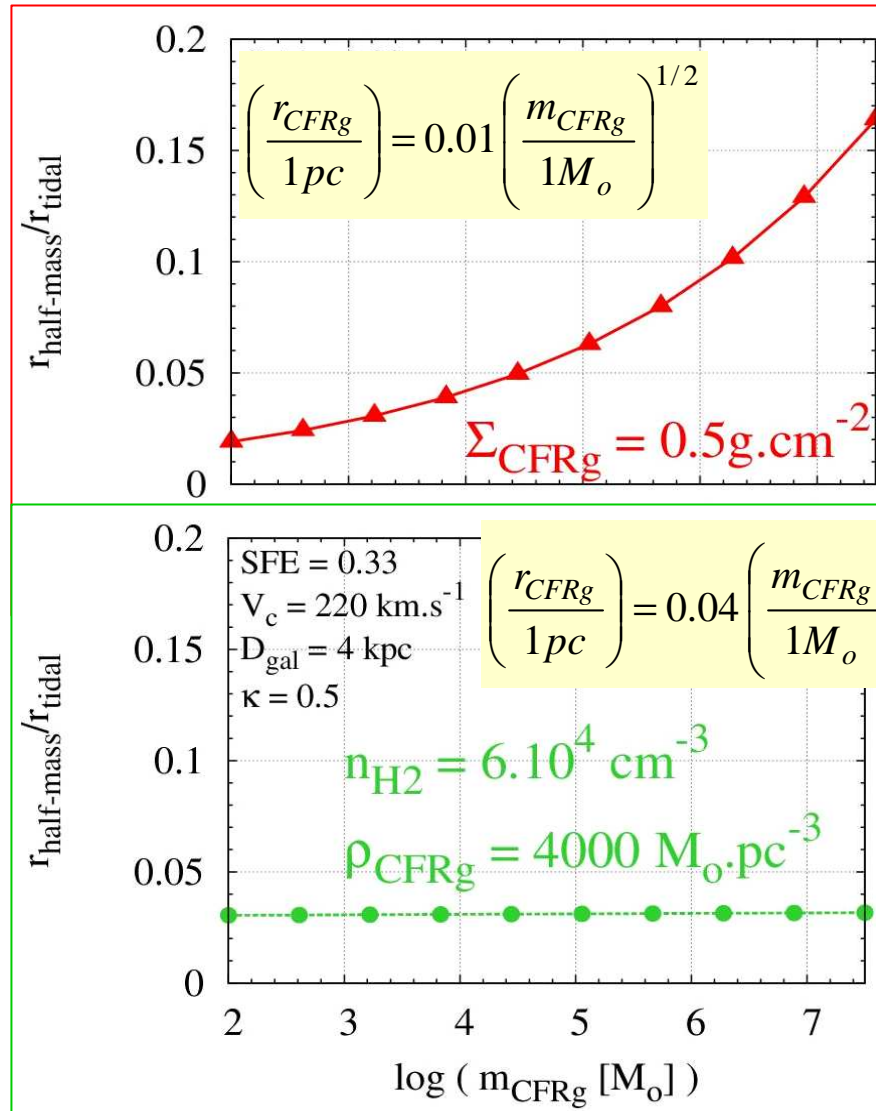
$$r_{tidal} = (m_{ecl})^{1/3} \left( \frac{G D_{gal}^2}{2 V_c^2} \right)^{1/3} \propto (SFE \cdot m_{CFRg})^{1/3}$$

Embedded cluster mass

SC environment



# Half-Mass Radius—to—Tidal Radius Ratio

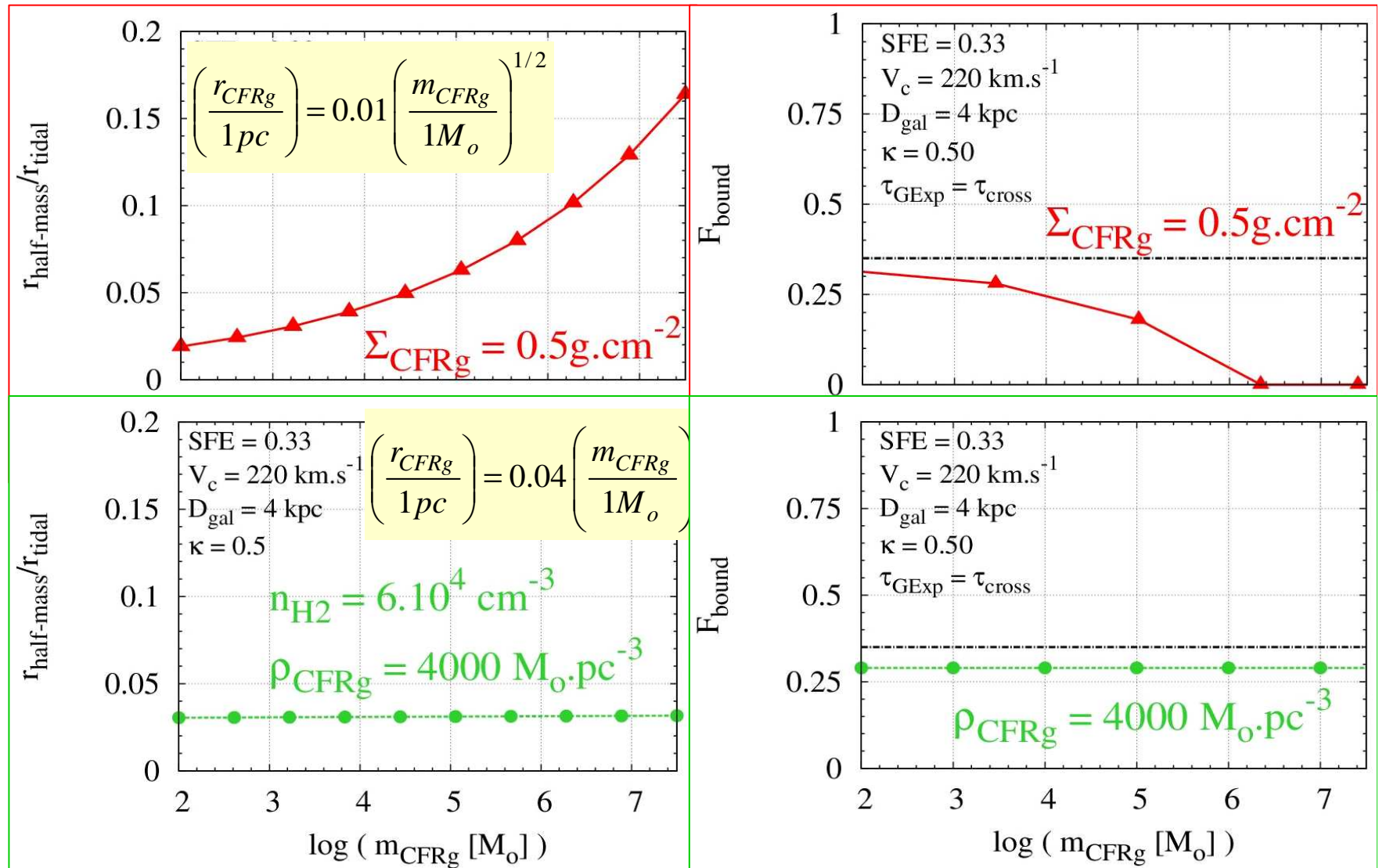


$$r_{\text{CFRg}} \propto r_{\text{half-mass}} \propto m_{\text{CFRg}}^{\delta}$$

$$r_{\text{tidal}} \propto m_{\text{ecl}}^{1/3} \propto m_{\text{CFRg}}^{1/3}$$

$$\frac{r_{\text{half-mass}}}{r_{\text{tidal}}} = m_{\text{CFRg}}^{\delta-1/3}$$

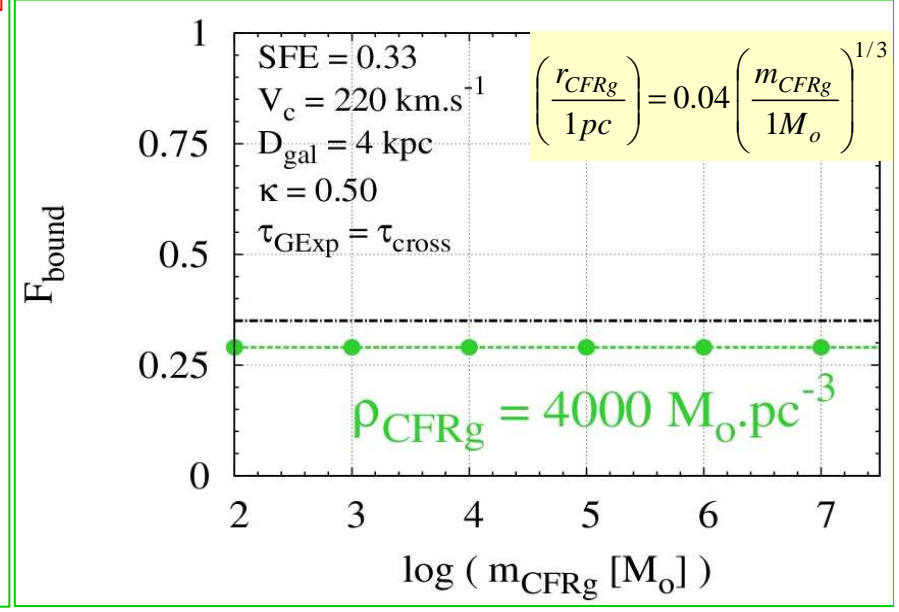
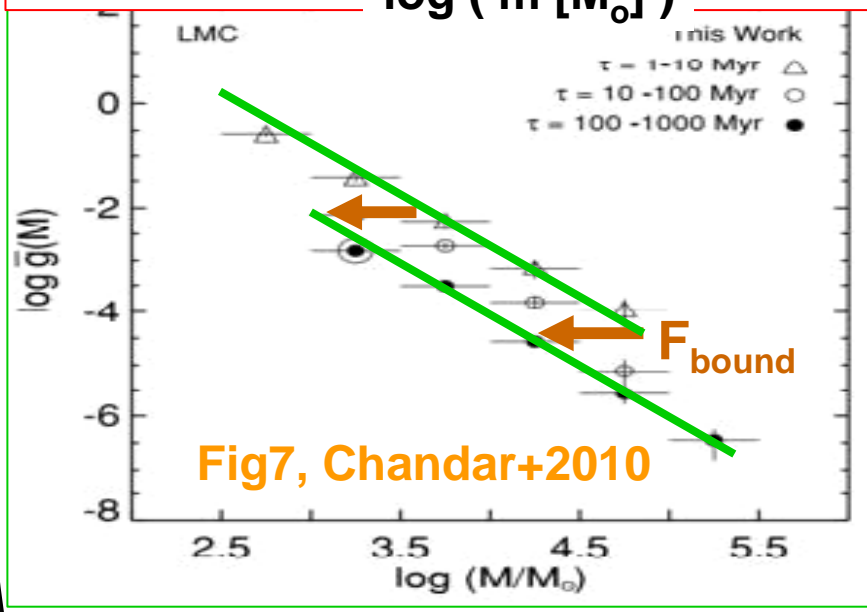
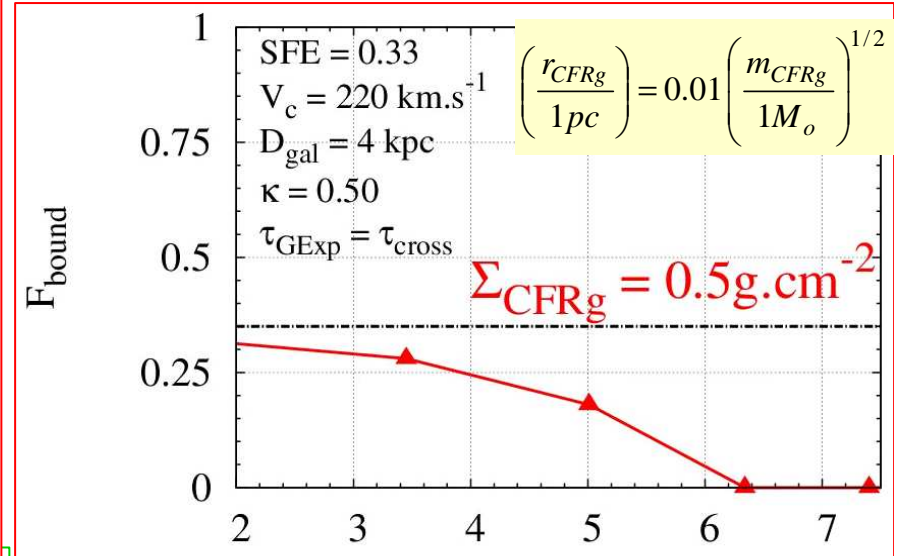
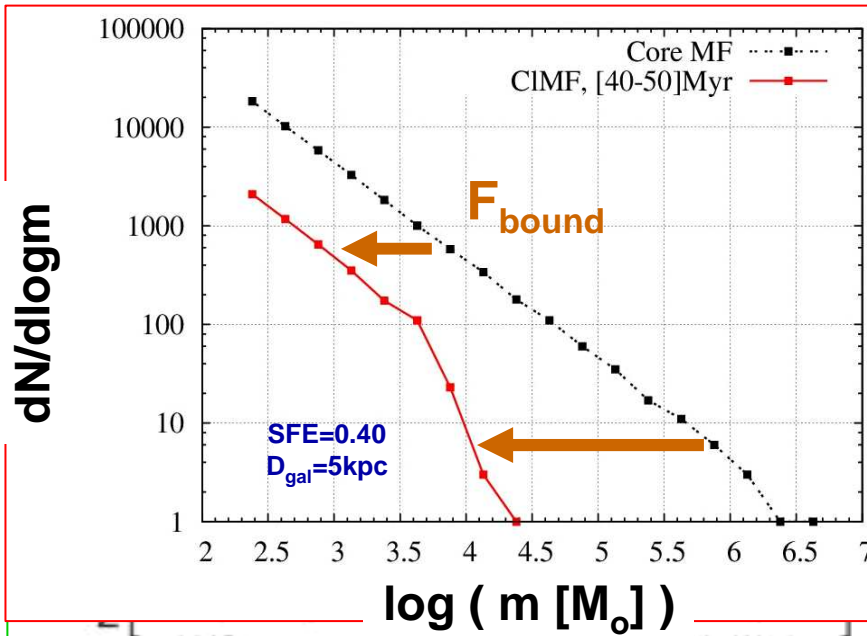
# Bound Fractions at the End of Violent Relaxation



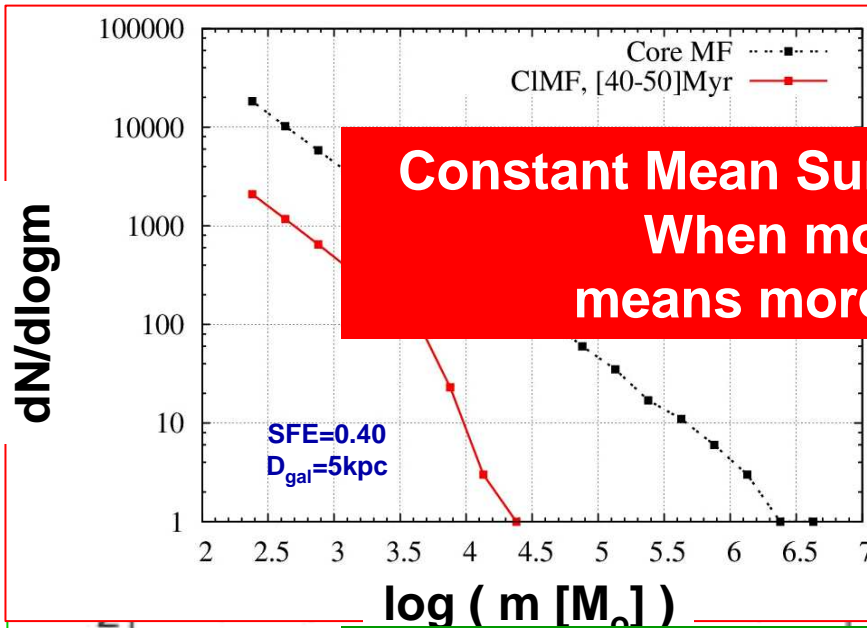
Parmentier & Kroupa (2011)



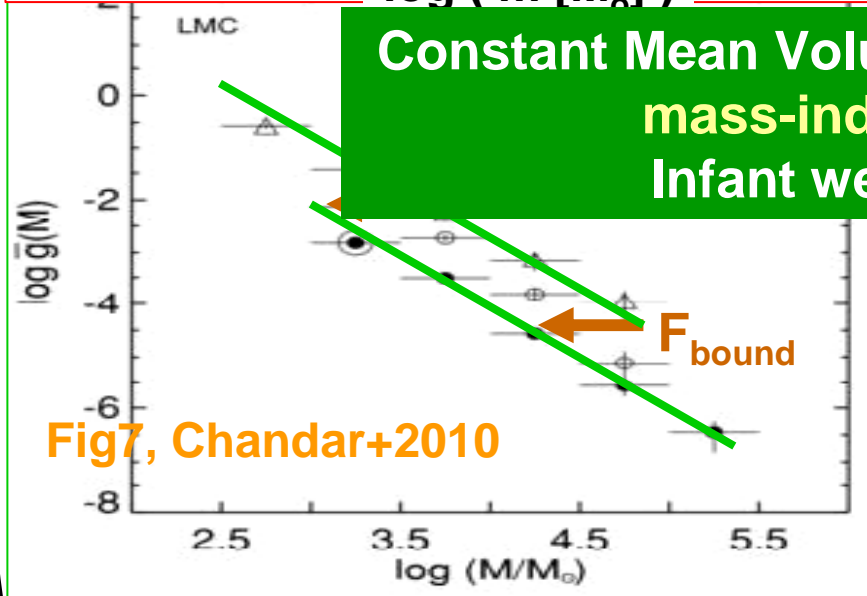
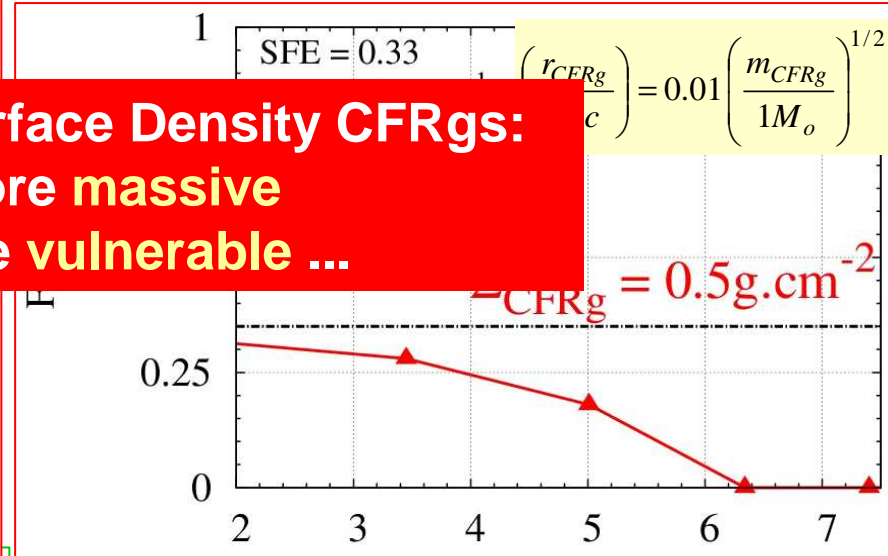
# Young SC Mass Functions



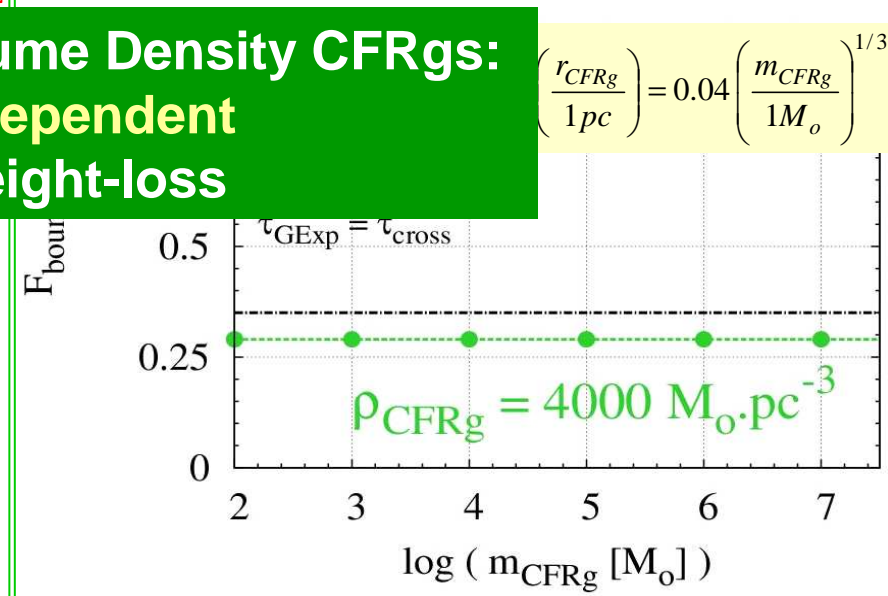
# Young SC Mass Functions



**Constant Mean Surface Density CFRGs:**  
When more massive  
means more vulnerable ...



**Constant Mean Volume Density CFRGs:**  
mass-independent  
Infant weight-loss



# A Volume Density Threshold for the Star-Forming Gas

© Gao & Solomon (2004), Wu+2005

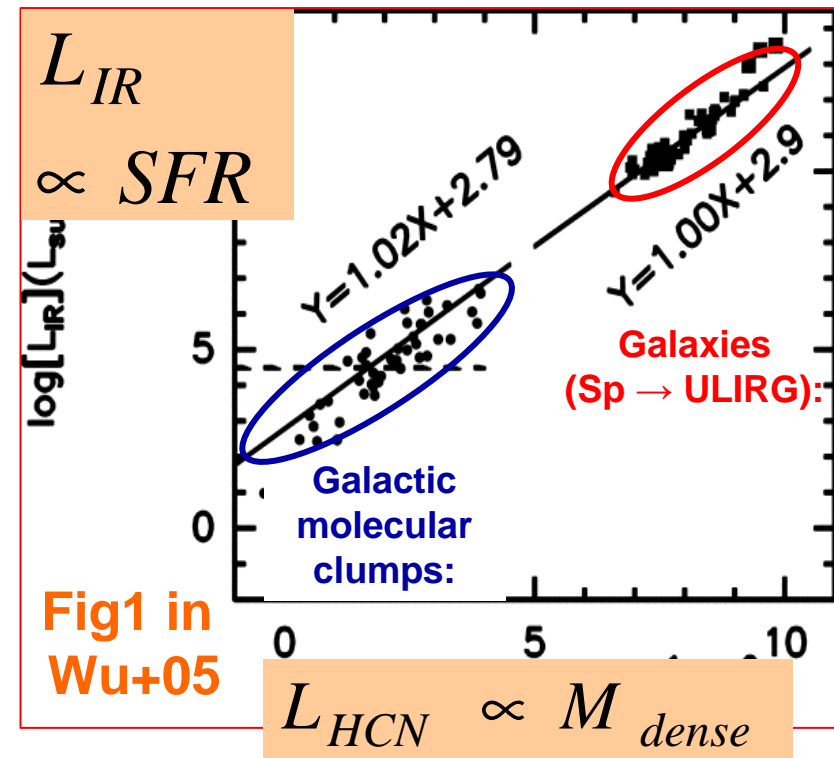
→ HCN mapping of entire galaxies  
+ Galactic individual molec clumps

➔ the SFR scales as the mass of dense molecular gas:  $n_{\text{H}_2} > 3 \cdot 10^4 \text{cm}^{-3}$

© Lada, Lombardi & Alves (2010)

→ comparison of IR extinction maps of molecular clouds with their census of Young Stellar Objects

➔ the SFR scales as the mass of dense molecular gas:  $n_{\text{H}_2} > 10^4 \text{cm}^{-3}$



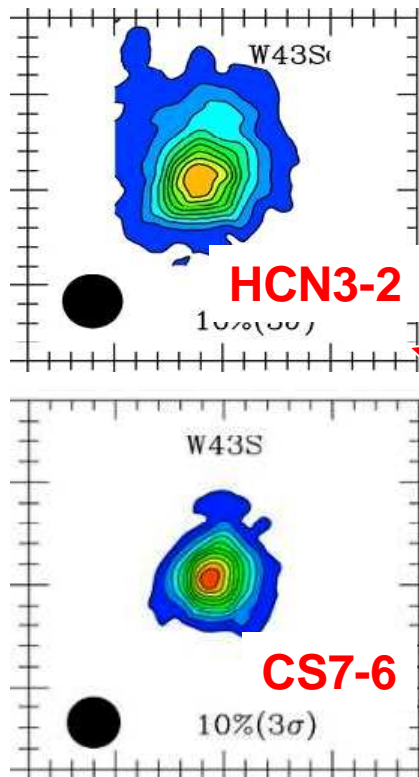
- CFRGs of about constant mean volume density ( $n_{\text{H}_2} = \text{few } n_{\text{th}}$ )
- Conclusion identical as for the tidal field impact analysis (Parmentier & Kroupa 2011)

Dense star-forming gas vs diffuse quiescent molecular gas

- Slopes of the cloud and cluster mass functions
- Slope of the Kennicutt-Schmidt law

# CFRGs - Molecular Clump Mapping: Do Not Mix !

Figs 9 and 21 Wu+2010



Star-forming region: W43S

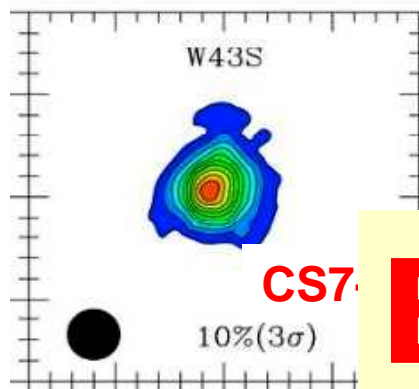
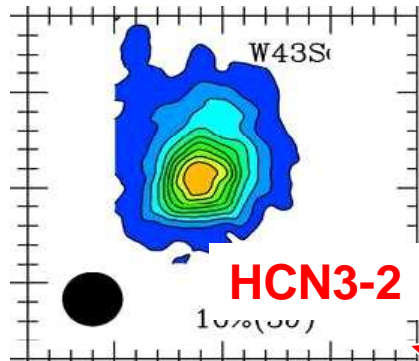
Tracers	FWHM [pc]	log(n [cm <sup>-3</sup> ])
HCN1-0	1.8	3.46
CS2-1	1.4	3.68
HCN3-2	0.6	4.50
CS7-6	0.3	5.21

● ≠ tracers probe ≠ molecular clump regions, with higher densities corresponding to inner, smaller regions.

● To identify a mass-radius diagram of molecular clumps as the mass-radius diagram of the star clusters they are forming is not as straightforward as sometimes quoted in the literature

# CFRgs - Molecular Clump Mapping: Do Not Mix !

Figs 9 and 21 Wu+2010



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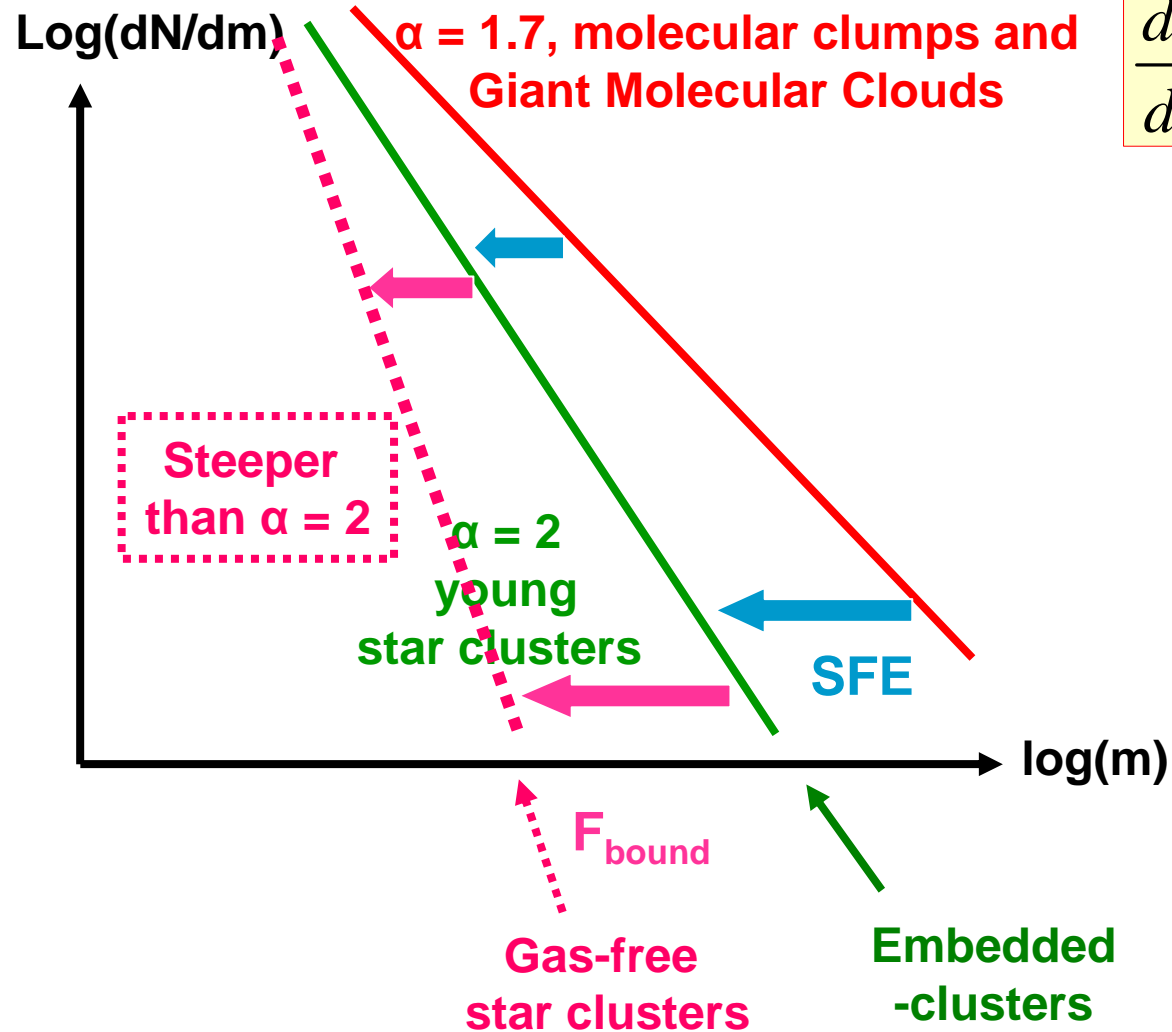
**BEWARE !!**

molecular clump  
densities  
smaller regions.

● To identify a mass-radius diagram of molecular clumps as the mass-radius diagram of the star clusters they are forming is not as straightforward as sometimes quoted in the literature



# From the mass function of GMCs/clumps to that of gas-free star clusters ...



$$\frac{dN}{dm} \propto m^{-\alpha}$$

Mass-varying SFE:  
lower SFE at higher  
cloud/clump mass ??

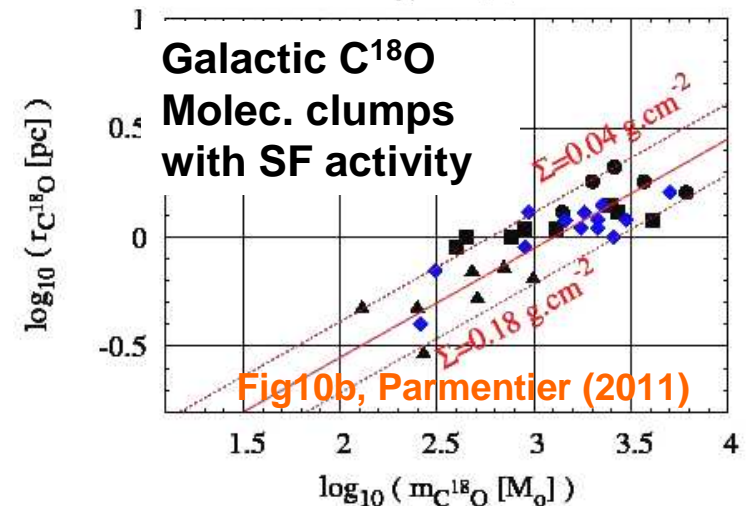
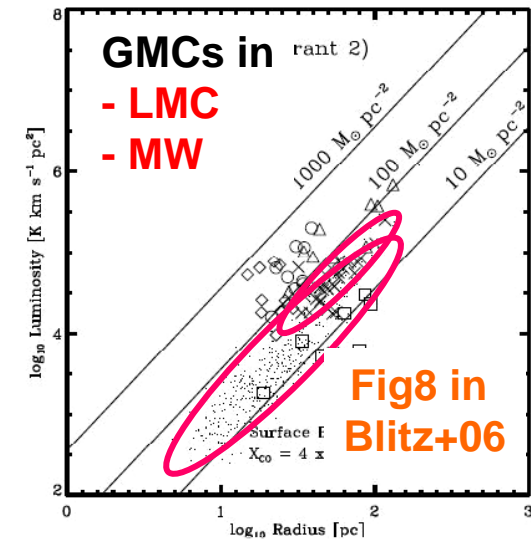
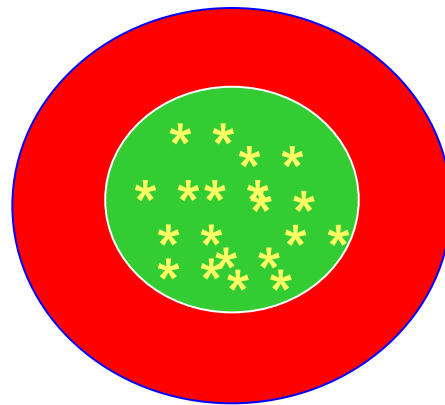
But then  
mass-varying  
 $F_{\text{bound}}$  too ??

# From the mass function of GMCs/clumps to that of gas-free star clusters ... with a volume density threshold for star formation

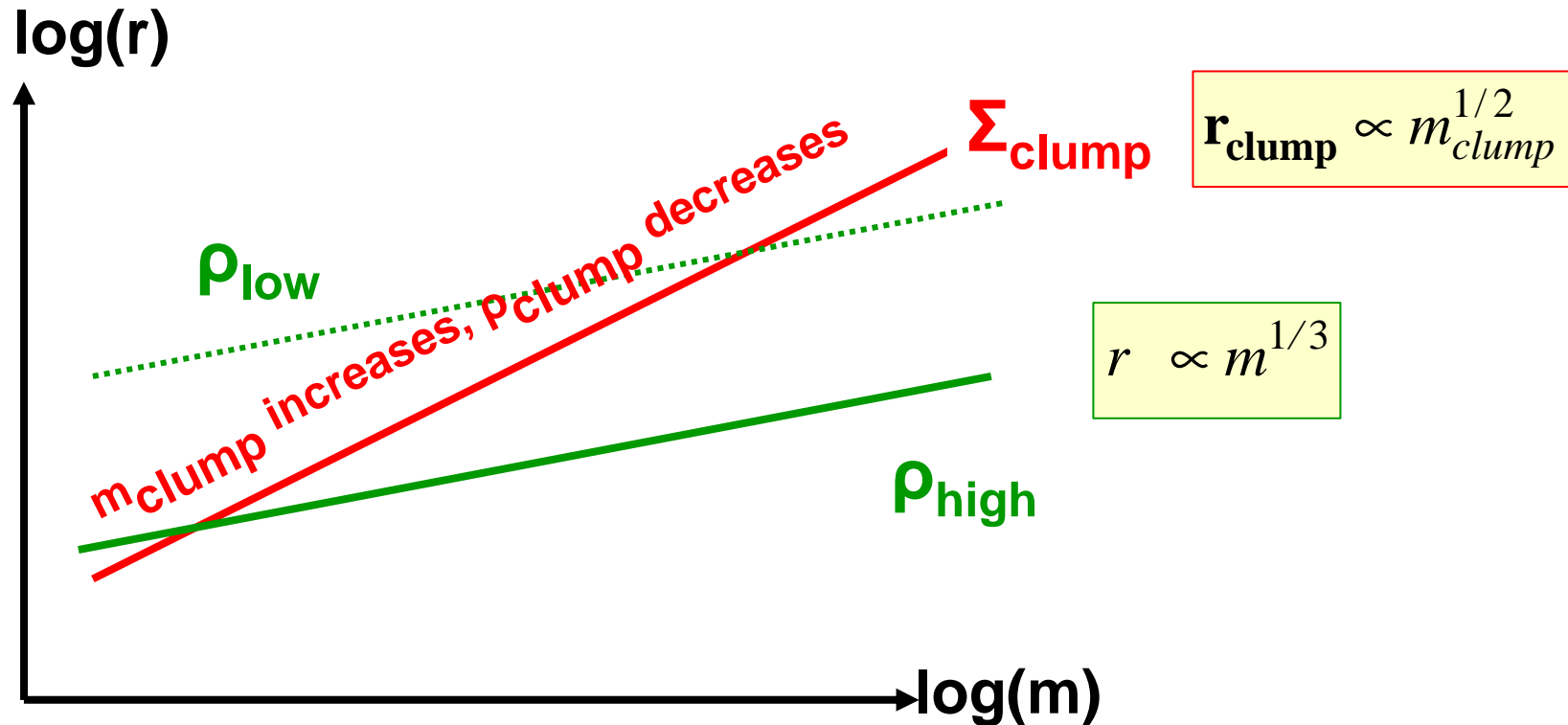
➤ Cluster-forming regions:  
**constant mean volume density**  
 (tidal field impact analysis)

➤ GMCs and  
 ➤ Molecular clumps with signs of SF activity:  
**constant mean surface density**

- Larson 1981
- Blitz+ 2006
- Heyer+ 2009



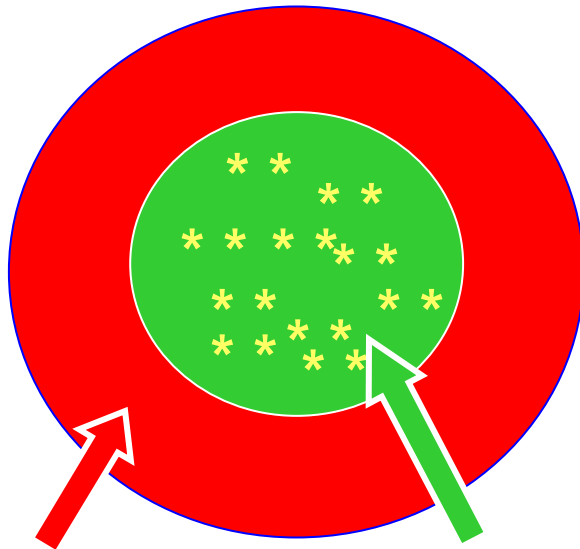
# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters



- Constant mean **surface** density clumps
- a clump of **higher mass** has a **lower fraction** of its mass above a given volume density threshold

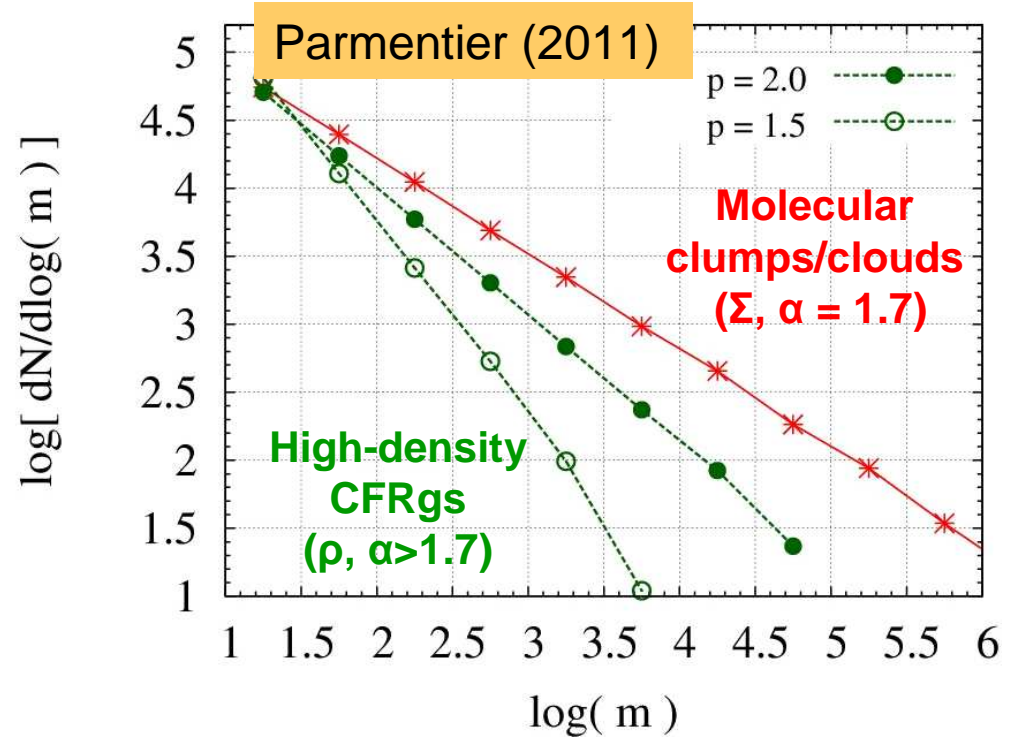
# From the Mass Function of Molecular Clumps to that of Embedded Star Clusters

**Molecular clumps:  
2-zone model**



**low-density  
outer  
envelope:**  
 $n_{\text{H}_2} < n_{\text{th}}$

**High-density  
cluster-forming  
region (CFRg):**  
 $n_{\text{H}_2} > n_{\text{th}}$



$$\rho_{clump}(r) \propto r^{-1.9} : \frac{m_{CFRg}}{m_{clump}} \propto m_{clump}^{-0.3}$$

**The local SFE must be measured over the  
CFRg, not over the whole molecular clump**

**Mueller+02:  
density index  $\approx 1.8$**

# Massive Star Formation (MSF) Limit

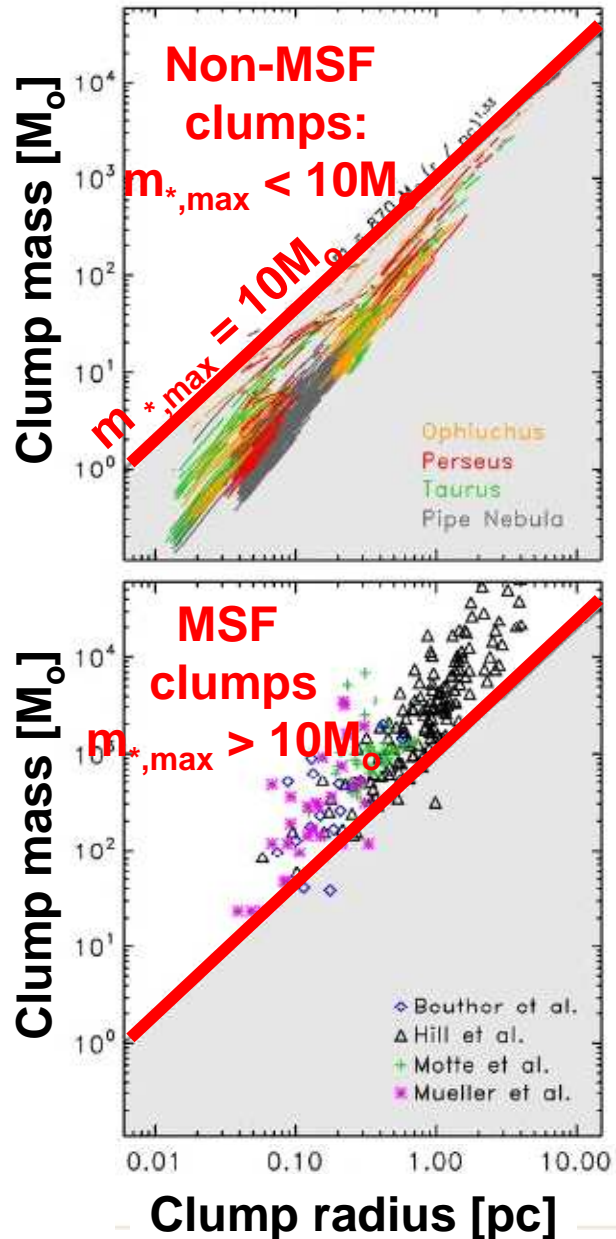


Fig2 and Eq1,  
 Kauffmann &  
 Pillai (2010)

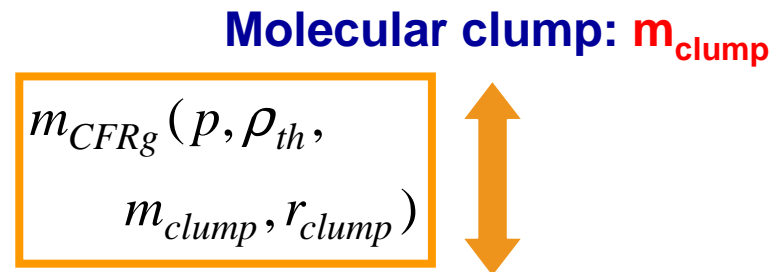
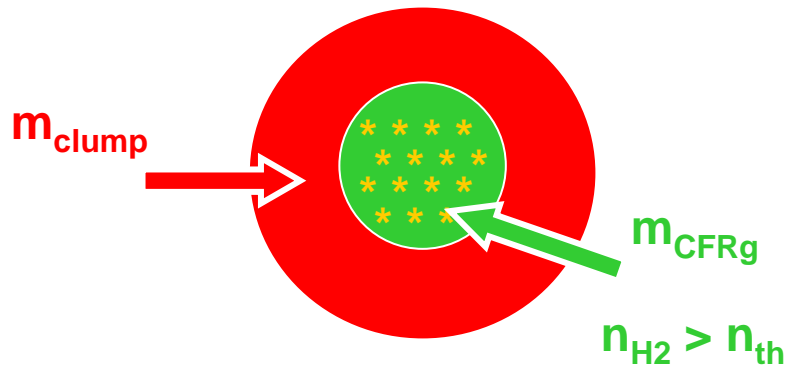
$$m_{clump} = 870M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33}$$

**Tool to define ALMA targets  
 for MSF studies**

**Intercept and slope?**



# What do we need to form a $10M_{\odot}$ star?



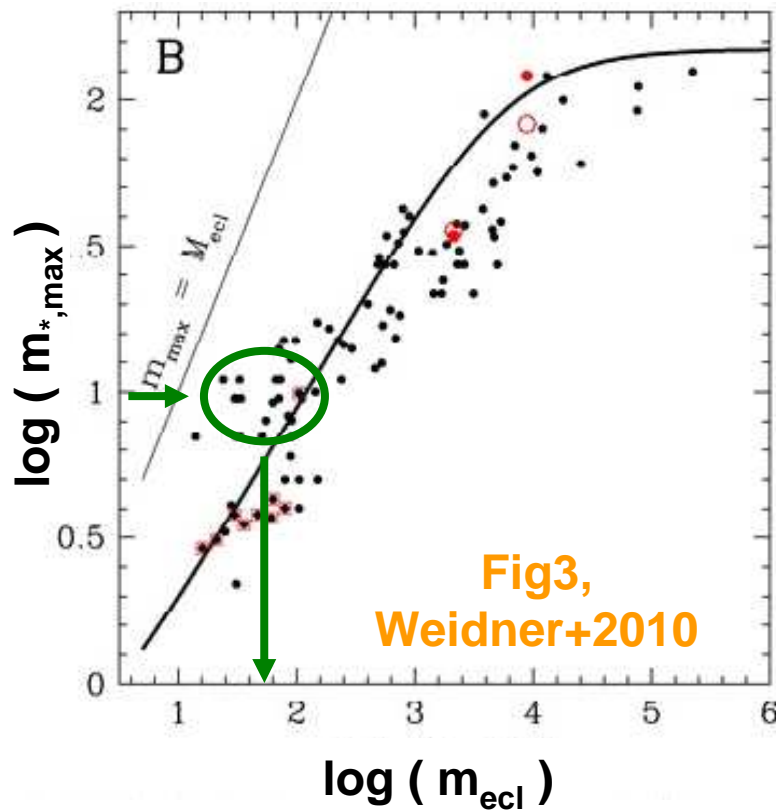
**Star-forming gas:**  
 $m_{\text{CFRg}} > 150M_{\odot}$

**SFE = 0.3**

**Embedded-cluster:**  
 $m_{\text{ecl}} > 50M_{\odot}$

**( $m_{\text{ecl}}, m_{*,\text{max}}$ )  
 relation**

**Most-massive star:**  
 $m_{*,\text{max}} > 10M_{\odot}$



# Massive Star Formation (MSF) Limit

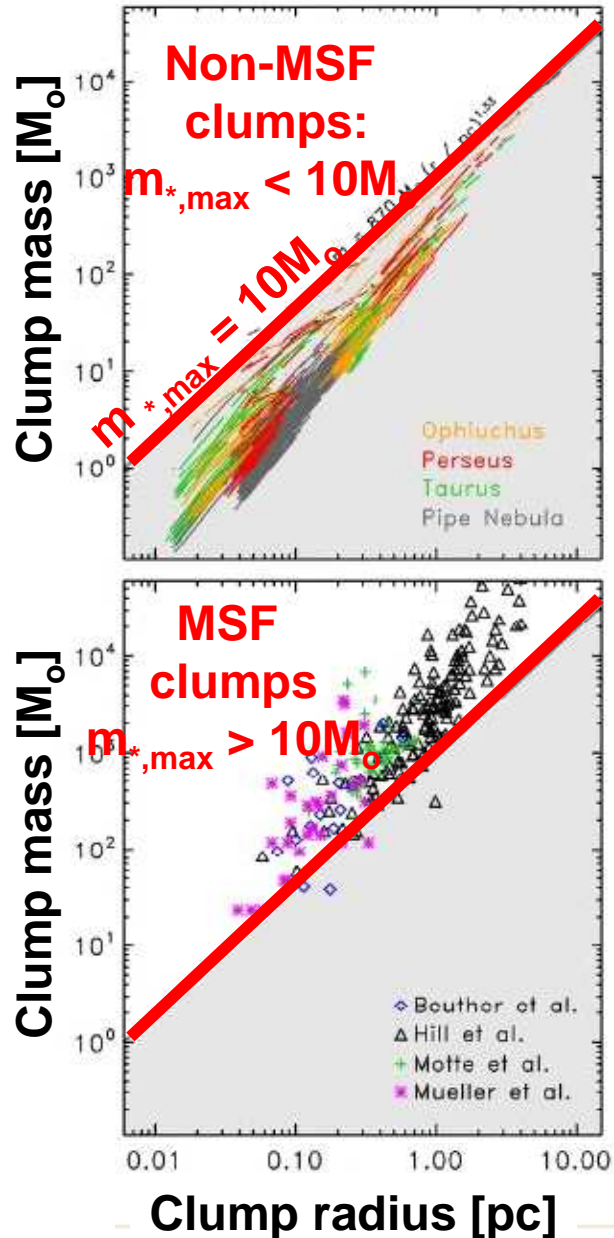


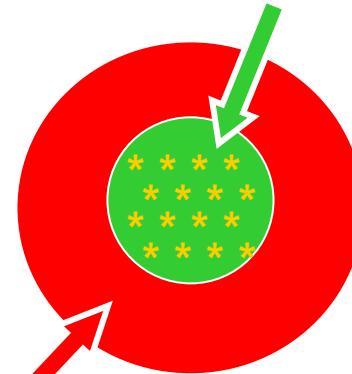
Fig2 and Eq1,  
 Kauffmann &  
 Pillai (2010)

Volume density threshold  
 for overall star formation:

$$n_{H_2} > n_{th}$$

$$m_* = 10M_{\odot} : m_{CFRg} = \frac{m_{ecl}}{SFE} \cong 150M_{\odot}$$

$$\langle n_{CFRg} \rangle = \text{few} \times n_{th}$$



$$m_{clump} = 870M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33}$$

# Massive Star Formation Limit

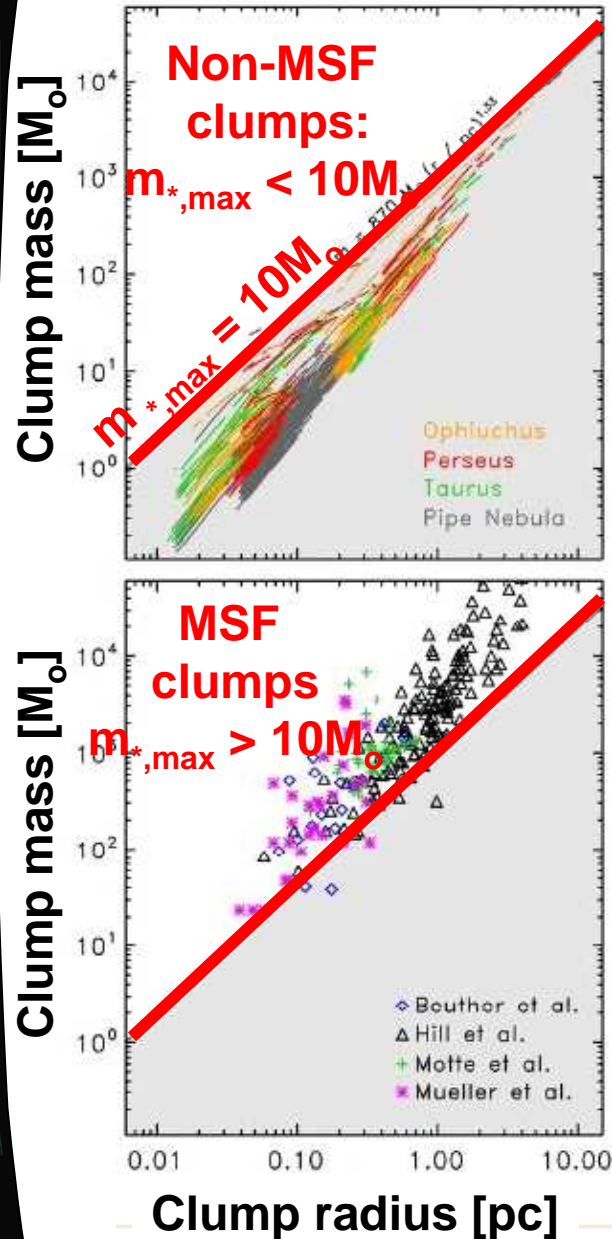
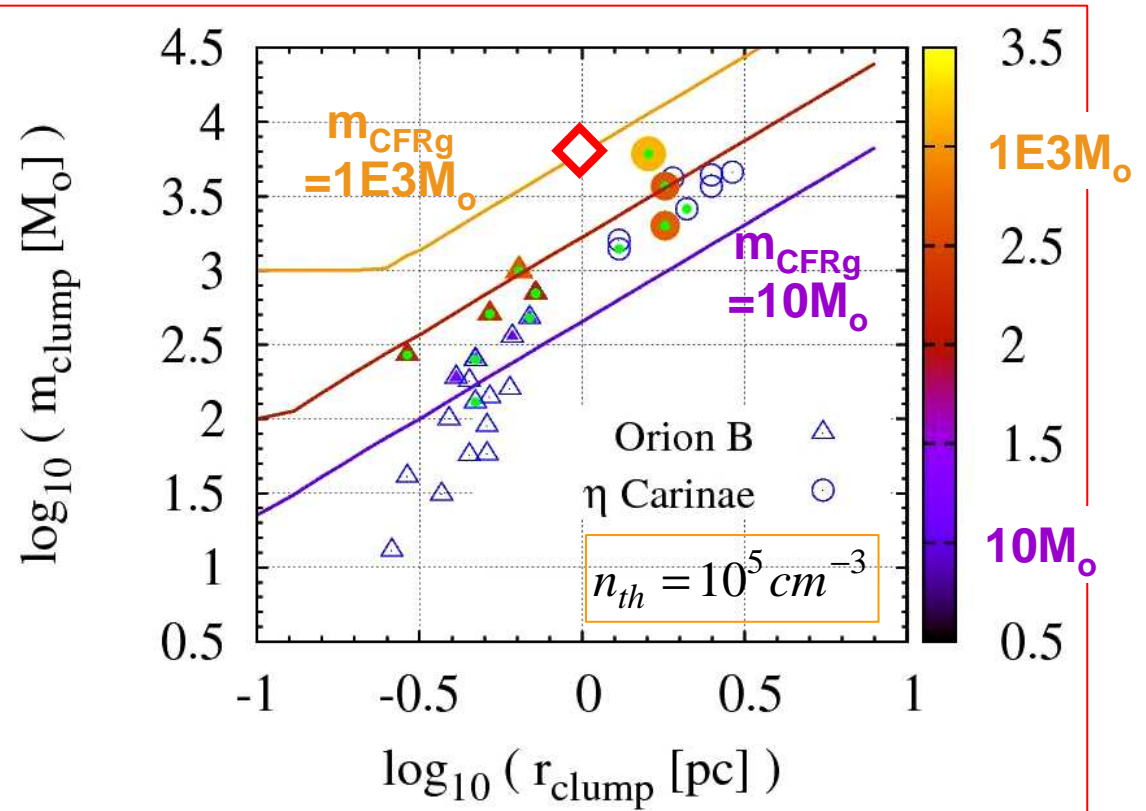


Fig2,  
 Kauffmann &  
 Pillai (2010)

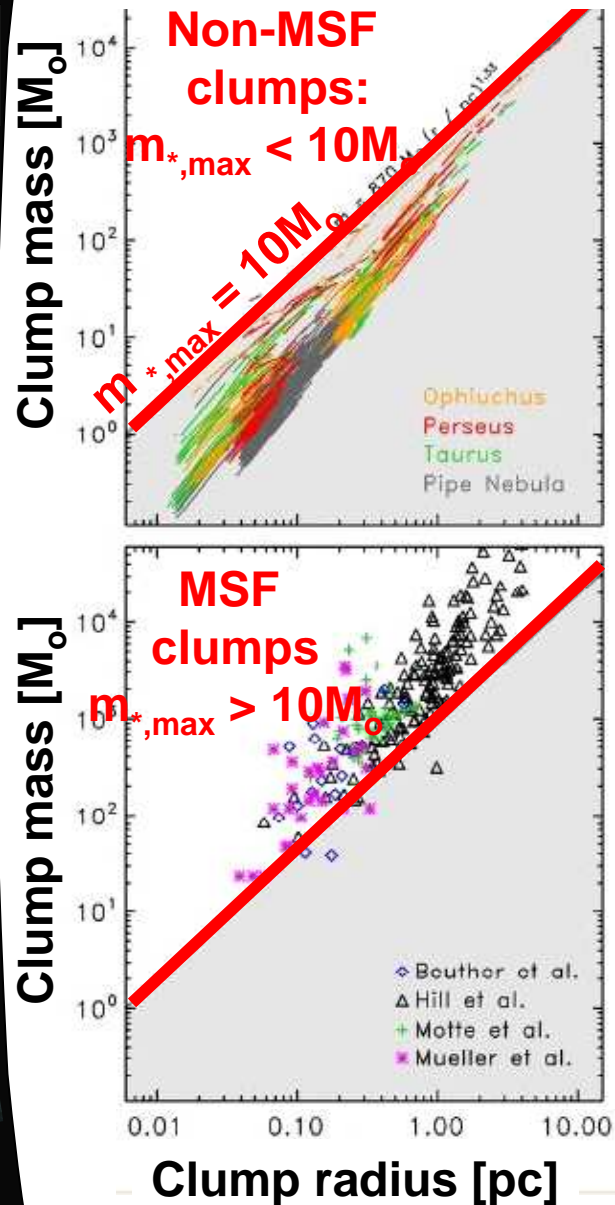
$$m_{clump} = \left(m_{CFRg}\right)^{p/3} \left(\frac{4\pi\rho_{th}}{3-p}\right)^{(3-p)/3} r_{clump}^{3-p}$$

Parmentier (2011), Eq.3

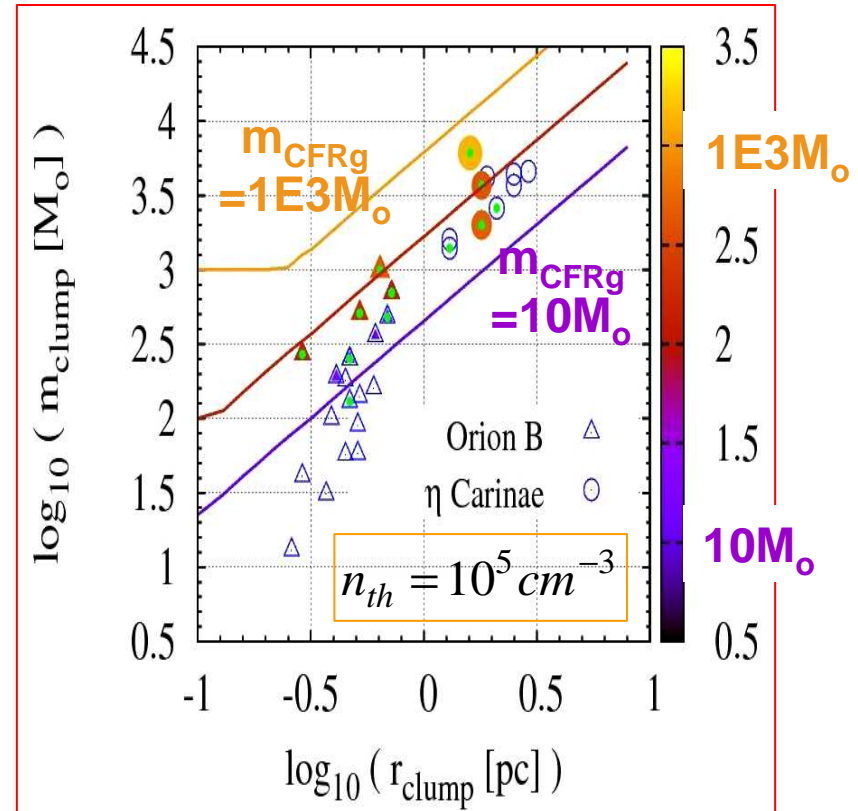


# Massive Star Formation Limit

Fig2, Kauffmann & Pillai (2010)



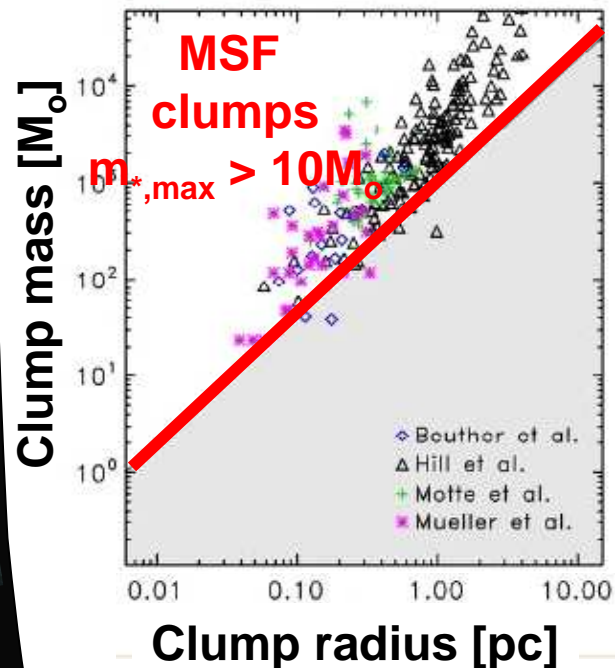
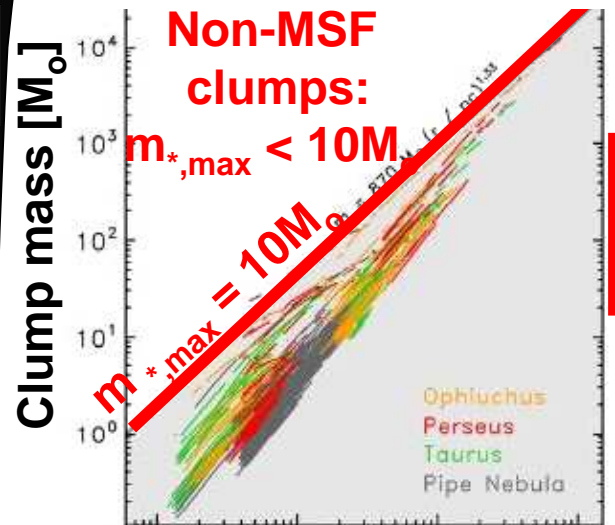
$$m_{clump} = 870M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33} = m_{CFRg}^{p/3} \left( \frac{4\pi\rho_{th}}{3-p} \right)^{(3-p)/3} r_{clump}^{3-p}$$





# Massive Star Formation Limit

Fig2, Kauffmann & Pillai (2010)



## Matching the slopes:

$$m_{clump} = 870 M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33} = m_{CFRg}^{p/3} \left( \frac{4\pi\rho_{th}}{3-p} \right)^{(3-p)/3} r_{clump}^{3-p}$$

- MSF limit:**  $p=1.7$  (Parmentier+, subm)  
**GMC/SC MFs:**  $p=1.9$  (Parmentier 2011)  
**Dust Cont. mapping:**  $p=1.8$  (Mueller+ 2002)

## Matching the intercepts:

$$m_{clump} = 870 M_{\odot} \left( \frac{r_{clump}}{pc} \right)^{1.33} = m_{CFRg}^{p/3} \left( \frac{4\pi\rho_{th}}{3-p} \right)^{(3-p)/3} r_{clump}^{3-p}$$

- Parmentier+, subm,  $m_{CFRg} = 150 M_{\odot}$
- Lada, Lombardi & Alves (2010):

$$n_{th,H2} = 10^4 \text{ cm}^{-3}$$



# Conclusions

## Properties of young star cluster systems

- sharp insights into the clustered mode of star formation
- star formation conditions determine what mass fraction clusters lose as they age
- information needed to reconstruct galaxy SFH
- time-variations ? (e.g. metallicity)

“Even a long journey starts with a one single step”  
Oriental saying

An exciting era has just started:  
HERSCHEL, ALMA, ...

